



SIGGRAPH 2024

DENVER+ 28 JUL — 1 AUG

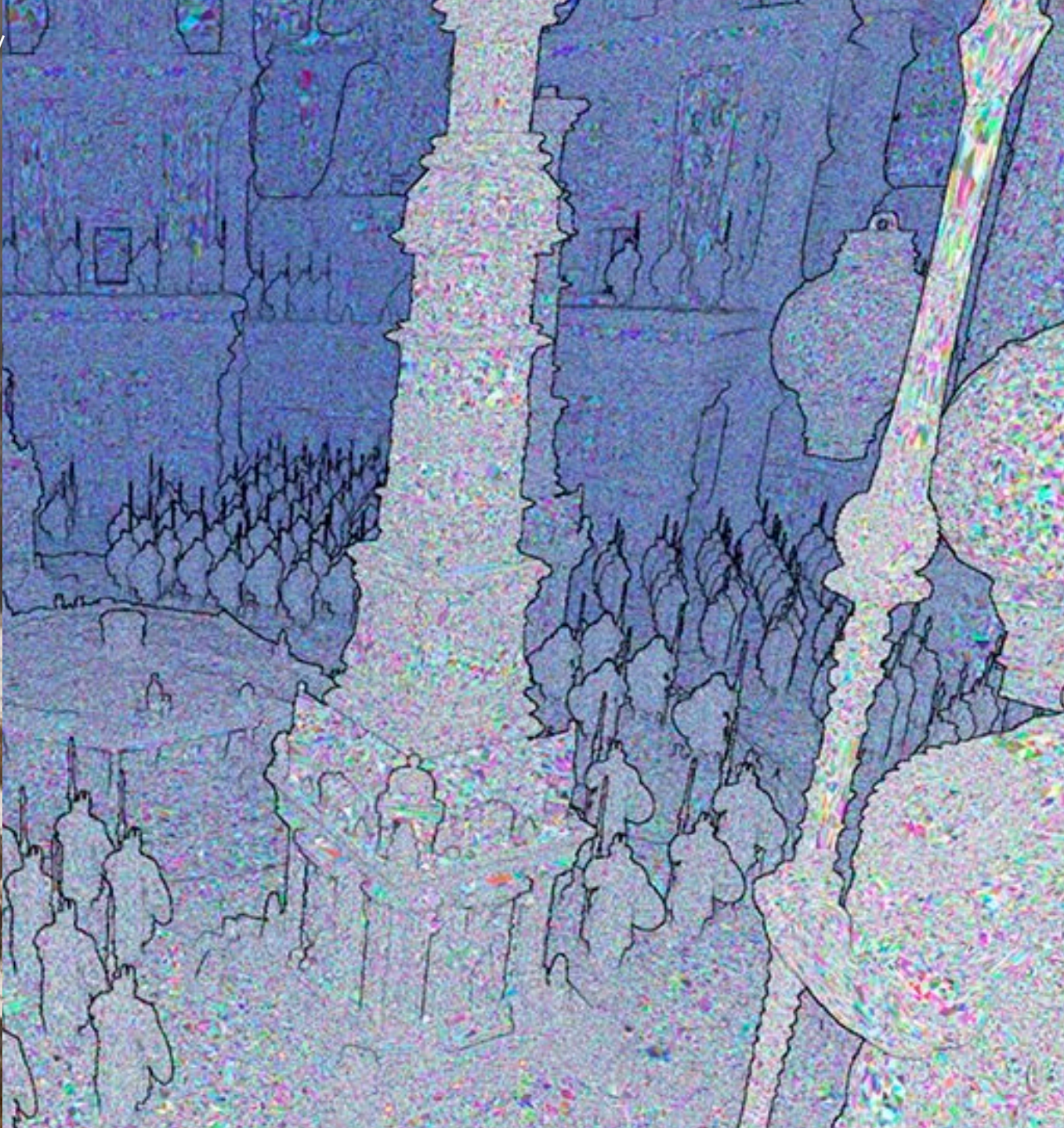
THE PREMIER CONFERENCE
& EXHIBITION ON
COMPUTER GRAPHICS &
INTERACTIVE TECHNIQUES

***FROM MICROFACETS TO PARTICIPATING
MEDIA: A UNIFIED THEORY OF LIGHT
TRANSPORT WITH STOCHASTIC GEOMETRY***

**DARIO SEYB¹, EUGENE D'EON², BENEDIKT BITTERLI²,
WOJCIECH JAROSZ¹**

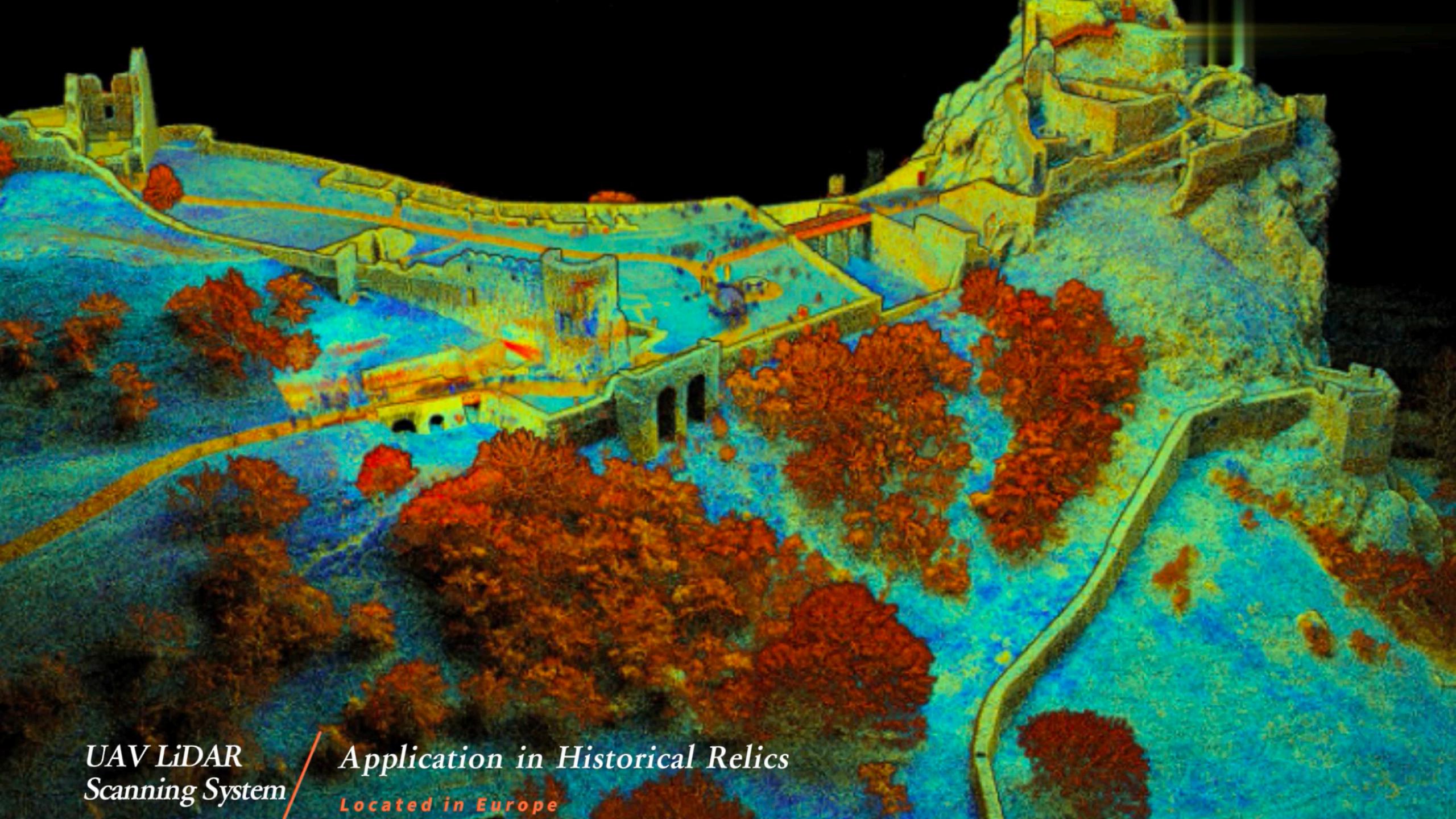
¹DARTMOUTH COLLEGE, ²NVIDIA











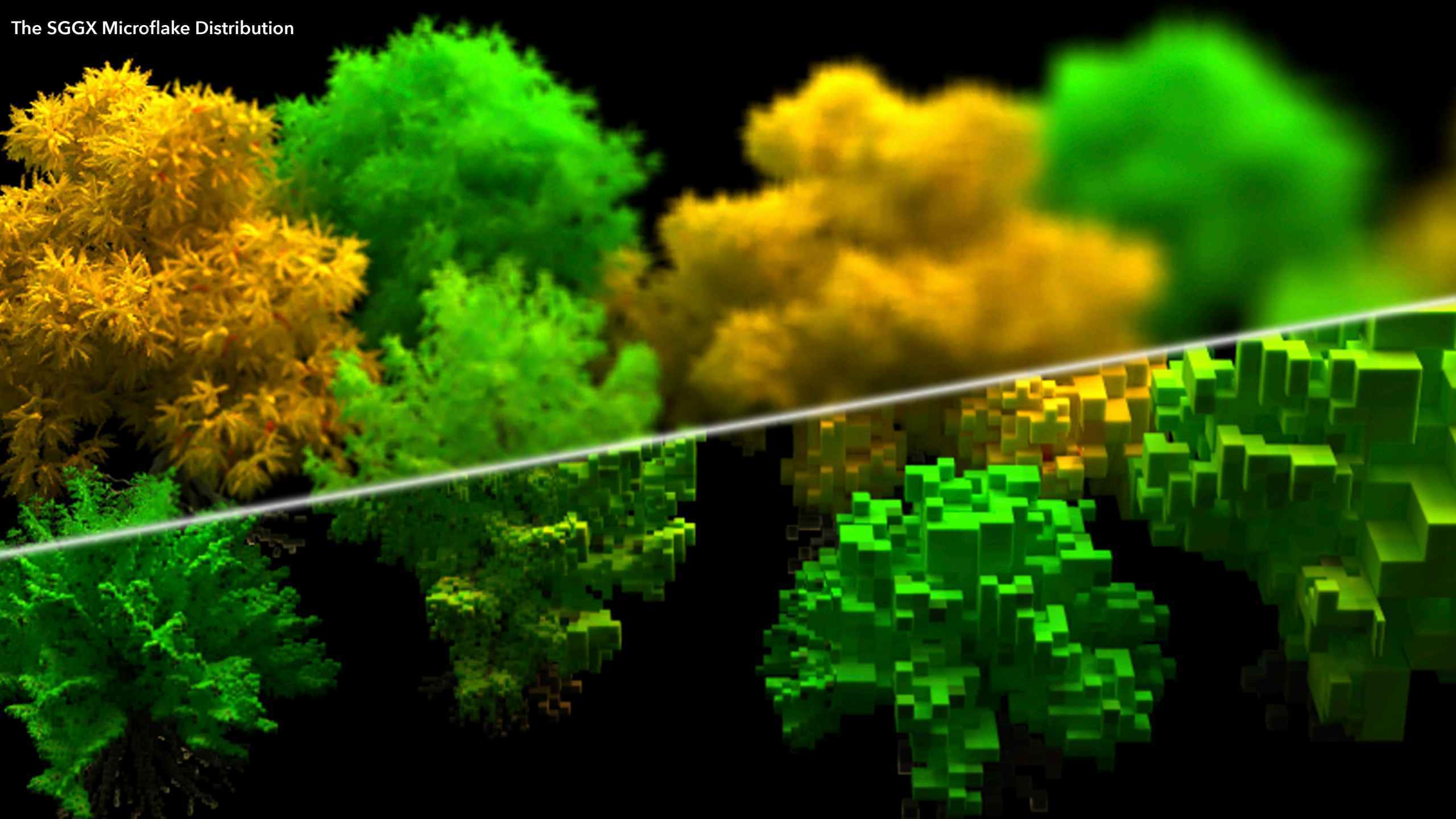
UAV LiDAR
Scanning System

Application in Historical Relics

Located in Europe



The SGGX Microflake Distribution



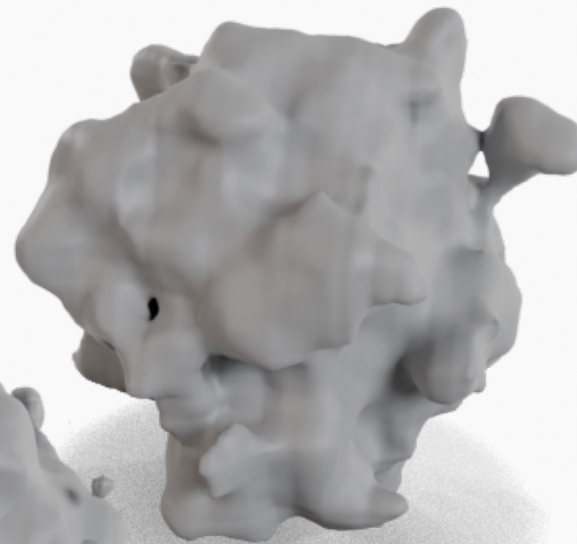
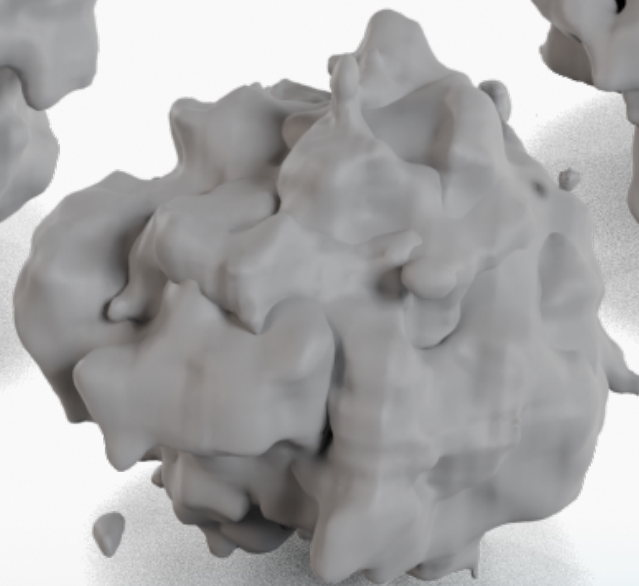
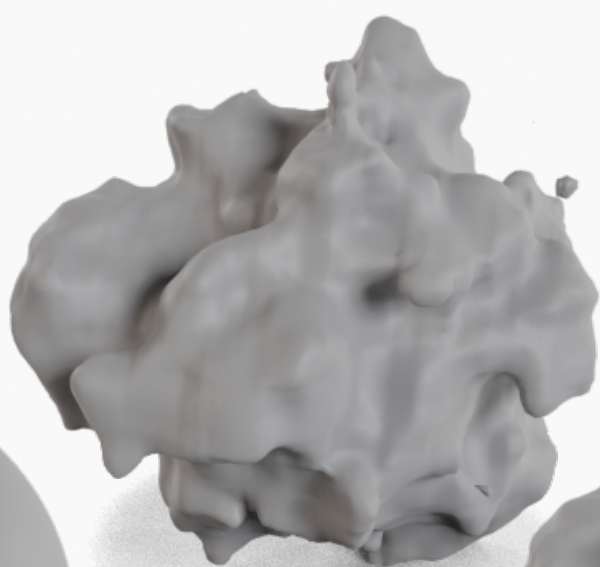
Lay the *foundations* for a new *geometry*
representation for *surfaces and volumes*.

