CS 10: Problem solving via Object Oriented Programming

Prioritizing

Main goals

- Implement priority queue
- Implement priority queue more efficiently with heap

Agenda

1. Priority Queue ADT

2. Implementation choices

3. Java's built-in PriorityQueue

We can model airplanes landing as a queue

Airplanes queued to land



Each airplane assigned a priority to land in order of arrival

First in the traffic pattern is the first to land (FIFO)

Sometimes higher priority issues arise and we need a different order

Airplanes queued to land



Suddenly one aircraft has an in-flight emergency and needs to land now!

Need a way to go to front of queue

Enter the priority queue

Priority Queues store/retrieve objects based on priority, not identity or arrival



Maps are a Key/Value store

- put(Key, Value) stores a Value associated with a Key (e.g., Key: Student ID and Value: Student Record)
- get(Key) return Value associated with Key
- Keys unique; identify object
- No ordering among Keys



- Item order depends on when item arrived
- Only one item accessible at any time (top or front)

Priority Queue order

5

Priority Queue

12

- Items stored/ retrieved by <u>priority</u>
- Priority does not represent identity as with a Map Key
- Not dependent on arrival order like Stack/Queue 6



Priority Queues have the ability to extract the highest priority item

Min Priority Queue Overview

- Lowest priority number removed first ("number 1 for landing")
- Can be used for sorting (put everything in, then repeatedly extract lowest priority number, one at a time, until queue empty)

• Operations

Max Priority Queue works similarly, but extracts the largest priority item with extractMax()

- insert(element) insert element into Priority Queue
 - Like BST, elements need a way to compare with each other to see which is the smallest, so element should implement compareTo()
 - We will say whatever *compareTo()* uses to compare elements is the <u>Key</u>
 - Many elements can have the same Key in a Priority Queue
- *extractMin()* remove and return element with smallest Key
- *minimum()* return element with smallest Key, but leaves the element in Priority Queue (like *peek()* or *front()* in Stack or Queue)
- *isEmpty()* true if no items stored, false otherwise
- decreaseKey() reduces an element's priority number (take CS 31 for more details on this)

Priority Queues are extensively used in simulations and scheduling

Job scheduling example



extractMin() again and get time 9

8

MinPriorityQueue.java specifies interface

MinPriorityQueue.java

```
6 public interface MinPriorityQueue<E extends Comparable<E>>> {
       /**
 7⊝
 8
        * Is the priority queue empty?
        * @return true if the priority queue is empty, false if not empty.
 9
        */
10
       public boolean isEmpty();
11
12
       /**
13⊝
14
        * Insert an element into the queue.
15
        * @param element thing to insert
16
        */
17
       public void insert(E element);
18
       /**
19⊝
20
        * Return the element with the minimum key, without removing it from the queue.
        * @return the element with the minimum key in the priority queue
21
22
        */
23
       public E minimum();
24
25⊝
       /**
26
        * Return the element with the minimum key, and remove it from the queue.
27
        * @return the element with the minimum key in the priority queue
28
        */
29
       public E extractMin();
30 }
```



- 1. Priority Queue ADT
- 2. Implementation choices
 - 3. Java's built-in PriorityQueue

Unsorted List

| 15 6 | 9 | 27 |
|------|---|----|
|------|---|----|

Operation Run time

isEmpty

insert

minimum

extractMin

Unsorted List

| 15 6 | 9 | 27 |
|------|---|----|
|------|---|----|

| Operation | Run time | Notes |
|------------|-------------|---|
| isEmpty | O(1) | Check size == 0 |
| insert | O(1) | Add on to end (amortized growth) |
| minimum | Θ(n) | Must loop through all elements to find smallest |
| extractMin | Θ(n) | Loop through all elements and move last item to fill hole |

Unsorted List

Sorted List

| 15 6 | 9 | 27 |
|------|---|----|
|------|---|----|

| 27 15 9 6 | |
|-----------|--|
|-----------|--|

| Operation | Unsorted | Sorted | Notes |
|------------|----------|--------|-------|
| isEmpty | O(1) | | |
| insert | O(1) | | |
| minimum | Θ(n) | | |
| extractMin | Θ(n) | | |

Unsorted List

| Sorted L | .ist |
|----------|------|
|----------|------|

| 15 6 | 9 | 27 |
|------|---|----|
|------|---|----|

| 27 15 9 6 | 27 15 9 6 | 15 | 7 | 2 | |
|-----------|-----------|----|---|---|--|
|-----------|-----------|----|---|---|--|

| Operation | Unsorted | Sorted | Notes |
|------------|----------|----------------|-----------------------|
| isEmpty | O(1) | O(1) | Check size == 0 |
| insert | O(1) | O(2n+1) = O(n) | Insert in order, move |
| minimum | Θ(n) | O(1) | Return last element |
| extractMin | Θ(n) | O(1) | Remove last element |

Unsorted List

| 15 6 | 9 | 27 |
|------|---|----|
|------|---|----|

| 27 15 9 6 |
|-----------|
|-----------|

| Operation | Unsorted | Sorted | Notes |
|------------|----------|--------|-----------------------|
| isEmpty | O(1) | O(1) | Check size == 0 |
| insert | O(1) | O(n) | Insert in order, move |
| minimum | Θ(n) | O(1) | Return last element |
| extractMin | Θ(n) | O(1) | Remove last element |