GAUSSIAN PROCESS IMPLICIT SURFACES (GPIS)

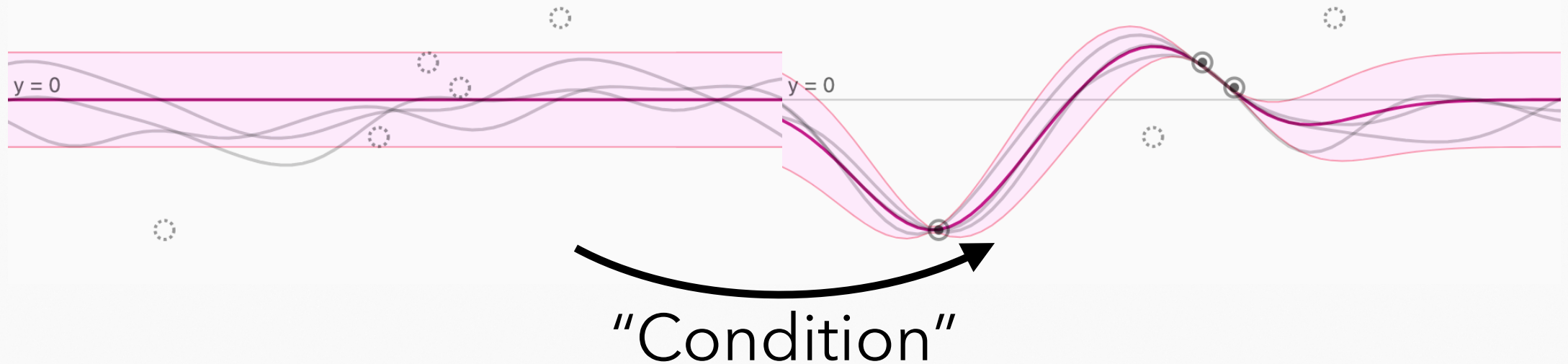
$$\{x \in \mathbb{R}^3 \mid f(x) = 0, f \sim \text{GP}\}$$



$$\{x \in \mathbb{R}^3 \mid \mu(x) = 0\}$$



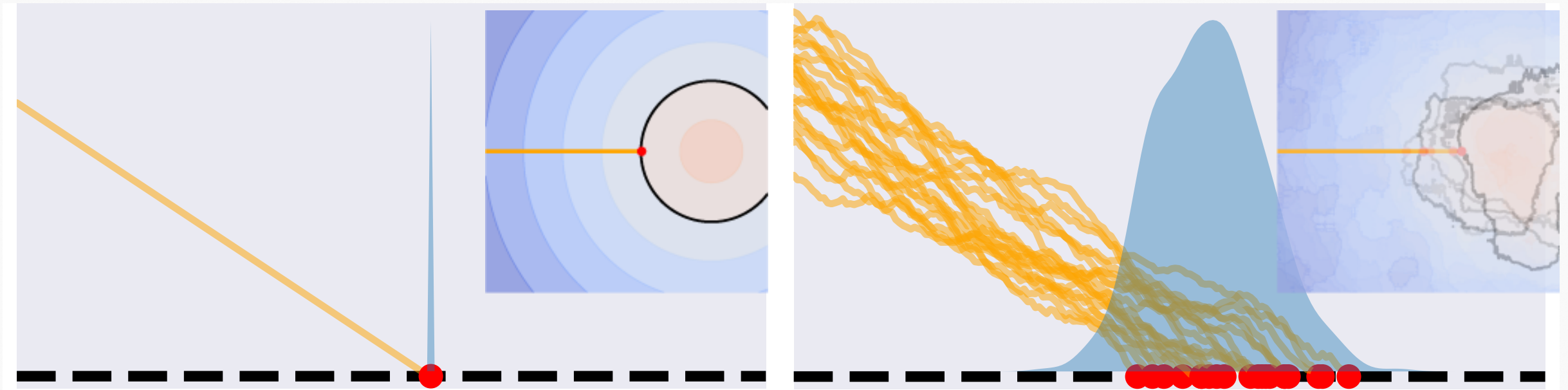
A distribution over *functions*



- Completely described by **mean function** and **covariance kernel**
- Closed under **linear transforms** (including derivatives)
- No relation to **Gaussian Splatting™**

Implicit Surface

Stochastic Implicit Surface

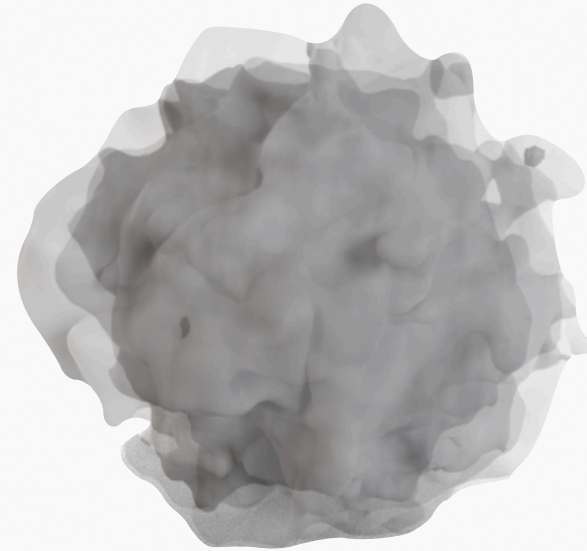


Special Case! $\sigma = 0$

$$E[\mathcal{L}]u$$

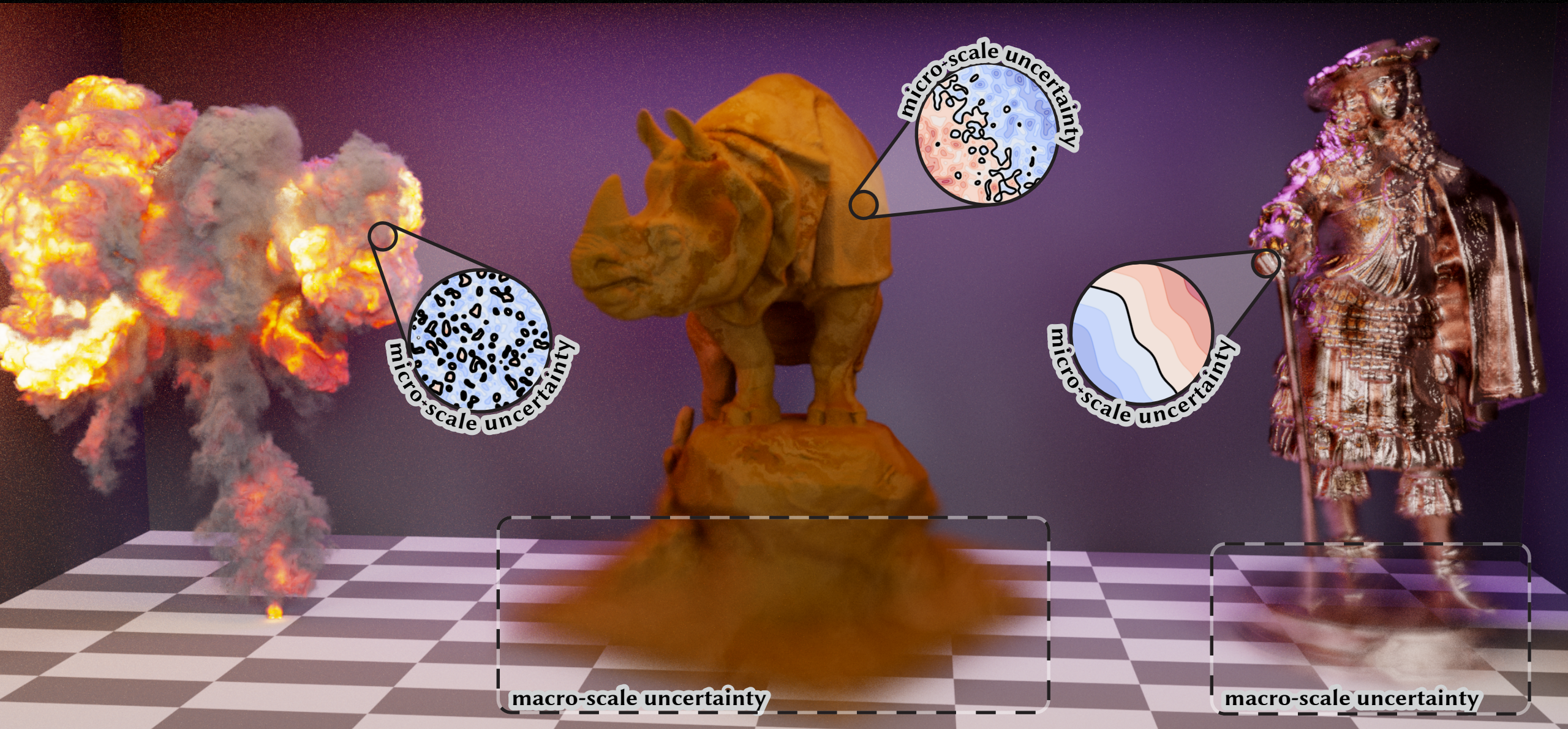


$$E[\mathcal{L}u]$$



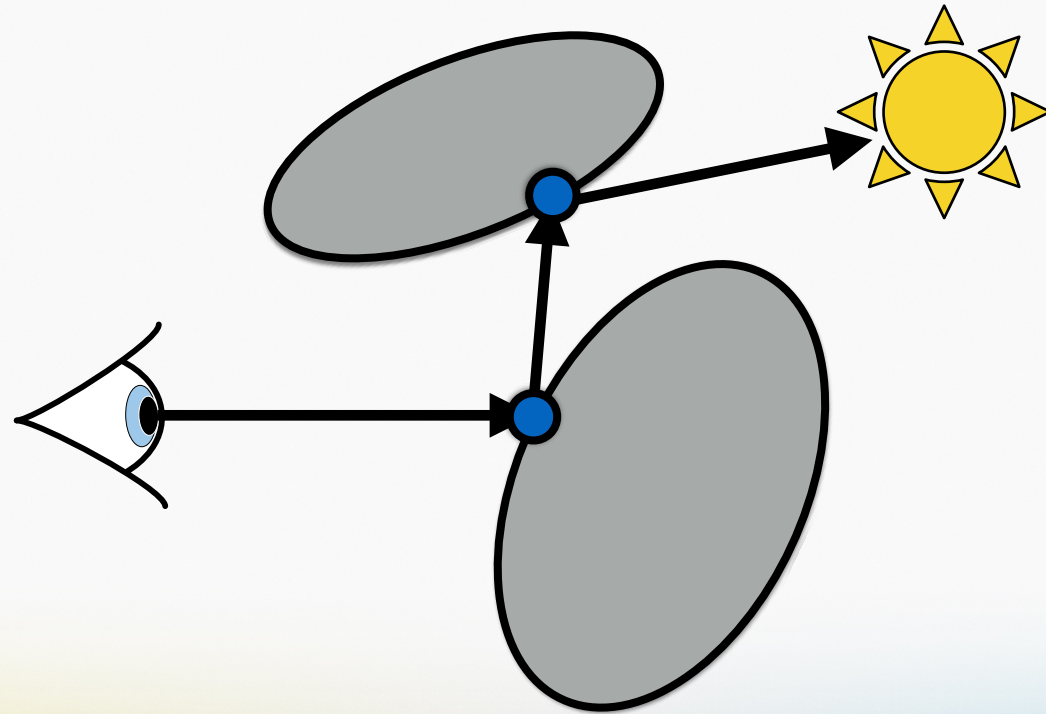
Remember: Light Transport is not linear in geometry!

LIGHT TRANSPORT IN STOCHASTIC IMPLICIT SURFACES

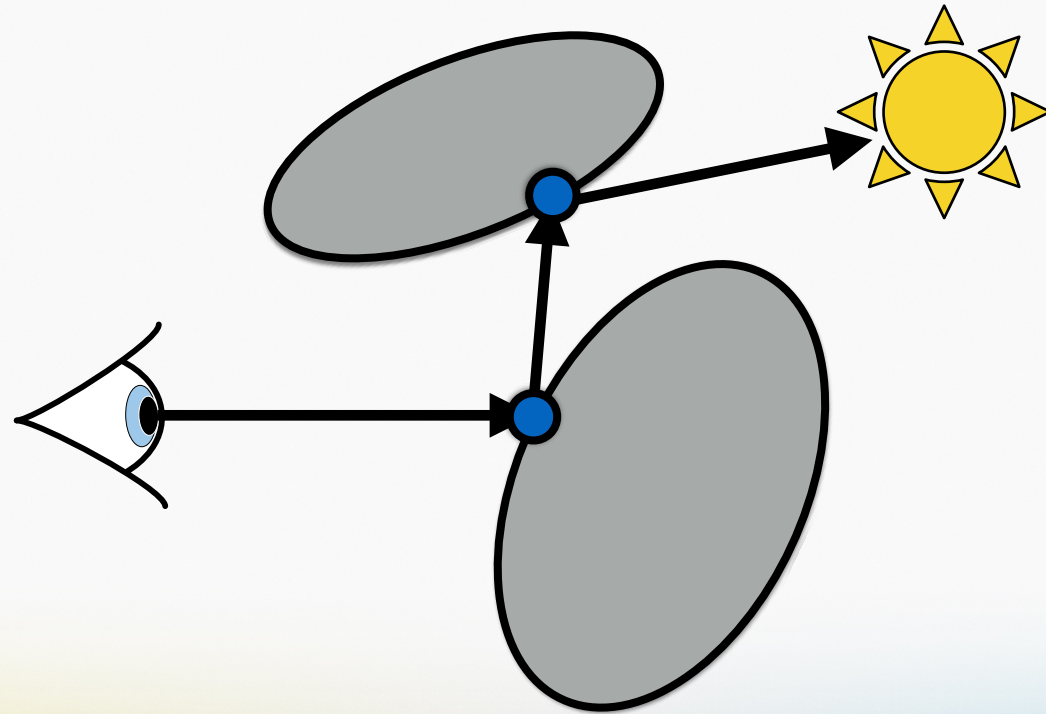


$$L_i(x, \omega) = \int_{\Omega} L_i(x_s, \omega_s) \rho(x_s, \omega_s, n_s) d\omega_s$$

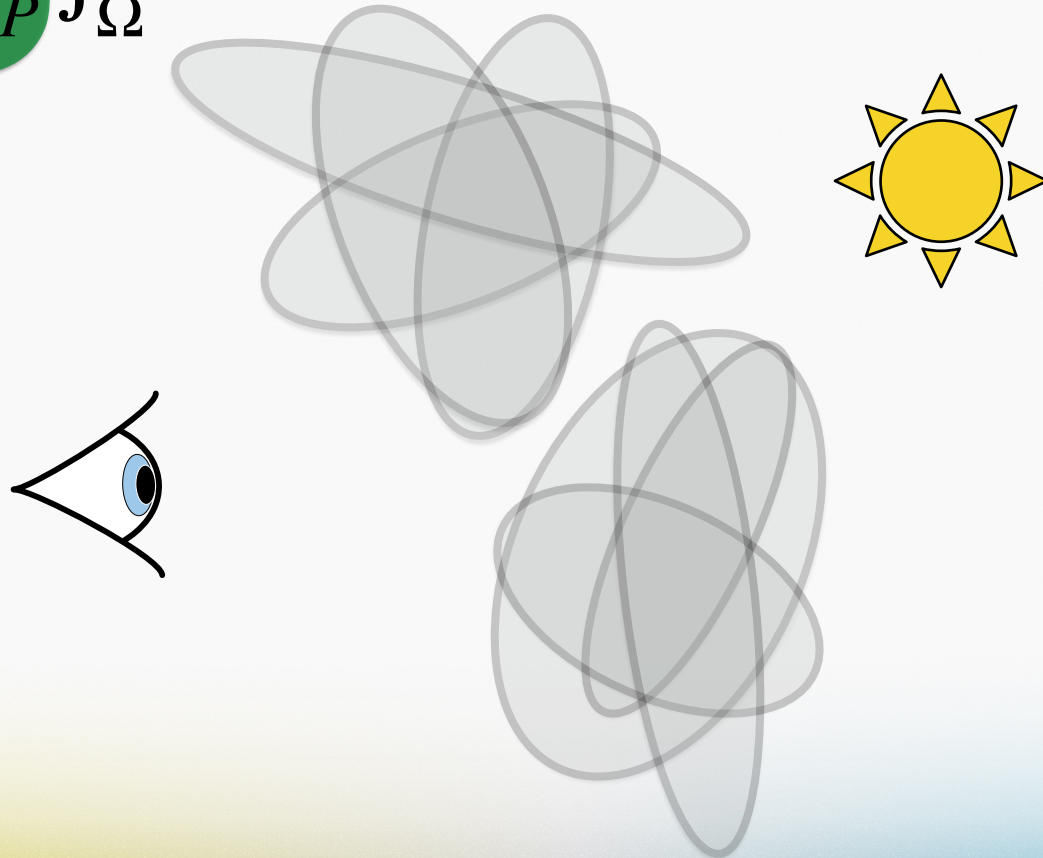
$$L_i(x, \omega) = \int_{\Omega} L_i(x_s, \omega_s) \rho(x_s, \omega_s, n_s) d\omega_s$$



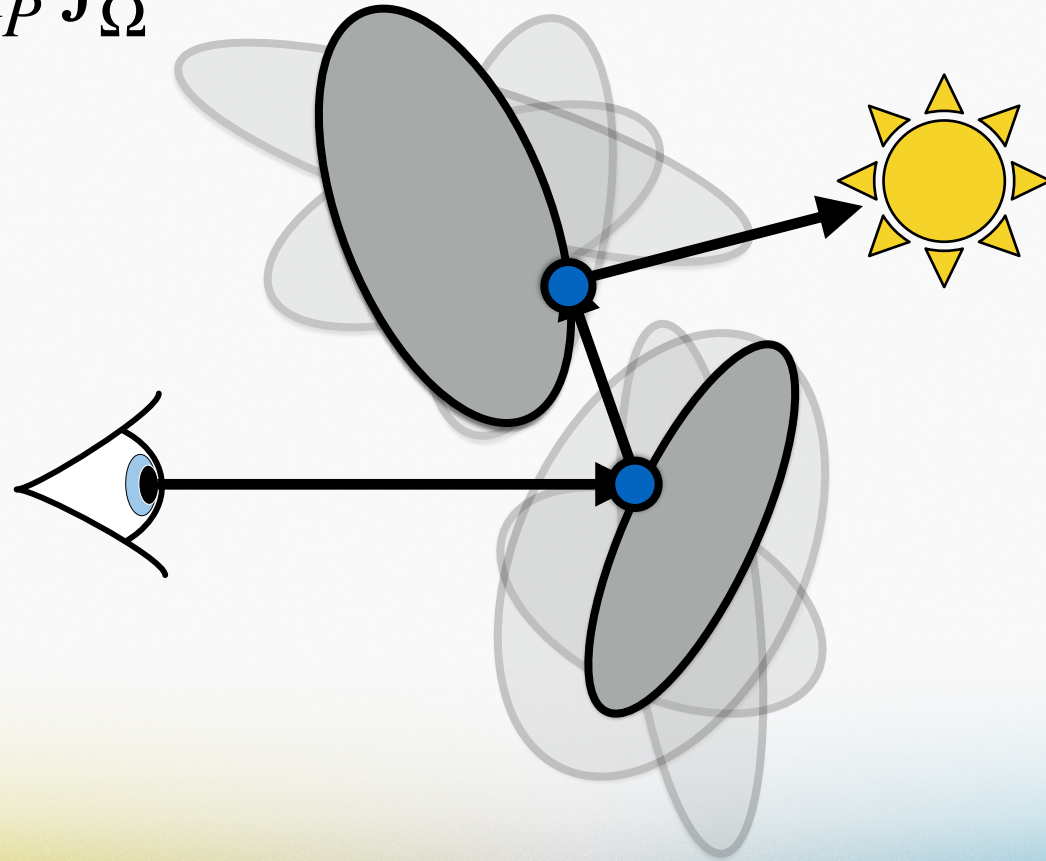
$$\langle L_i(x, \omega) \rangle_{GP} = \int_{GP} \int_{\Omega} L_i(x_s^f, \omega_s) \rho(x_s^f, \omega_s, n_s^f) d\omega_s d\gamma(f)$$



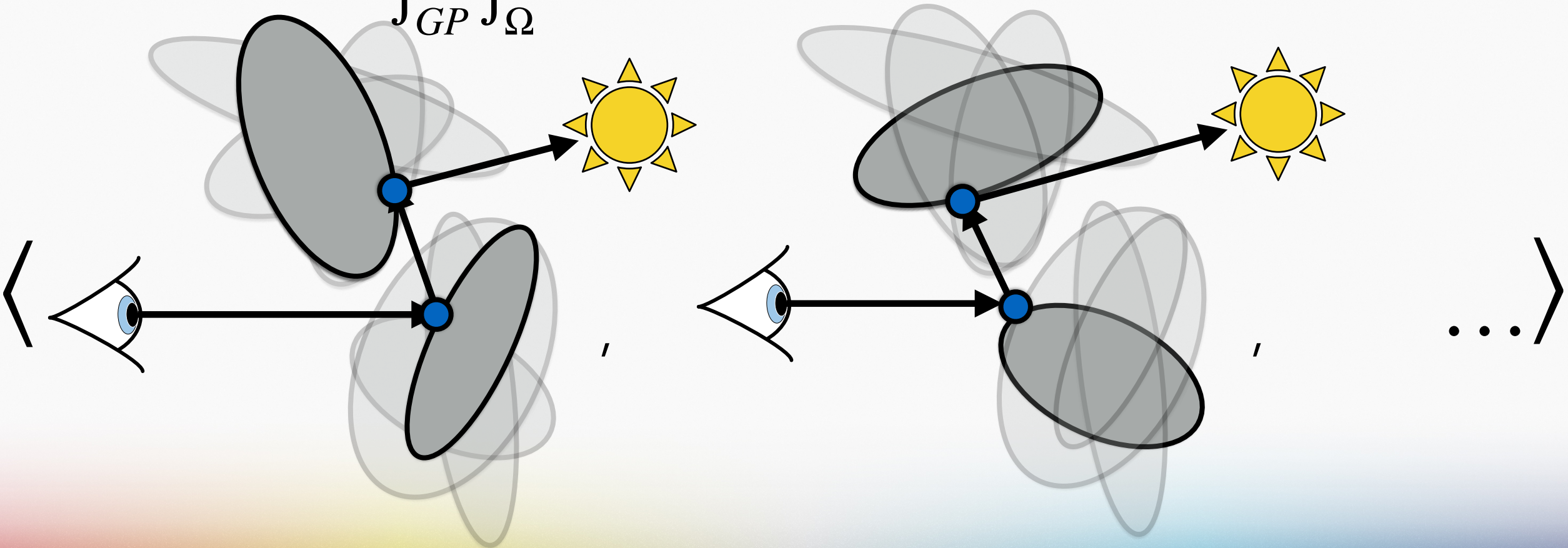
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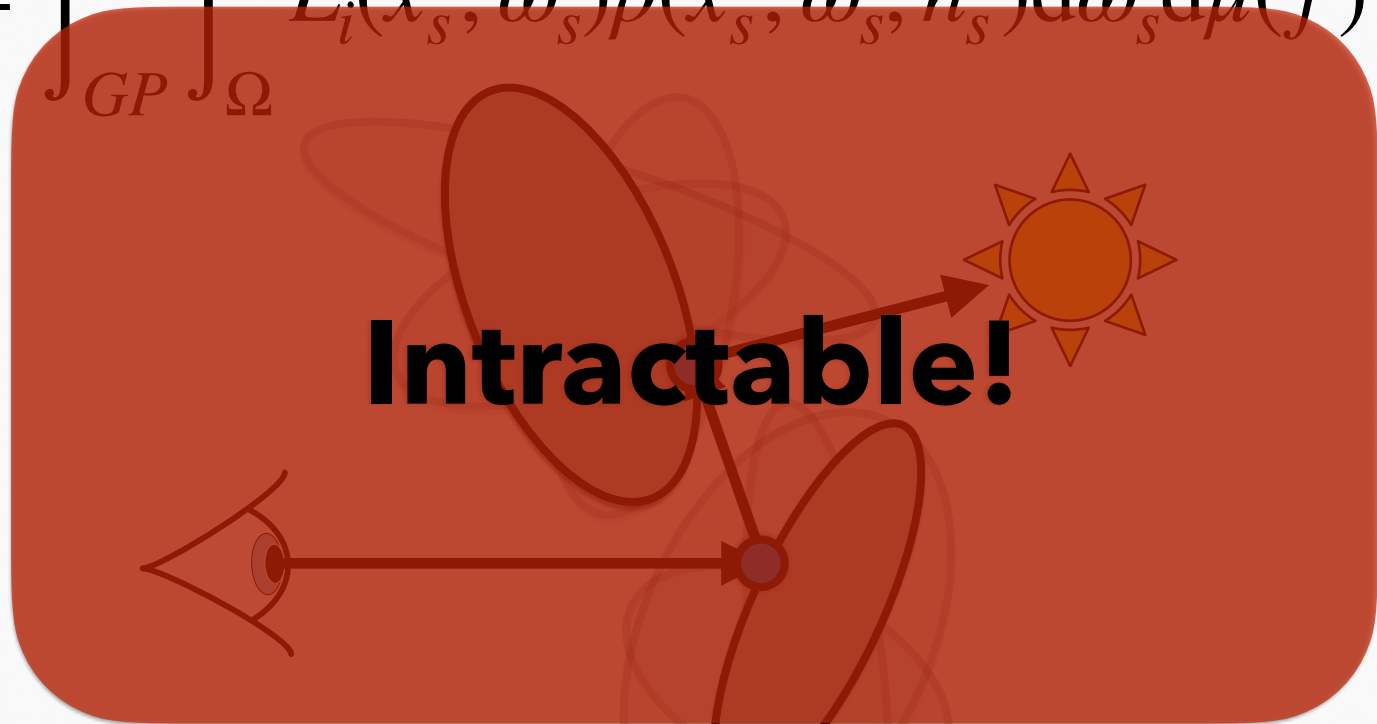
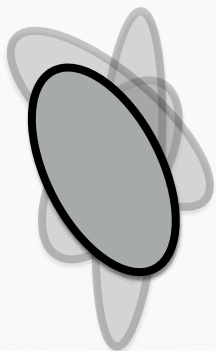
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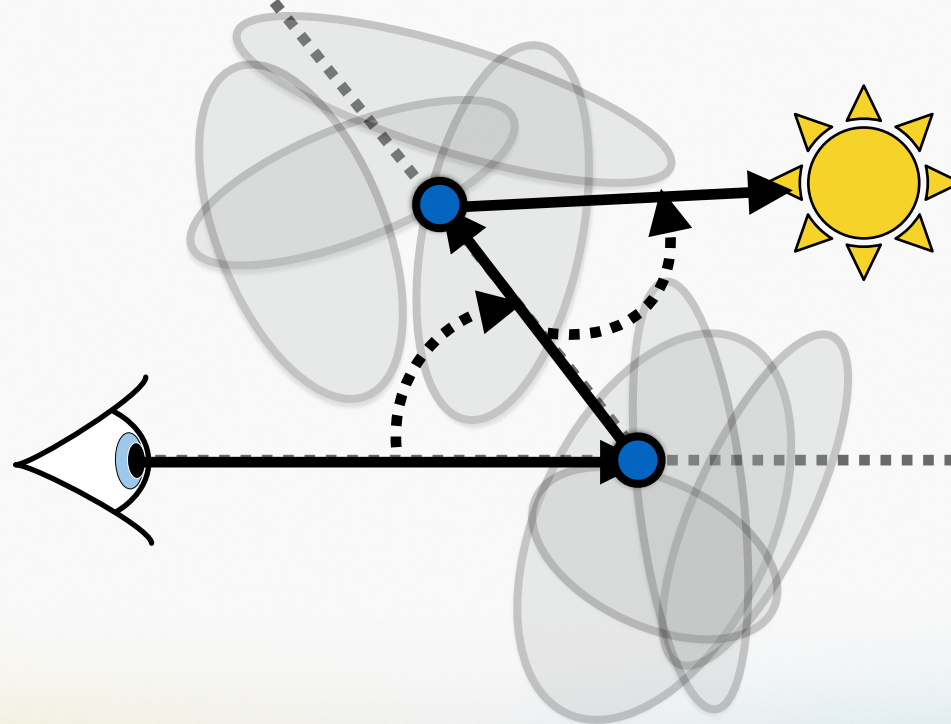
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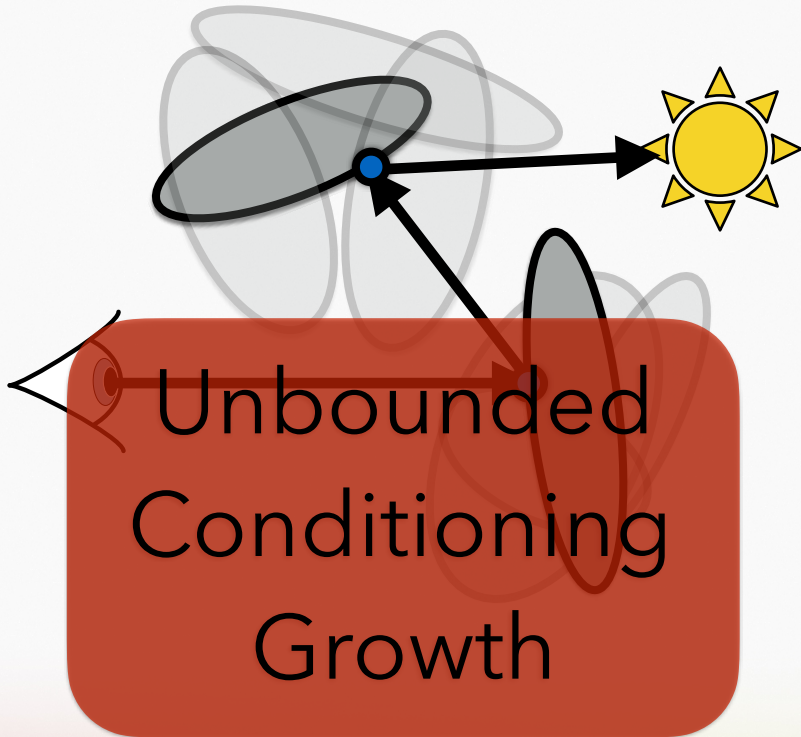
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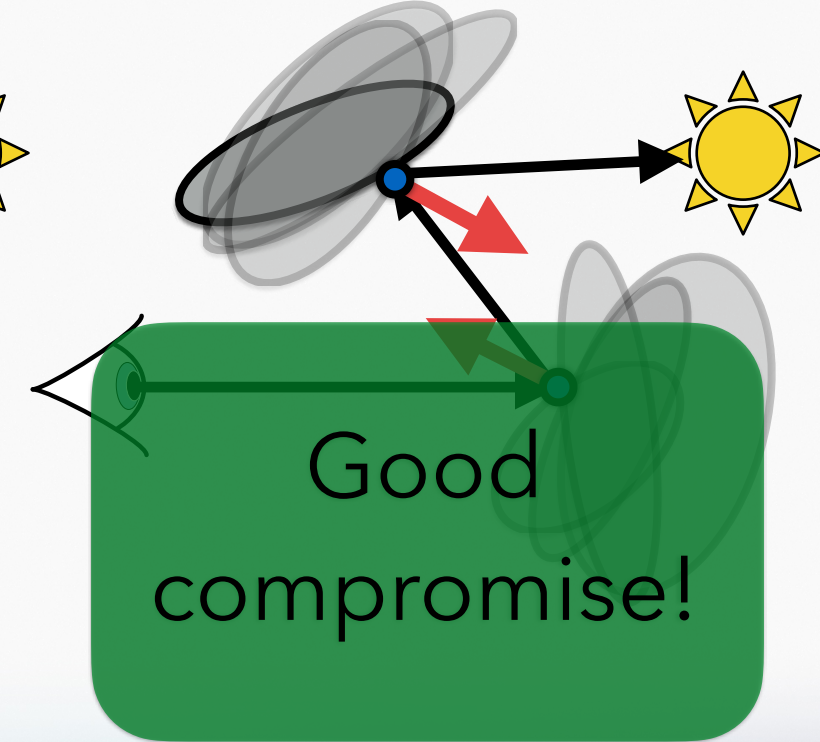
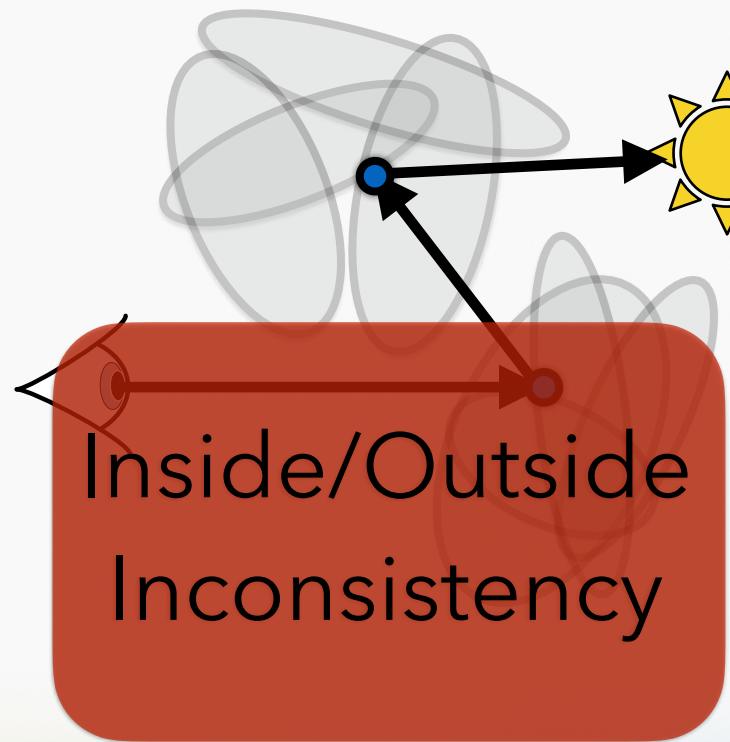
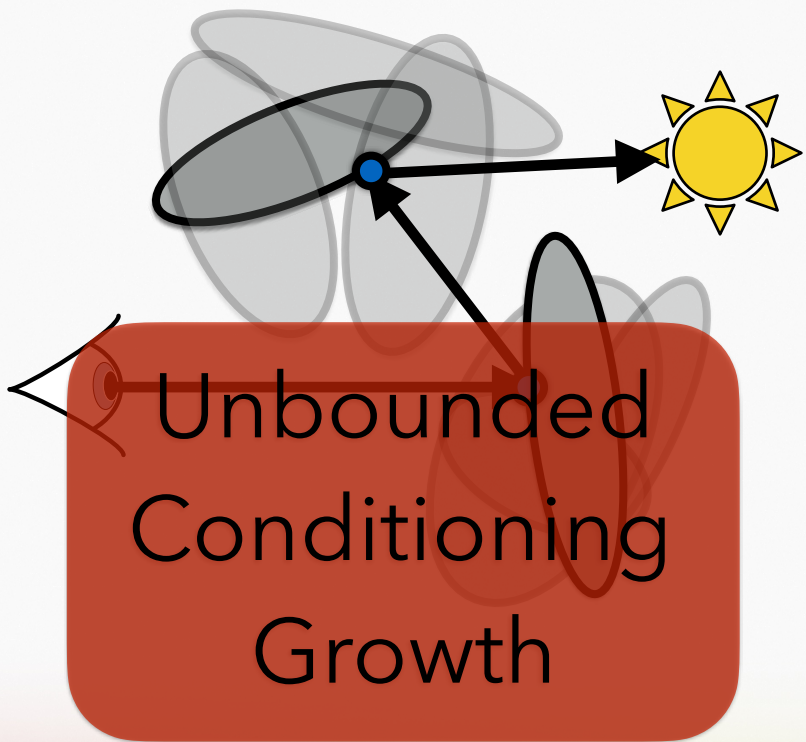
$$\langle L_i(x, \omega) \rangle_{GP} = \int_0^\infty \iint \langle L_i(x_s, \omega_s) \rangle_{|x_s n_s} \rho(x_s, \omega_s, n_s) p(x, \omega; x_s, n_s) d\omega_s dn_s ds$$



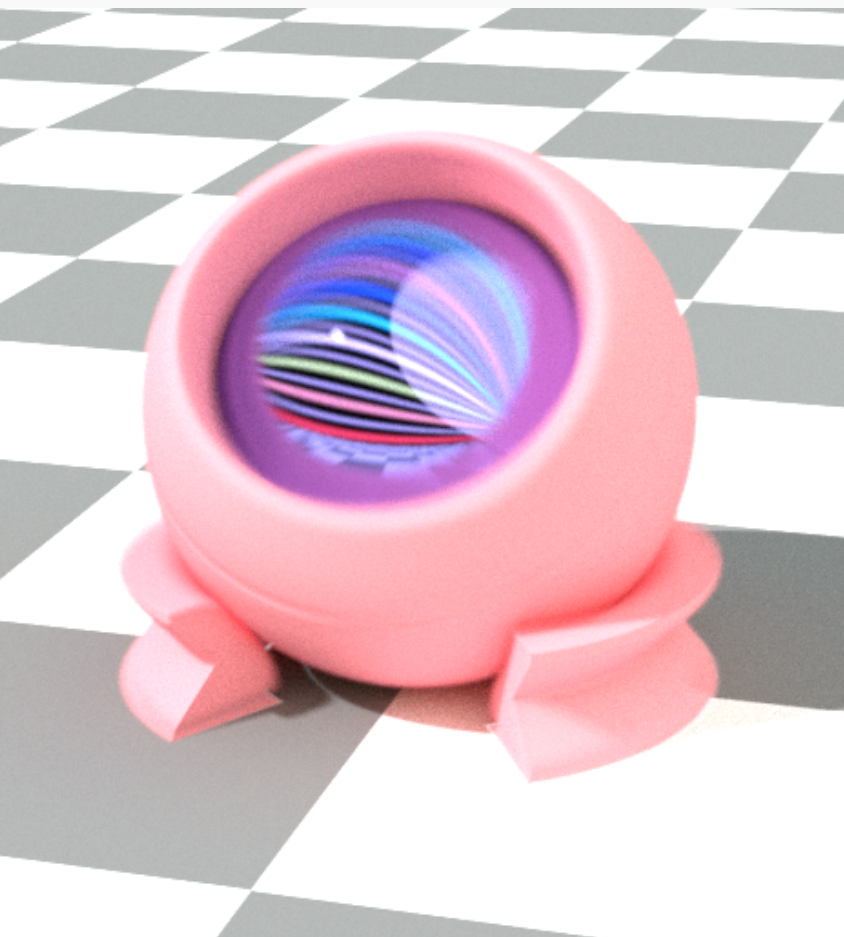
Globally Consistent



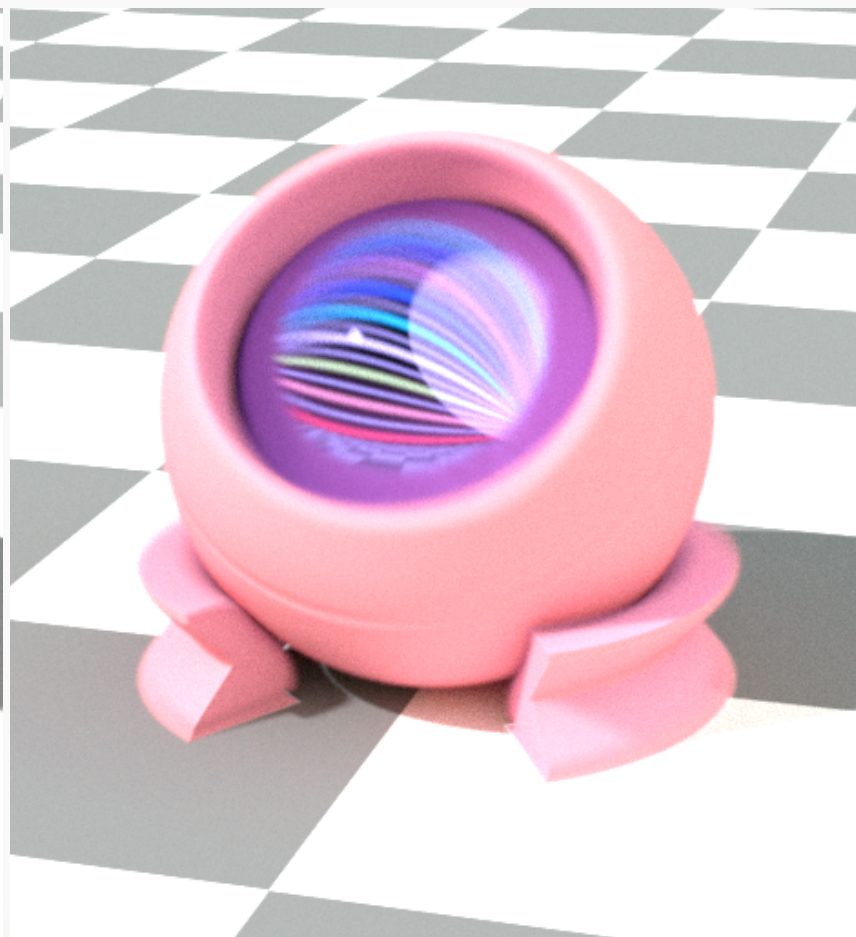
Globally Consistent Position Consistent + Normal Consistent



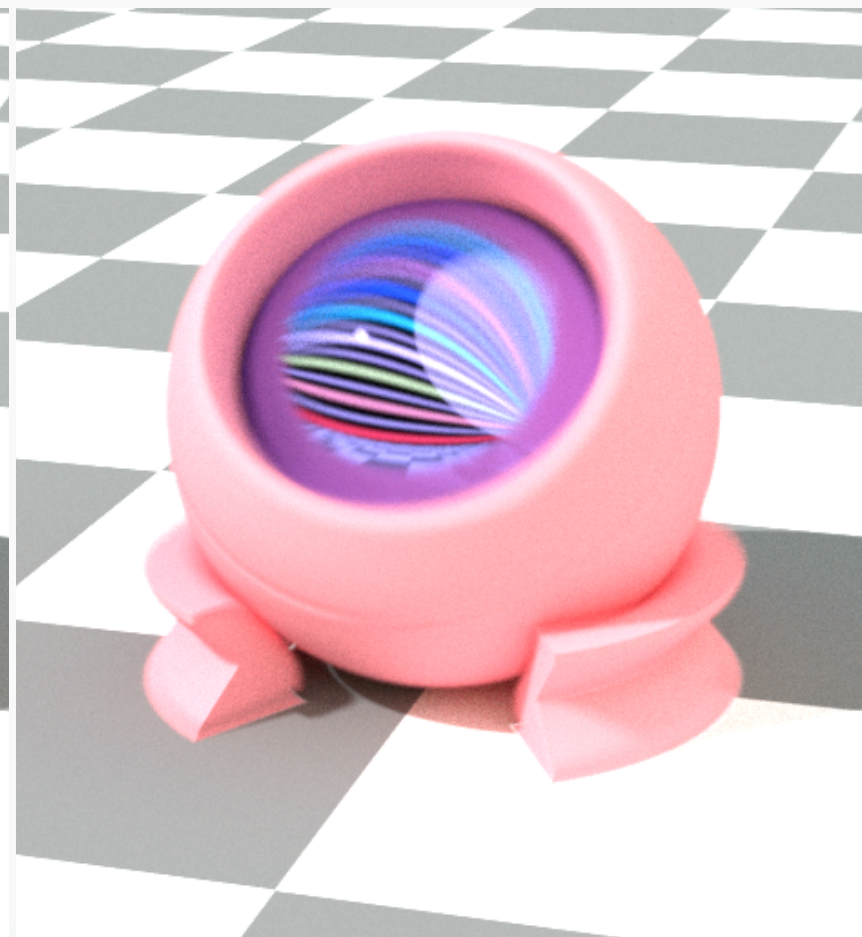
PROCESS MEMORY MODELS



Global



Position



Position+Normal

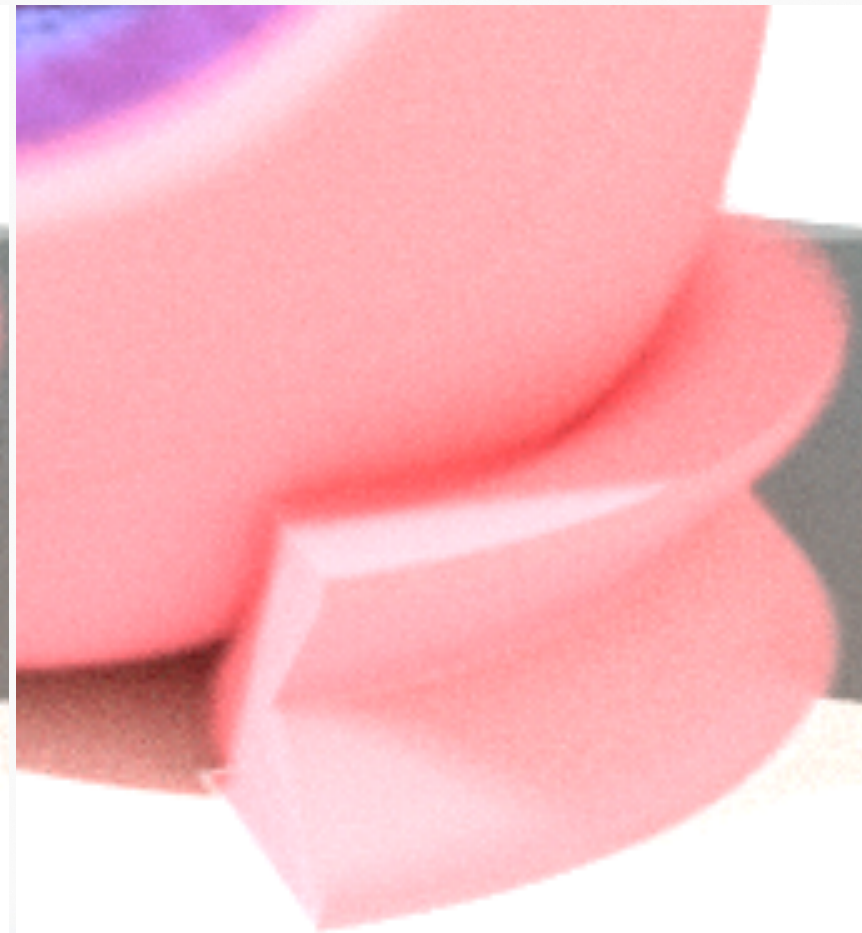
PROCESS MEMORY MODELS



Global



Position



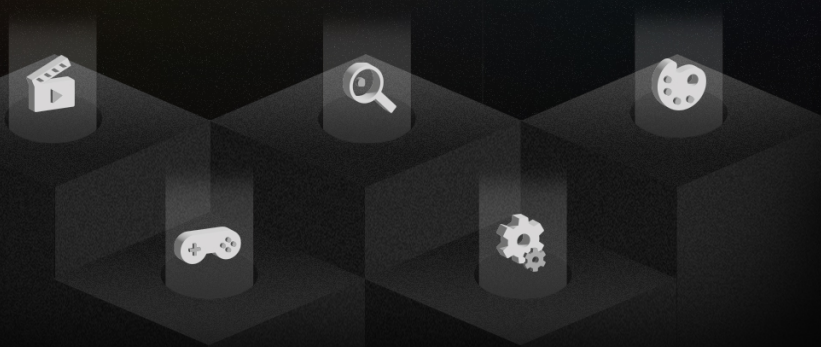
Position+Normal

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2024

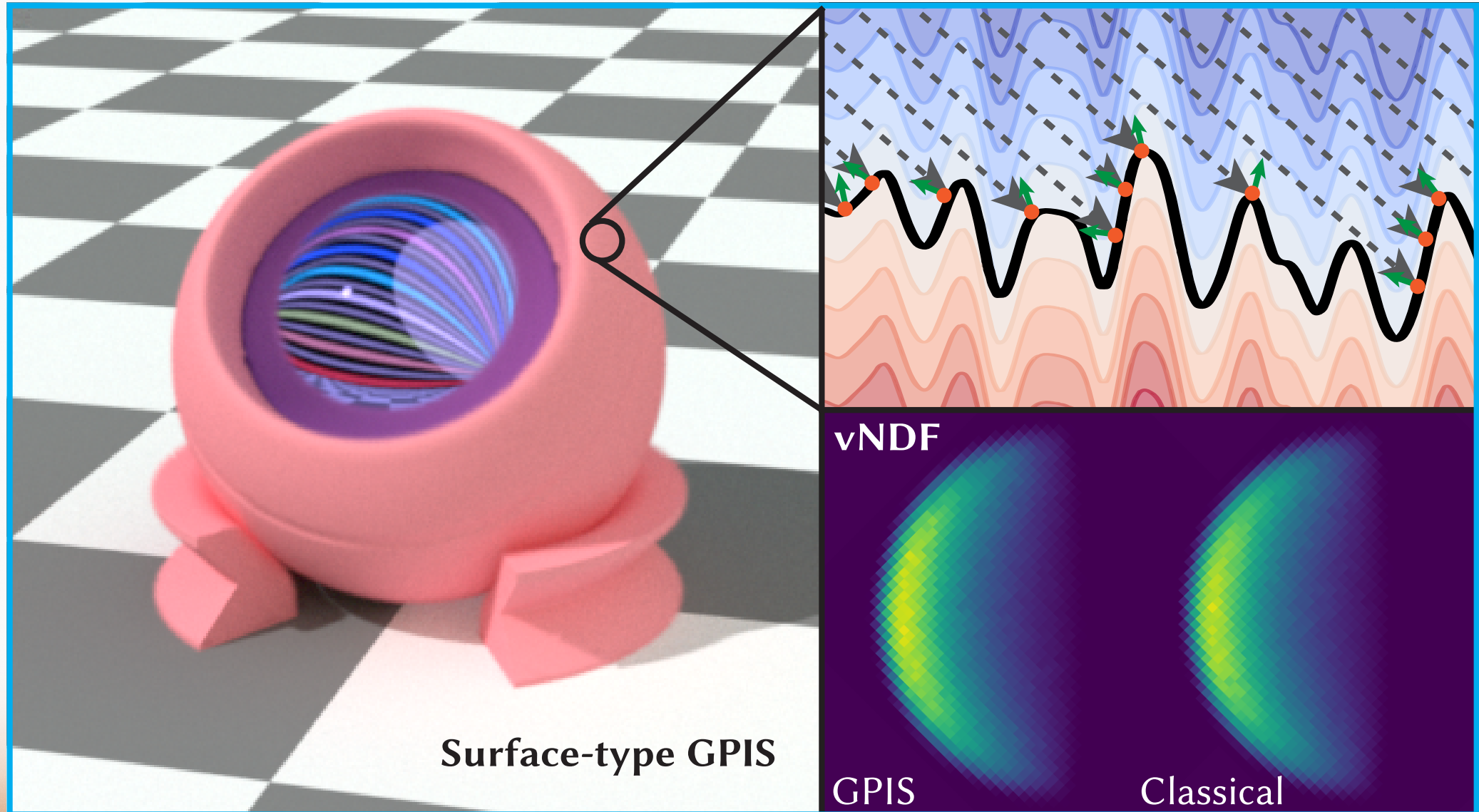


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APPEARANCE SPACE OF STOCHASTIC IMPLICIT



SURFACE-TYPE GPISSES INCLUDE MICROFACET SURFACES



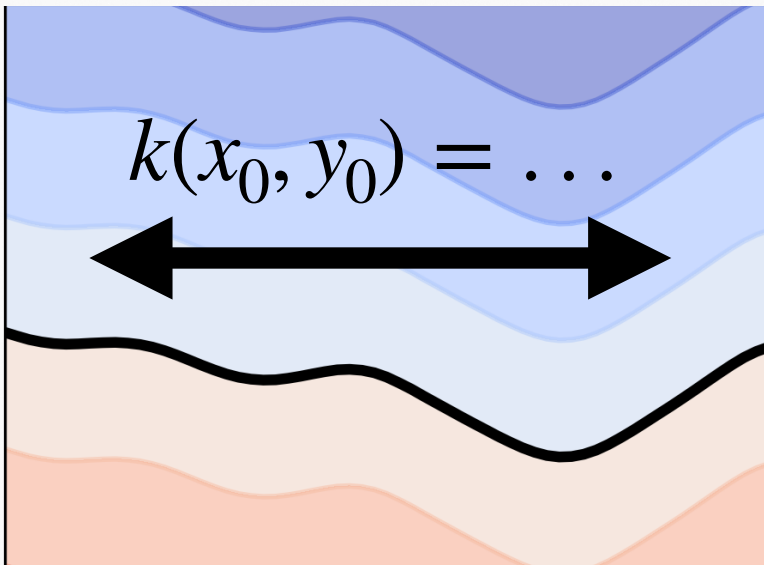
Surface-type GPIS

vNDF

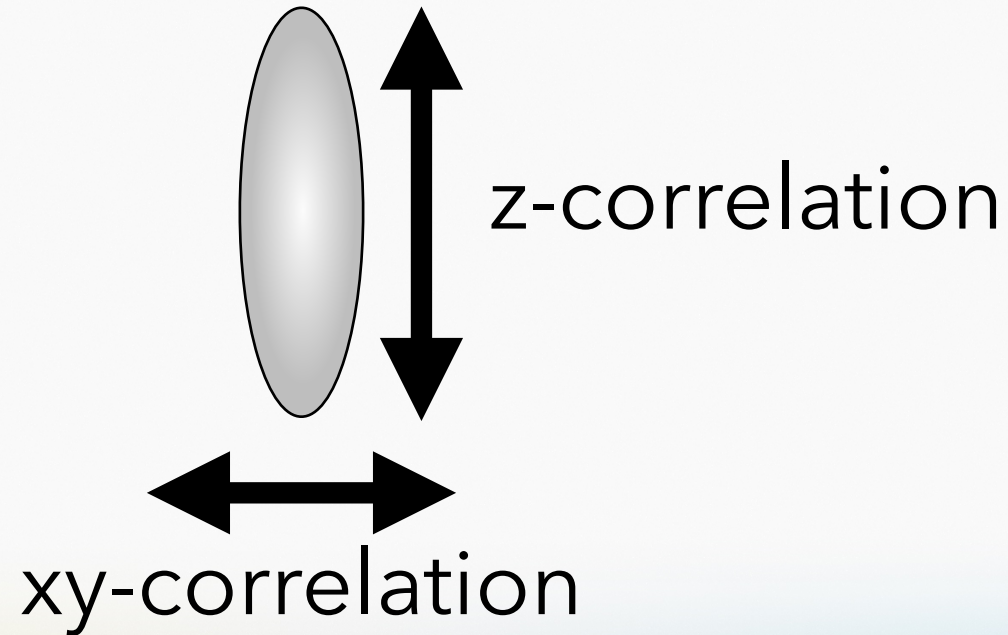
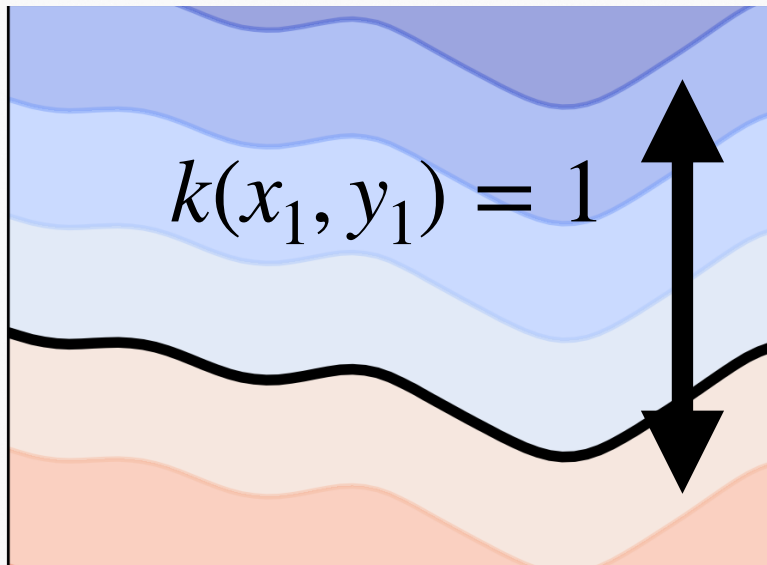
GPIS

Classical

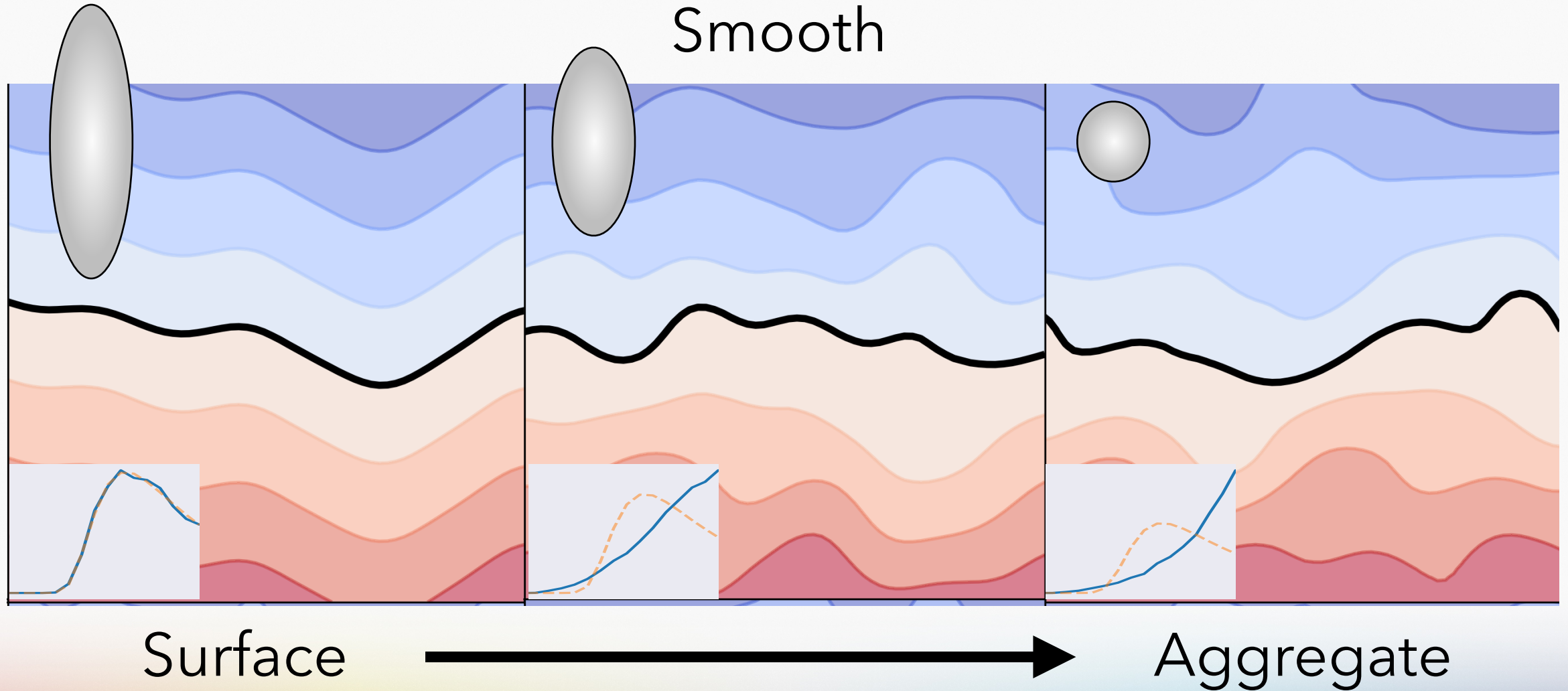
2D heightfields are the special case!



2D heightfields are the special case!

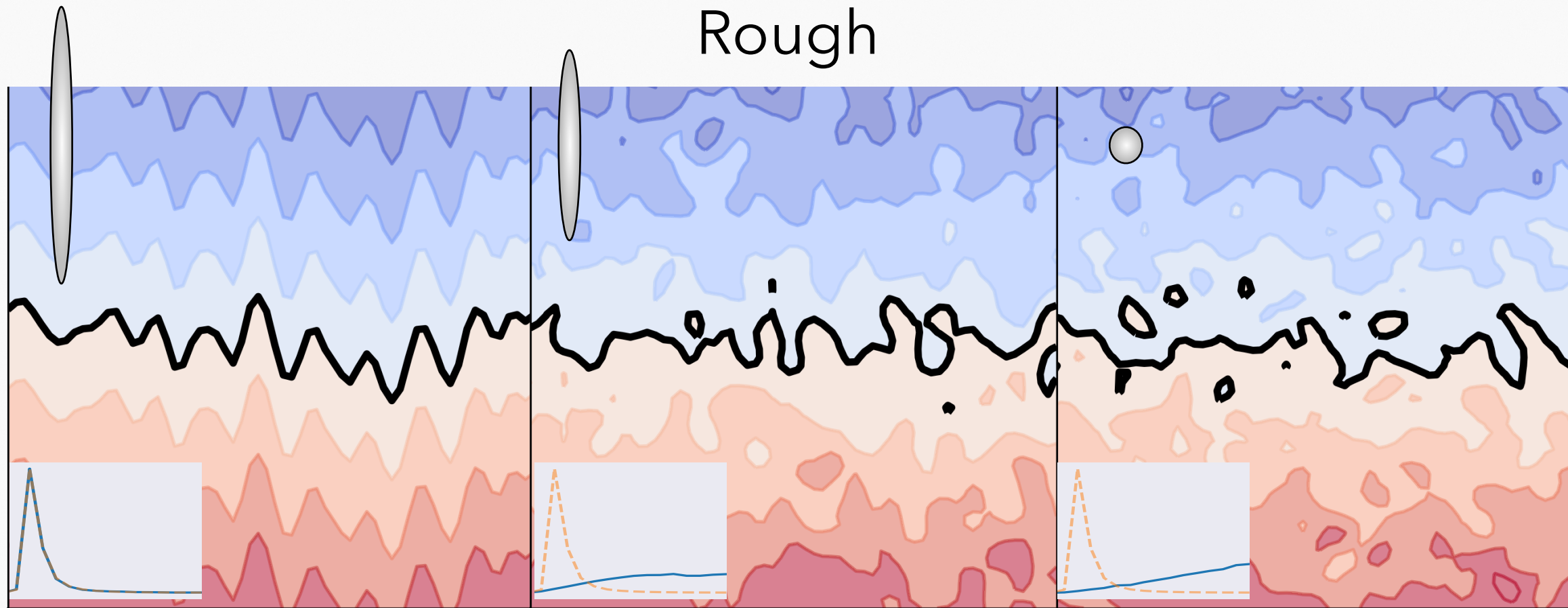


CONNECTIONS TO MICROFACET THEORY



CONNECTIONS TO MICROFACET THEORY

Rough

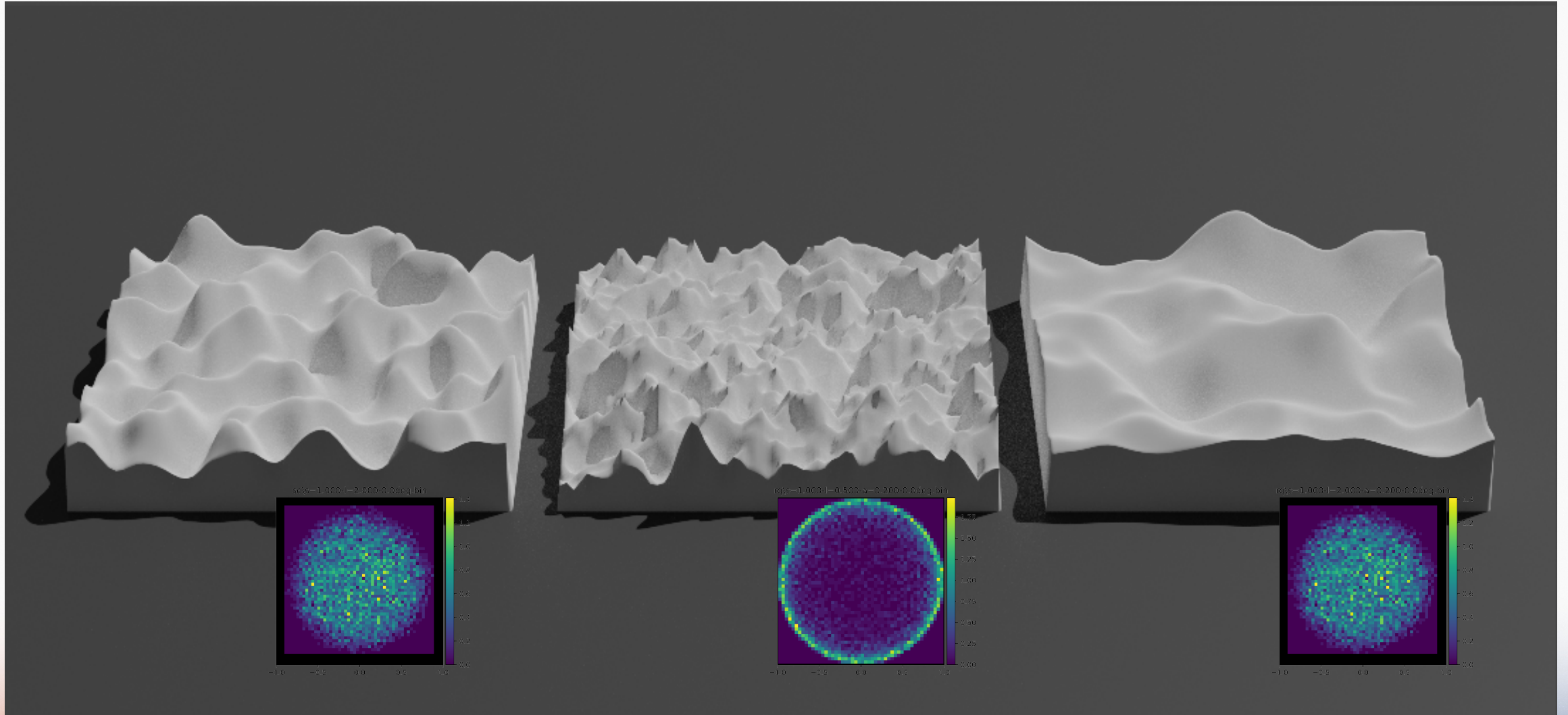


Surface

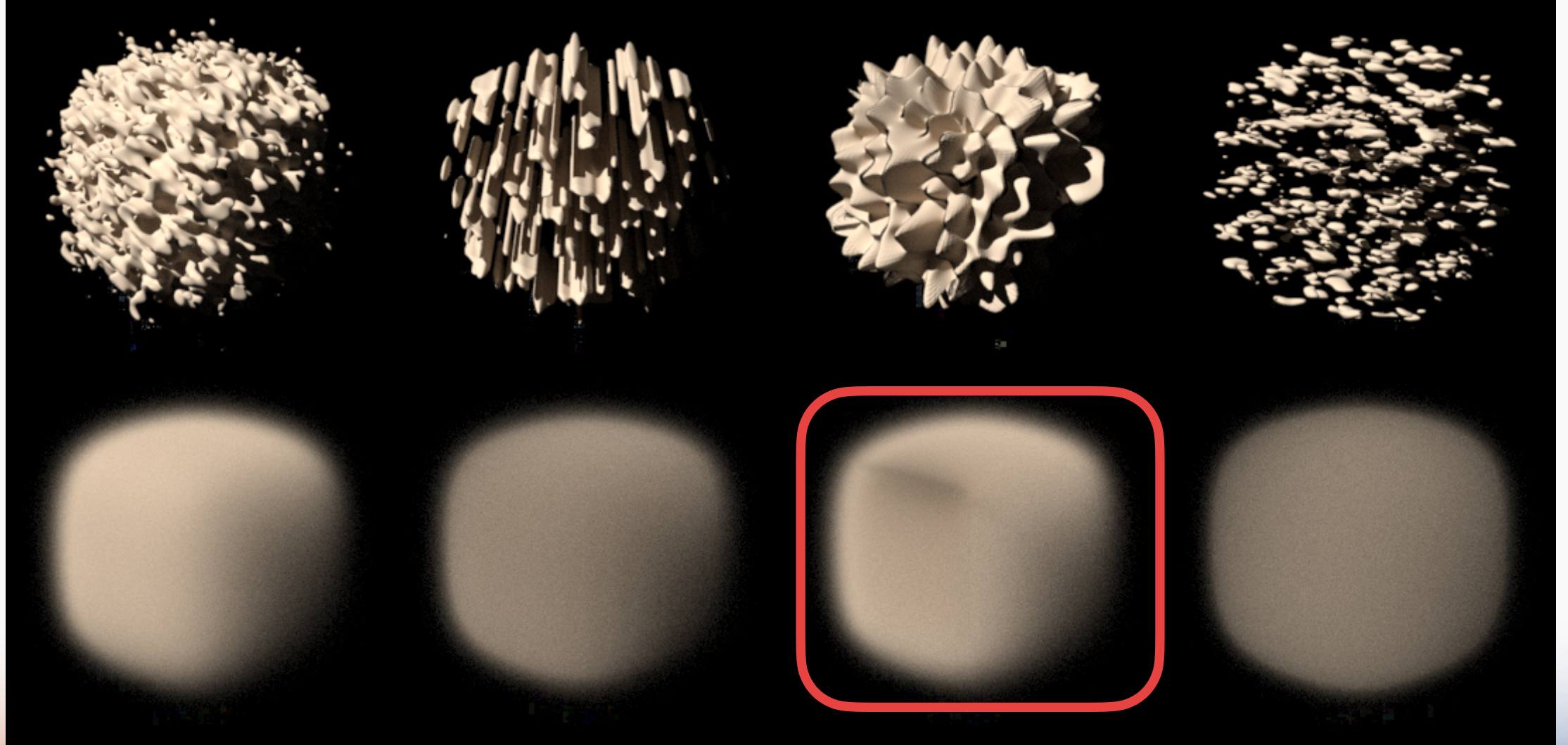


Aggregate

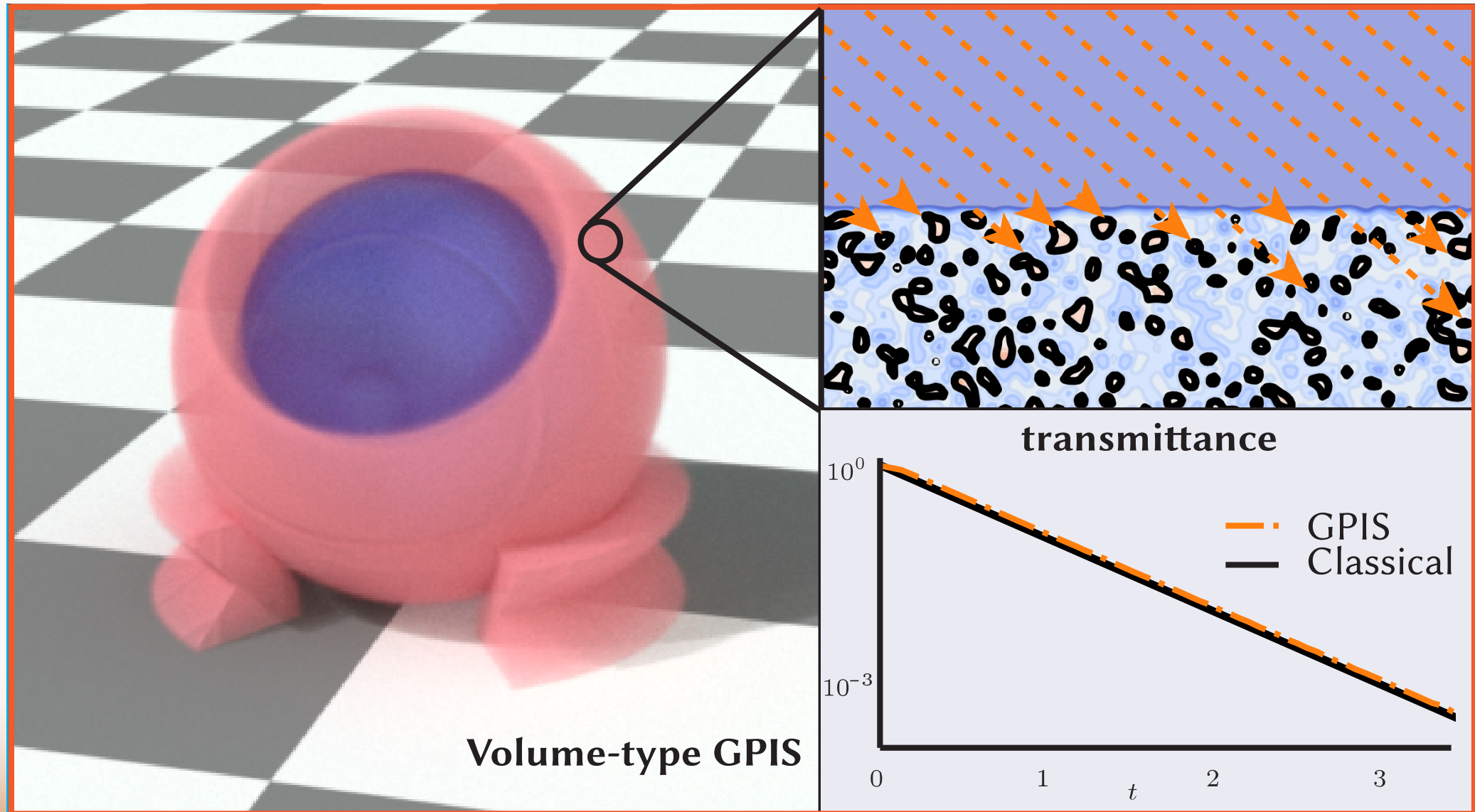
GENERATE SURFACES WITH GIVEN NDFS



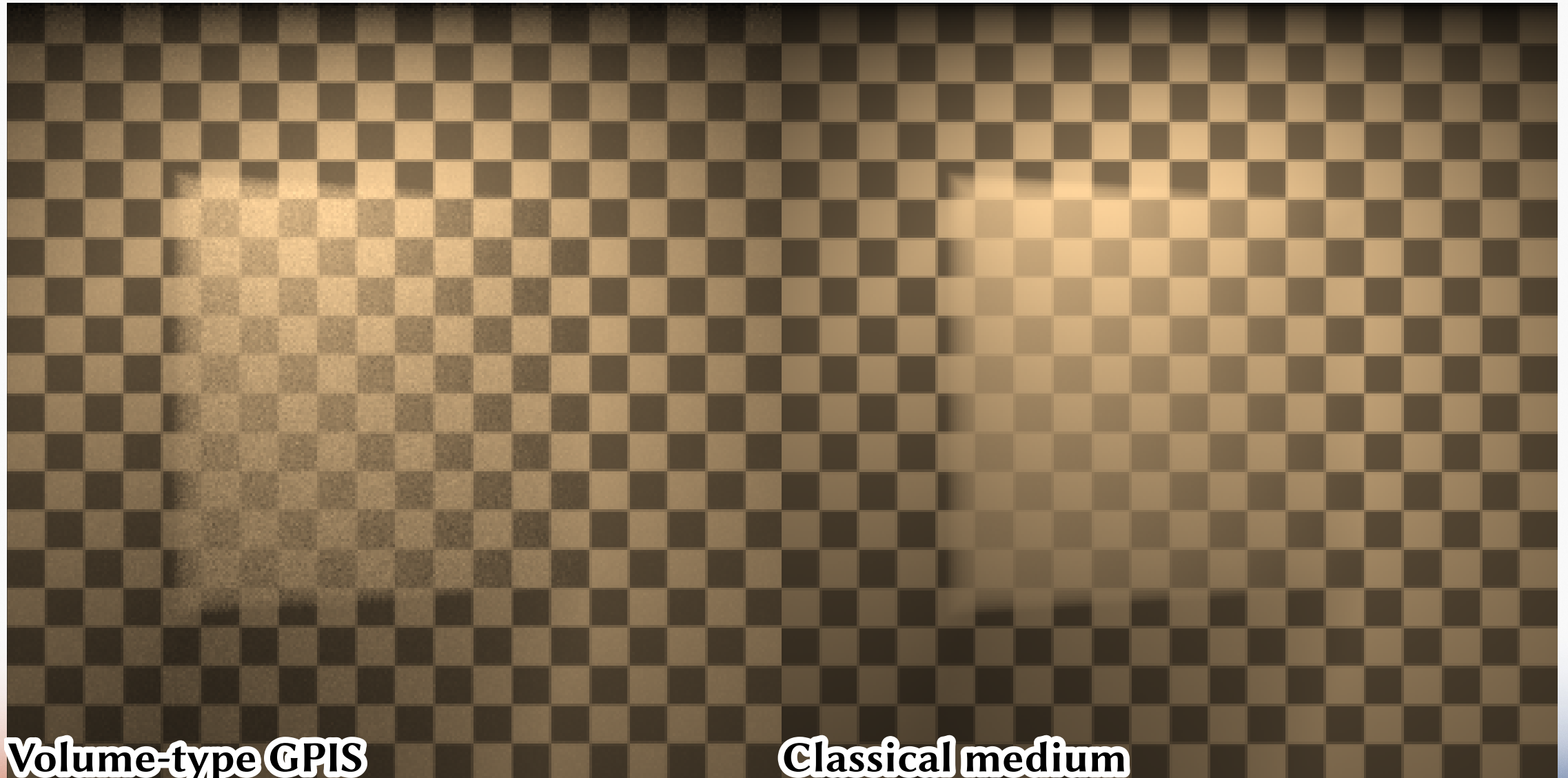
OR LOOK AT MORE GENERAL GEOMETRY!



VOLUME-TYPE GPIS APPROXIMATE CLASSICAL MEDIA



CONNECTIONS TO PARTICIPATING MEDIA



Volume-type GPIS

Classical medium

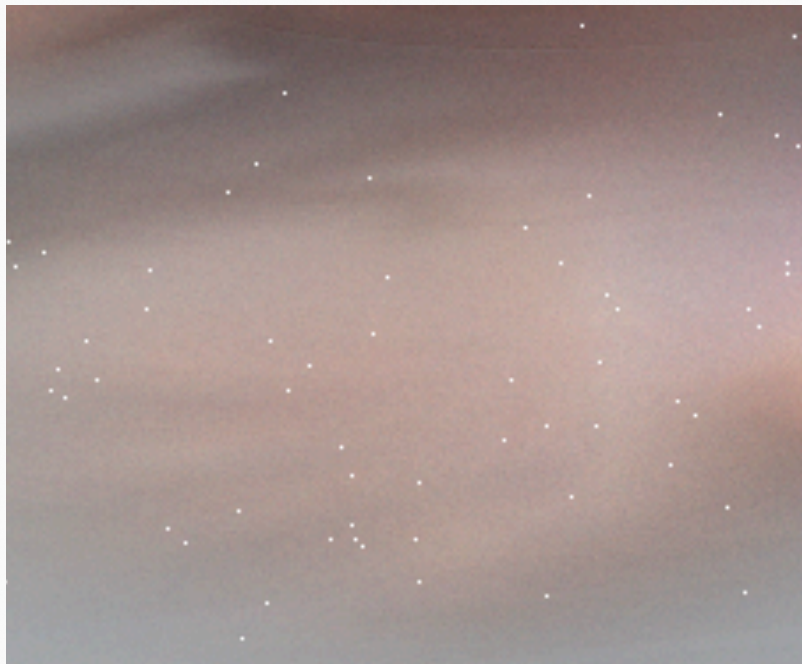
A NON-STATIONARY GPIS MODEL



A NON-STATIONARY GPIS MODEL



Surface

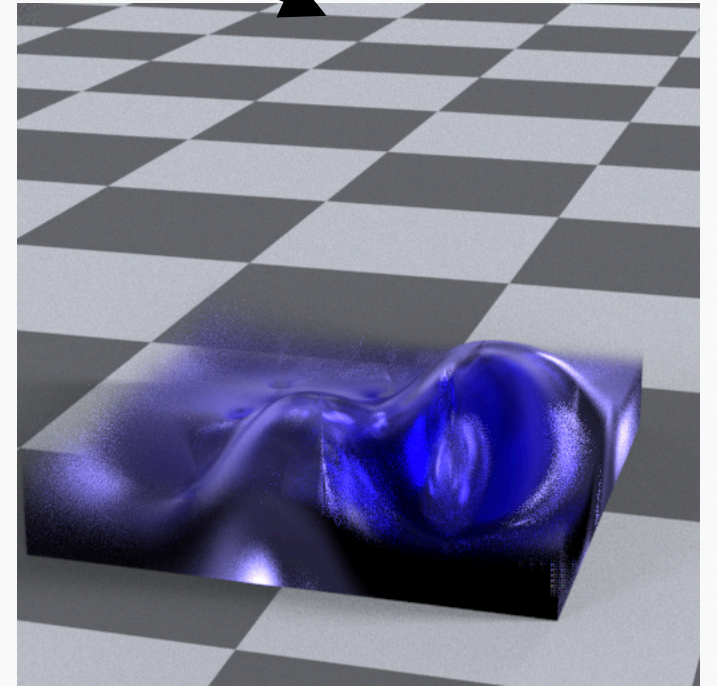
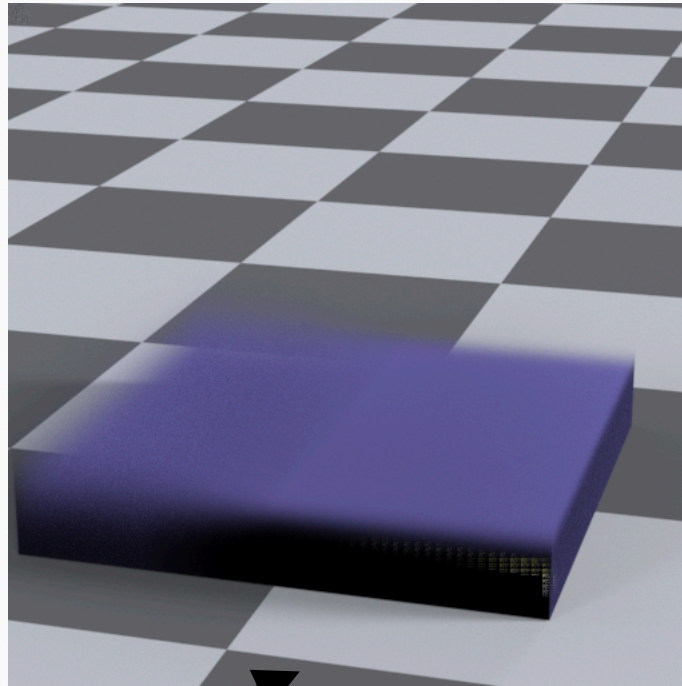
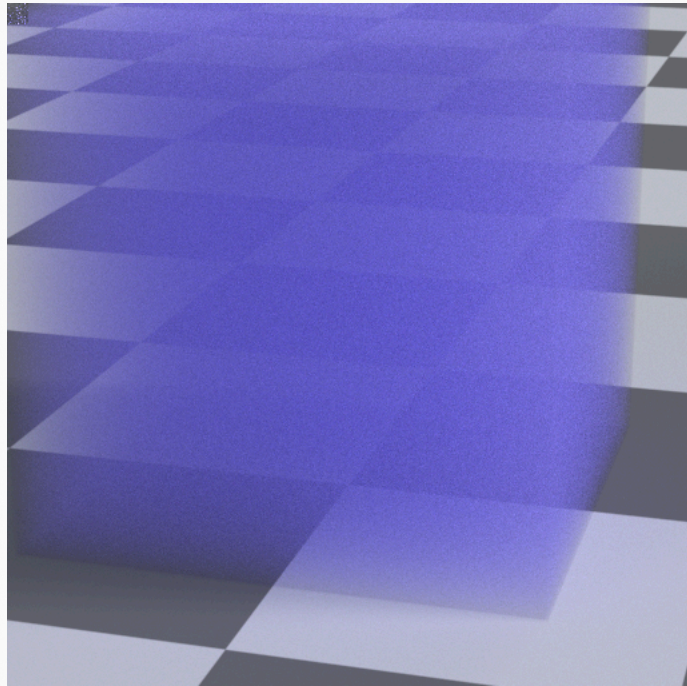


Volume



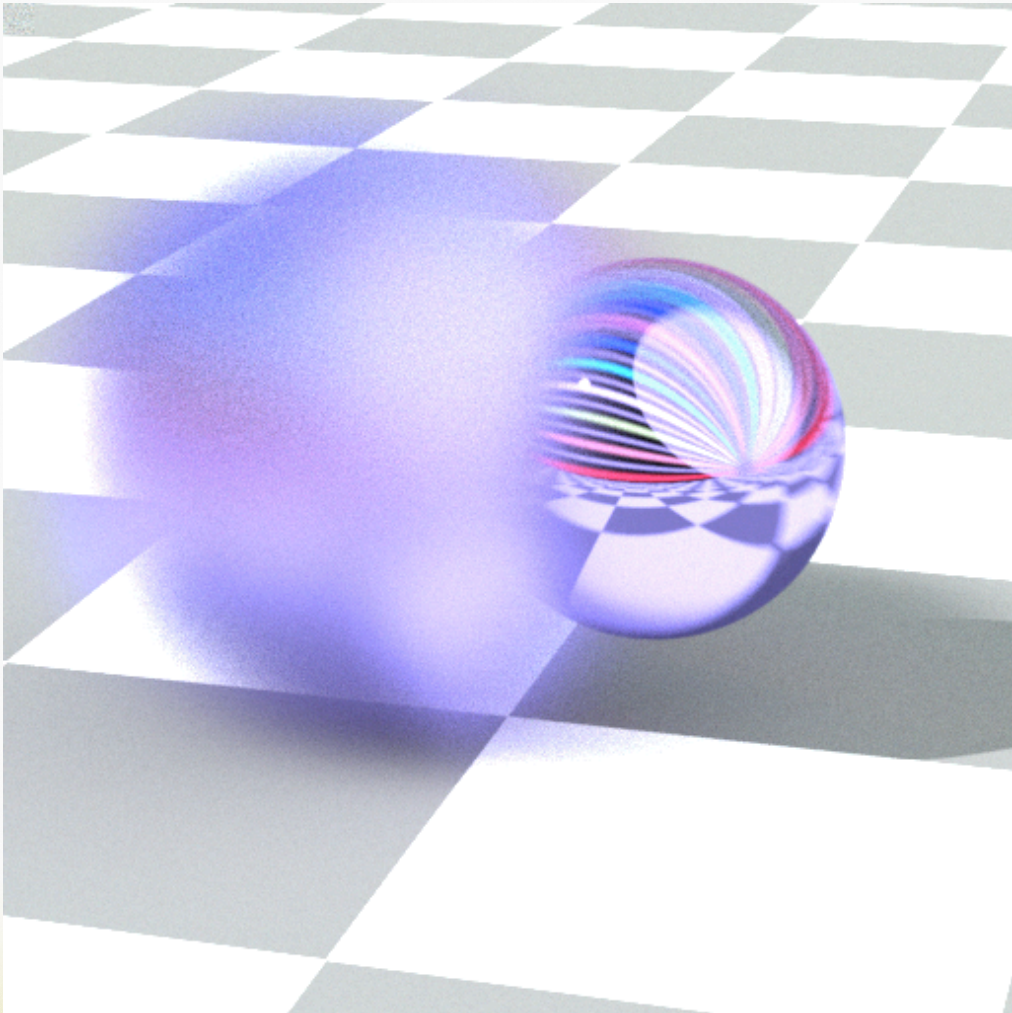
"Motion Blur"

“posterior editing”

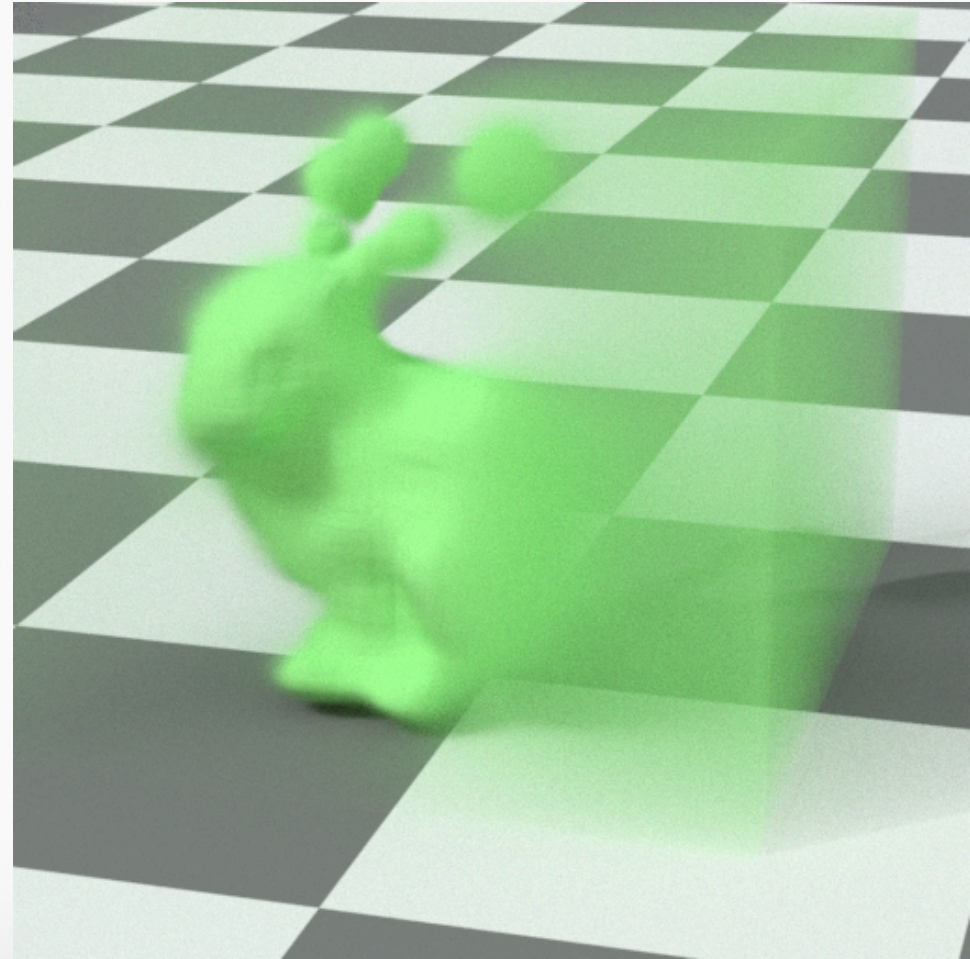
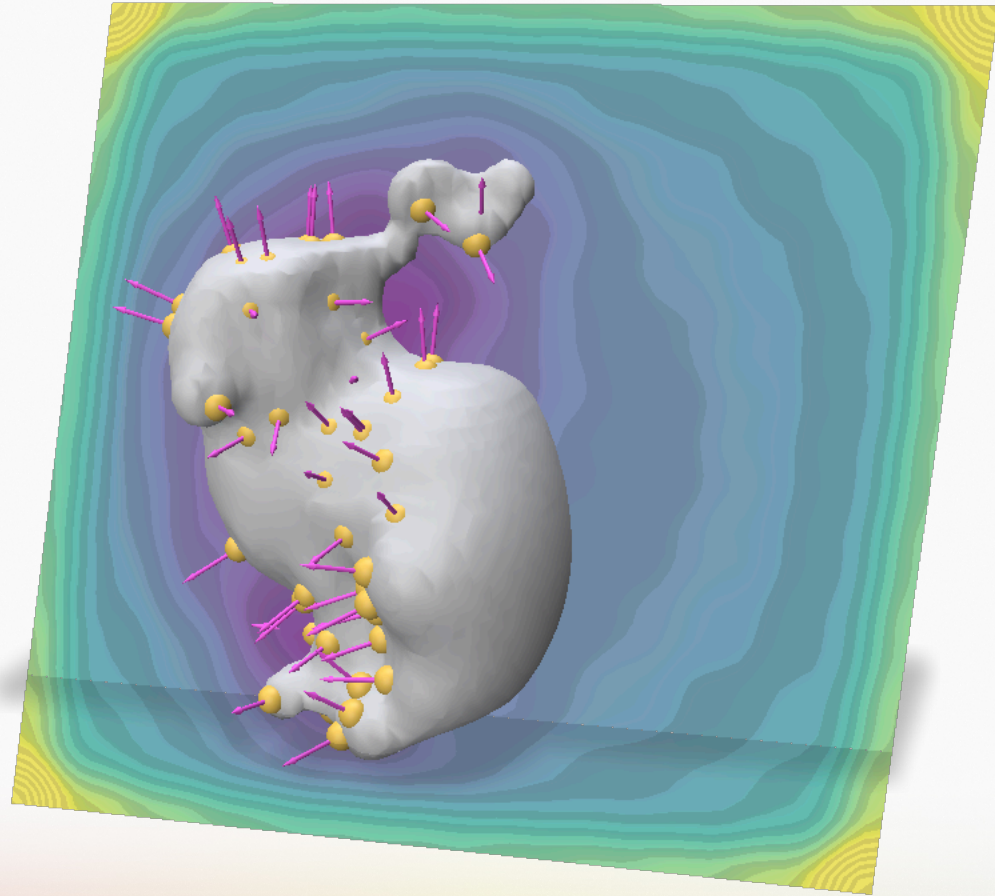


“prior editing”

STOCHASTIC CONSTRUCTIVE SOLID GEOMETRY



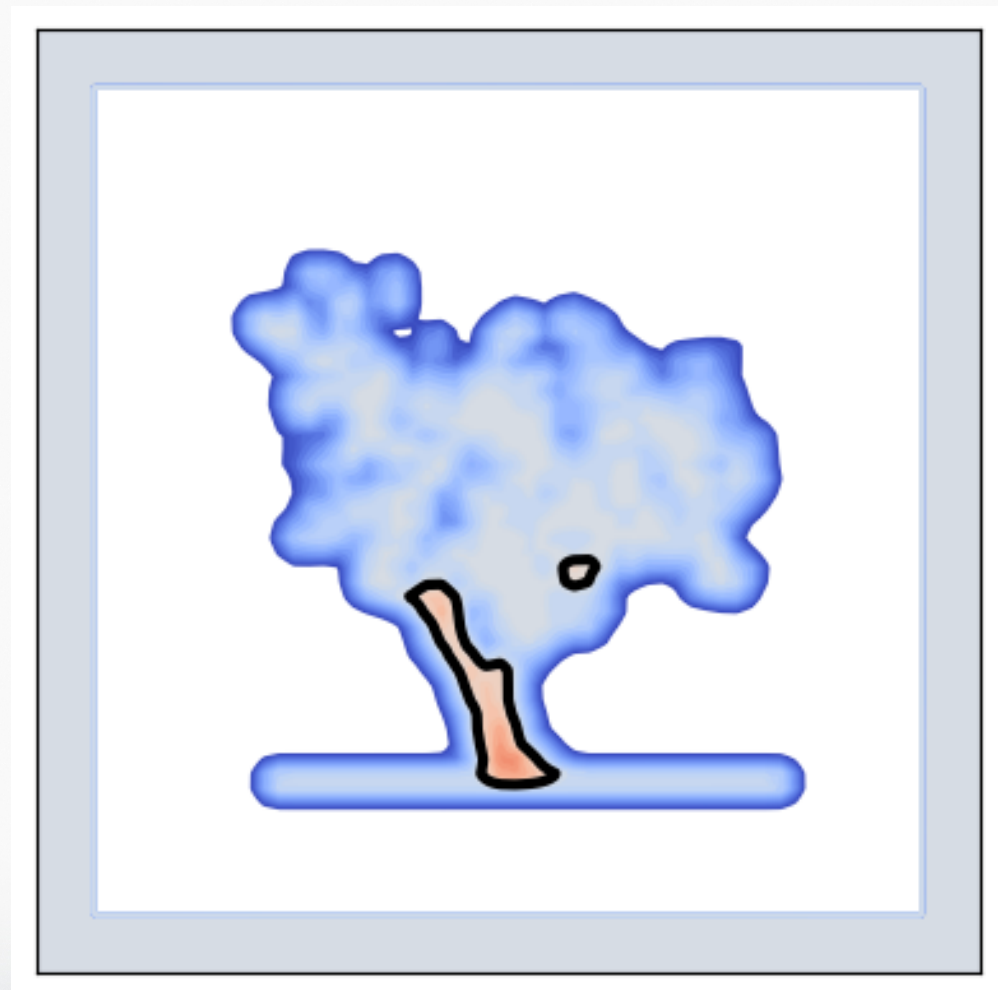
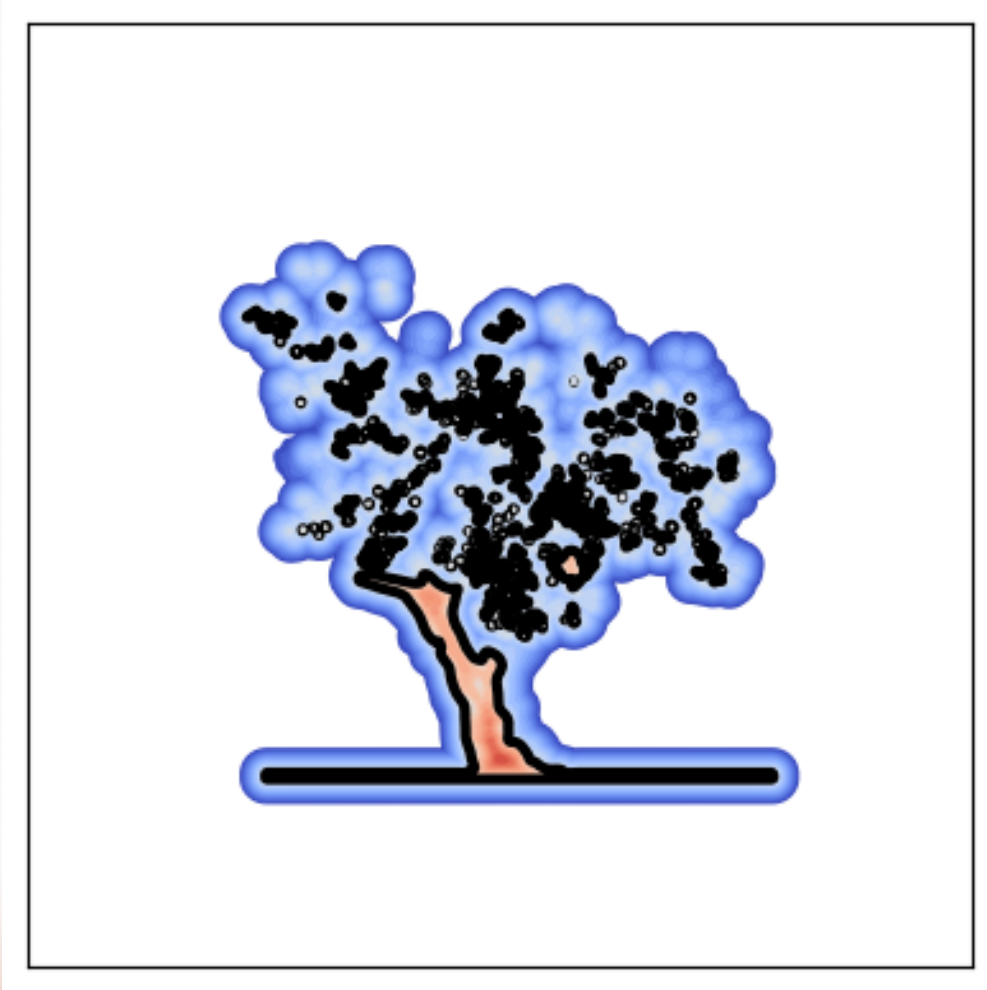
STOCHASTIC POISSON SURFACE RECONSTRUCTION



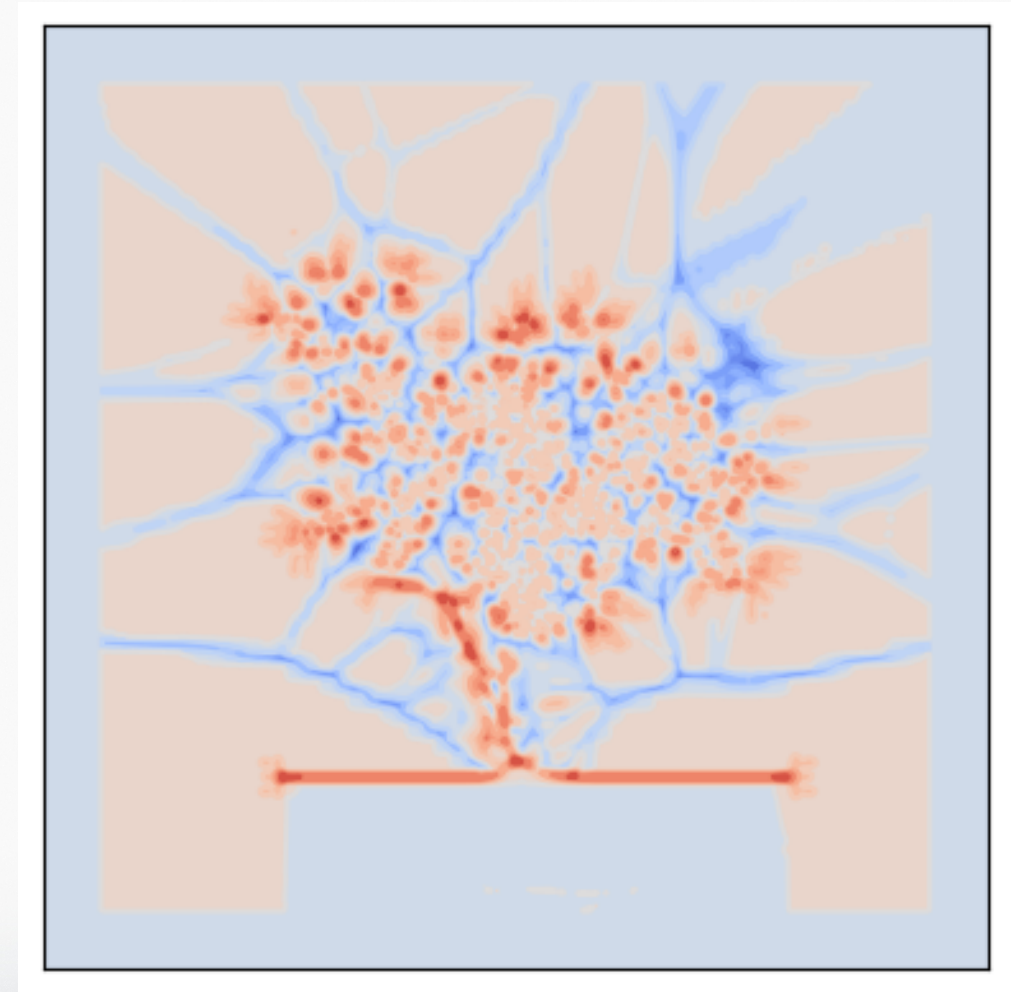
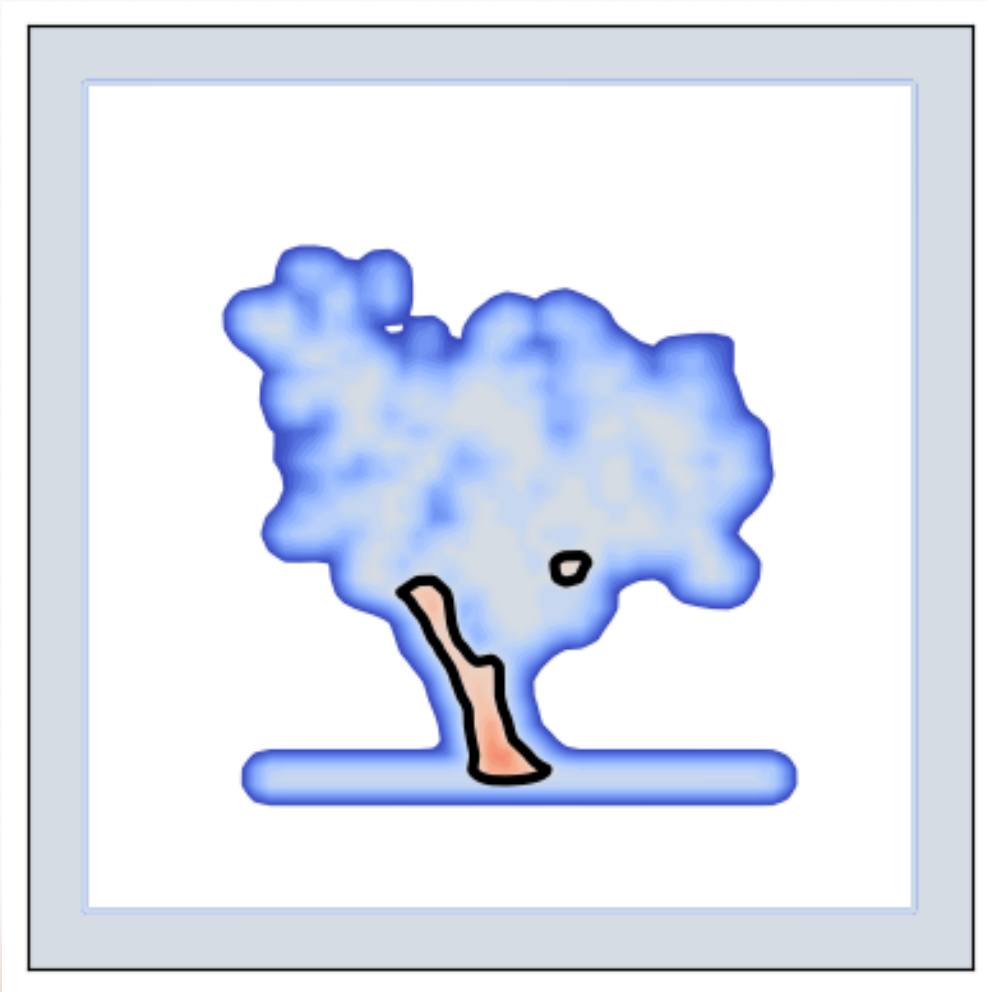
FILTERING IMPLICIT SURFACES



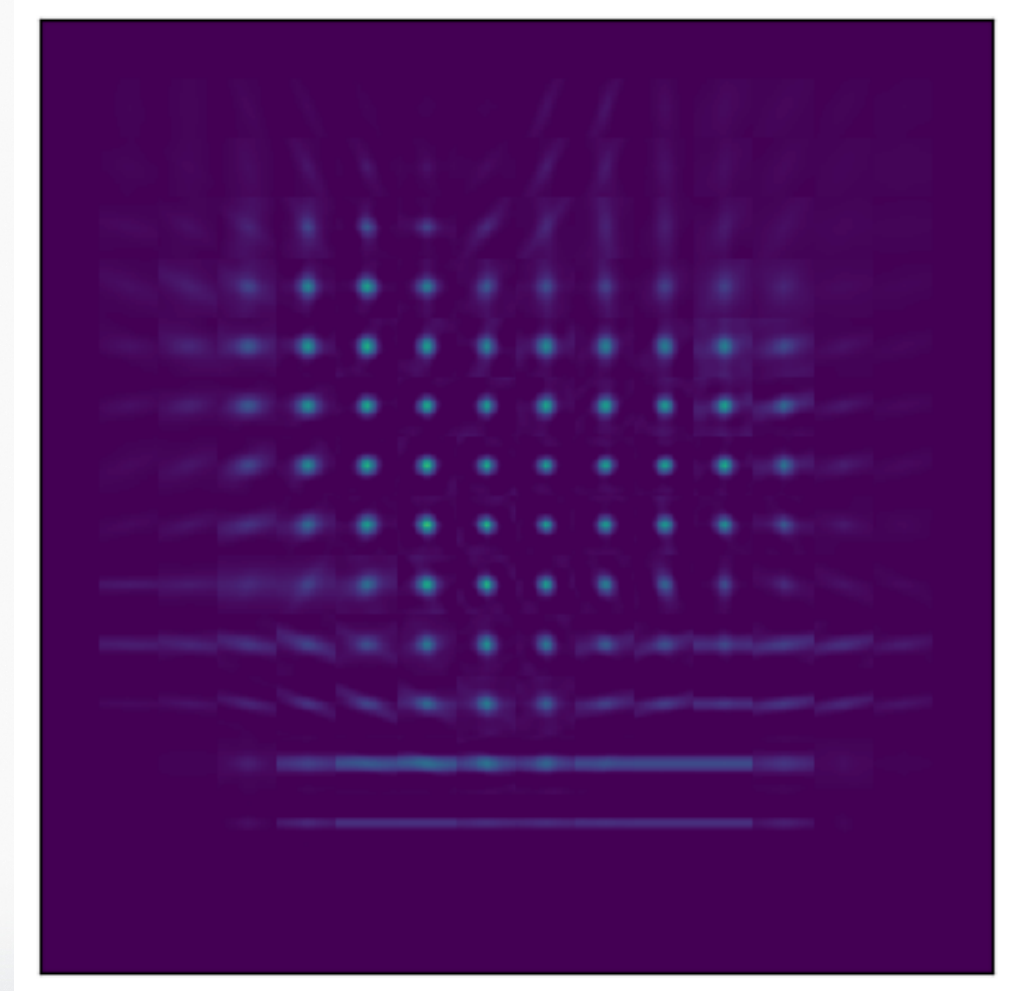
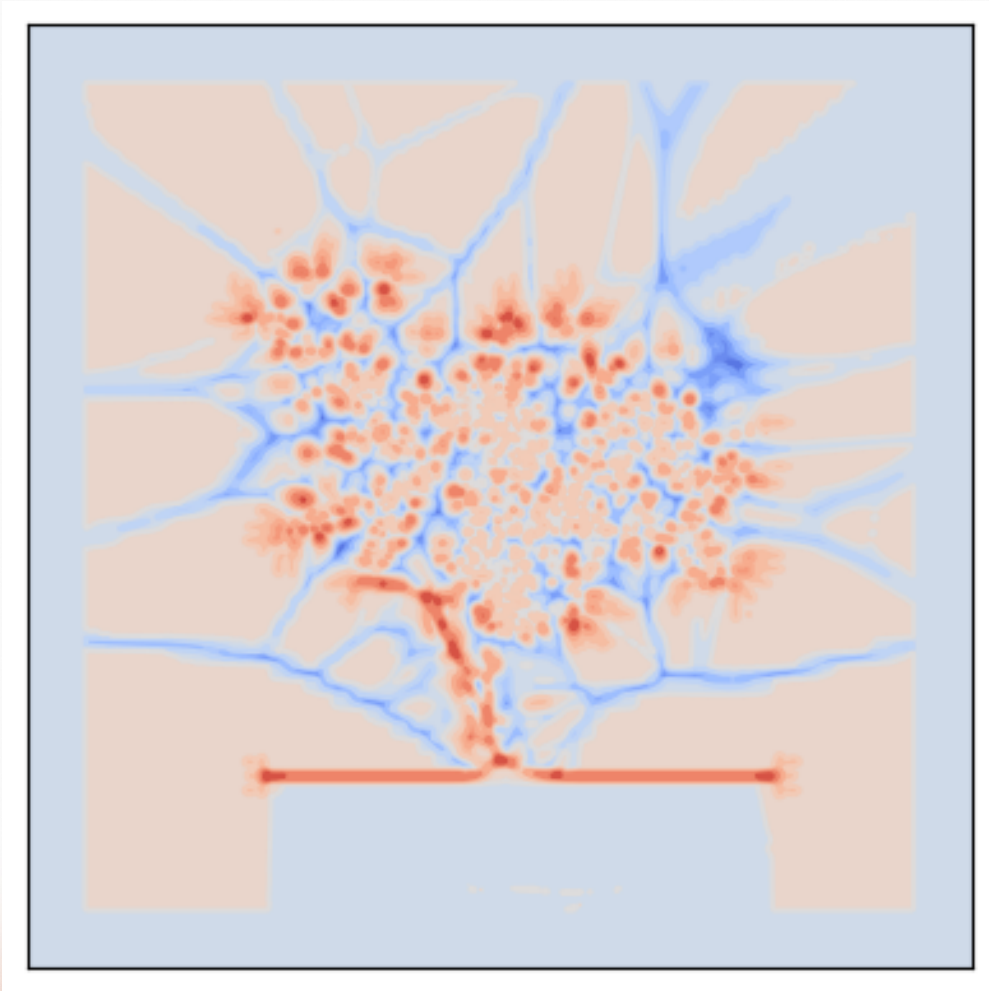
FILTERING IMPLICIT SURFACES



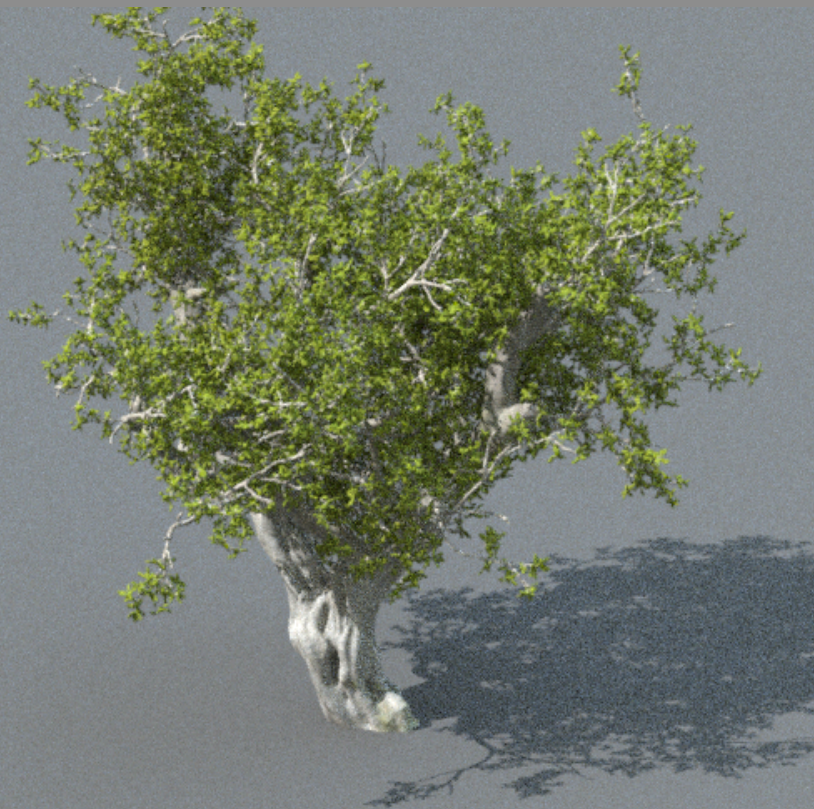
FILTERING IMPLICIT SURFACES



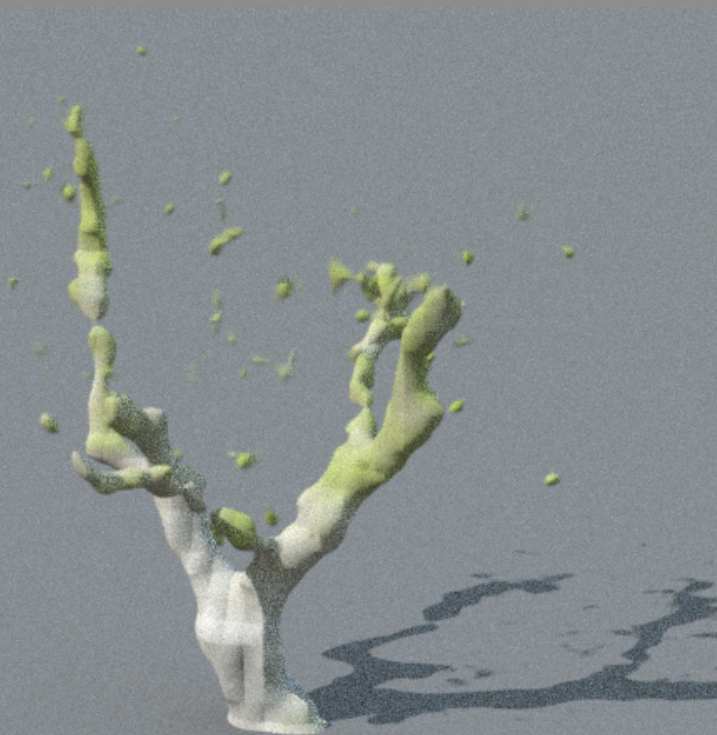
FILTERING IMPLICIT SURFACES



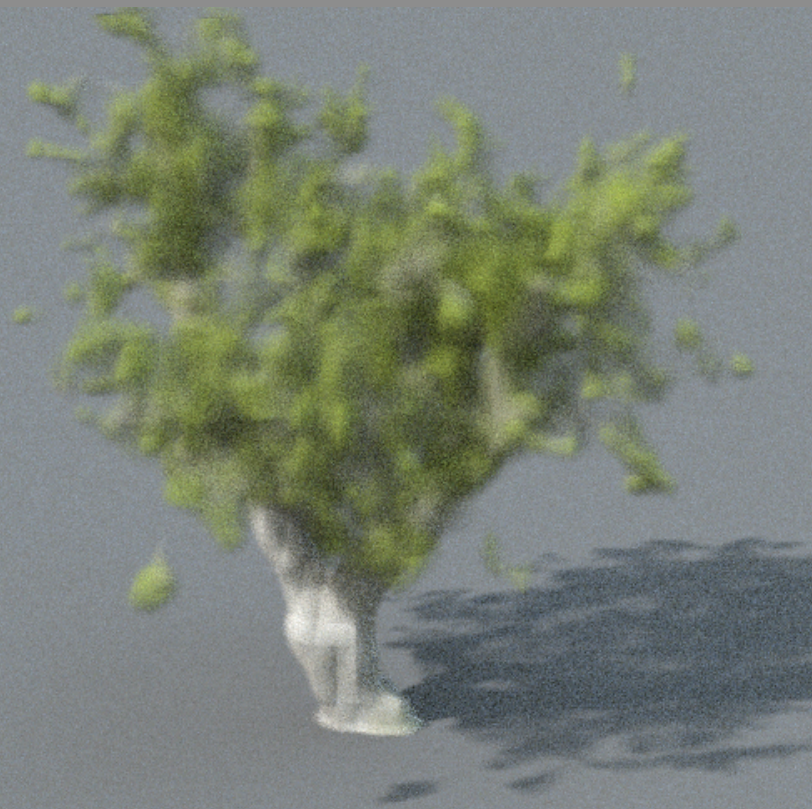
Original



Downsampled

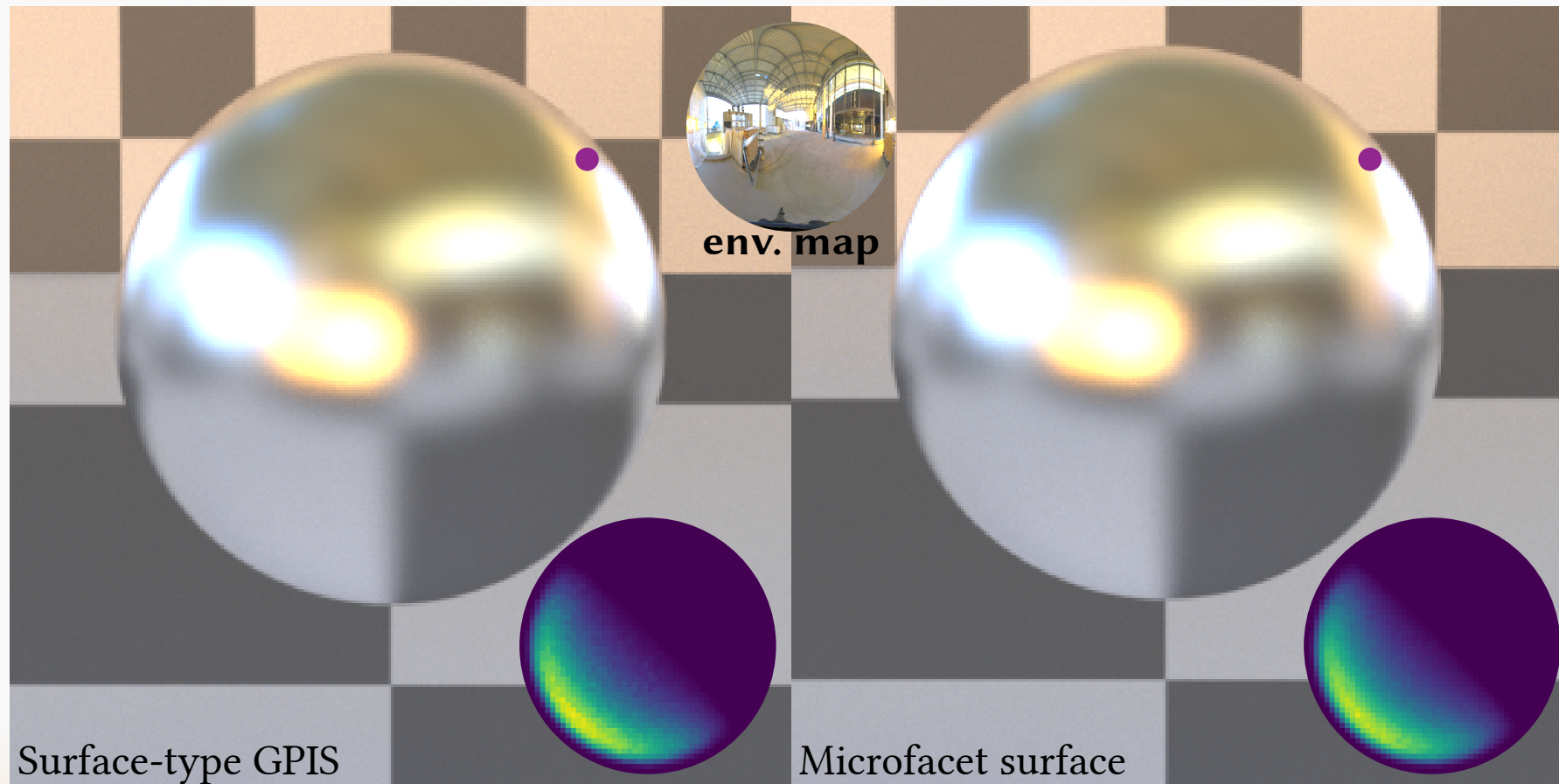


Ours



Ours

Classical



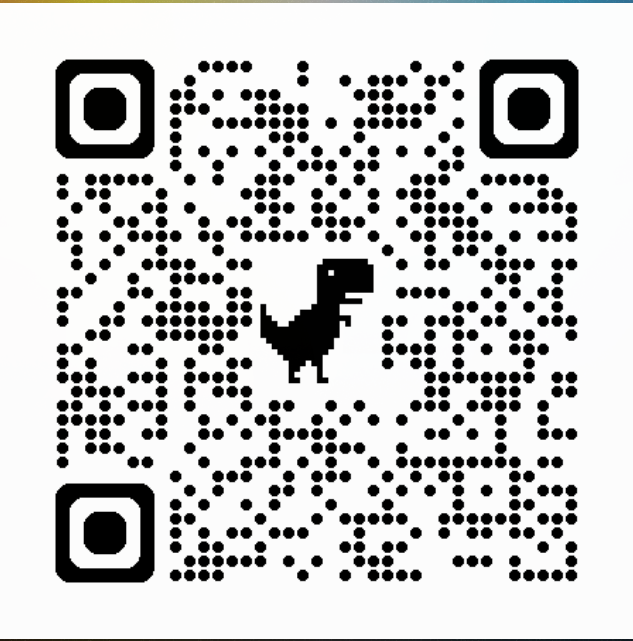
Surface-type GPIS

Microfacet surface

~100x slower...

- Find closed-form approximations for transmittance.
- Differentiable rendering algorithm
- Wider range of stochastic processes
- Apply to Monte Carlo PDE solvers

Project Page/Code



THANK YOU!



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Eugene d'Eon



Benedikt Bitterli



Wojciech Jarosz