Either way we pay a price, on min/extractMin or on insert Heaps are a better choice



- 1. Priority Queue ADT
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Heaps are based on Binary Trees

Tree data structure



Subtree

In a Binary Tree, each node has 0, 1, or 2 children Height is the number of edges on the longest path from root to leaf Each node has a Key and a Value No guarantee of balance in Tree, could have Vine

Heaps have two additional properties beyond Binary Trees: Shape and Order

Shape property keeps tree compact



Shape property

- Nodes added starting from root and building downward
- New level started only once a prior level is filled
- Nodes added left to right
- Called a "complete" tree
- Prevents "vines"
- Makes height as small as possible: h = [log₂ n]

Heaps have two additional properties beyond Binary Trees: Shape and Order

Order property keeps nodes organized

Root is largest in max heap (smallest in min heap)



Subtree root is largest in subtree

Order property

Reverse inequality for min heap

- ∀nodes i ≠ root, value(parent(i)) ≥ value(i)
- Root is the largest value in a max heap (or min value in a min heap)
 - Largest value at any subtree is at the root of the subtree
 - Unlike BST, no relationship between two sibling nodes, other than they are less than parent

The shape property makes an array a natural implementation choice

Array implementation

Heap is conceptually a tree, data actually stored in an array



Nodes stored in array

- Node *i* stored at index *i*
- Parent at index (i-1)/2
- Left child at index i*2 +1
- Right child at index *i*2+2*



Node 3 containing 8

- *i=3* Drop any decimal component
- Parent = (3-1)/2=1
- Left child = 3*2+1 = 7
- Right child = 3*2+2=8



- 1. Priority Queue ADT
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Inserting into max heap must keep both shape and order properties intact

Max heap insert



Insert 15

 Shape property: fill in next spot in left to right order (index i=10)

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|----|----|----|---|---|---|---|---|---|---|
| 16 | 14 | 10 | 8 | 7 | 9 | 3 | 2 | 4 | 1 |

Inserting into max heap must keep both shape and order properties intact

Max heap insert



Insert 15

 Shape property: fill in next spot in left to right order (index i=10)

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|----|----|----|---|---|---|---|---|---|---|----|
| 16 | 14 | 10 | 8 | 7 | 9 | 3 | 2 | 4 | 1 | 15 |

- Order property: parent must be larger than children
- Can't keep 15 below 7
- Swap parent and child

Inserting into max heap must keep both shape and order properties intact

Max heap insert



Insert 15

 Shape property: fill in next spot in left to right order (index i=10)



- Order property: parent must be larger than children
- Can't keep 15 below 7
- Swap parent and child
- Parent is at index (i-1)/2 = 4

We may have to swap multiple times to get both heap properties

Max heap insert



Insert 15

- Shape property: good!
- Order property: parent must
 be larger than children, not
 met



- Swap parent and child
- Child is at index *i=4*
- Parent at (i-1)/2=1

Eventually we will find a spot for the newly inserted item, even if that spot is the root

Max heap insert



Insert summary:

- Add new node at bottom left of tree
- Bubble new node up (possibly to root) until order restored
- Tree will be as compact as possible
- Largest node at root

Insert 15

- Shape property: good!
- Order property: good!
- Done

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|----|----|----|---|----|---|---|---|---|---|----|
| 16 | 15 | 10 | 8 | 14 | 9 | 3 | 2 | 4 | 1 | 7 |

General rule

- Keep swapping until order property holds again
- Here done after swapping 14 and 15

extractMax means removing the root, but that leaves a hole

extractMax



extractMax -> 16

- Max position is at root (index 0)
- Removing it leaves a hole, violating shape property



- Also, bottom right most node must be removed to maintain shape property
- Solution: move bottom right node to root (like unsorted)

Moving bottom right node to root restores shape, but not order property

extractMax



After swap

- Shape property: good!
- Order property: want max at root, but do not have that



- Left and right subtrees are still valid
- Swap root with larger child
- New root will be greater than everything in each subtree

May need multiple swaps to restore order property

extractMax



After swap 15 and 7

- Shape property: good!
- Order property: invalid
- Swap node with largest child



Stop once order property is restored

extractMax



After swap 7 and 14

- Shape property: good!
- Order property: good!

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|----|----|----|---|---|---|---|---|---|---|
| 15 | 14 | 10 | 8 | 7 | 9 | 3 | 2 | 4 | 1 |

extractMax summary:

- Remove root
- Move last node to root
- Bubble new root down by repeatedly swapping with largest child until order is restored

Can implement heap-based Min Priority Queue using an ArrayList

HeapMinPriorityQueue.java

```
public class HeapMinPriorityQueue<E extends Comparable<E>>
 9
   implements MinPriorityQueue<E> {
10
       private ArrayList<E> heap;
11
12
13⊝
       /**
14
           Constructor
        */
15
16∍
       public HeapMinPriorityQueue() {
17
           heap = new ArrayList < E > ();
18
       }
19
```

NOTE: example was for a MAX Priority Queue, this code implements a <u>MIN</u> Priority Queue

Easy to change to this code to a MAX Priority Queue

Helper functions make finding parent and children easy

HeapMinPriorityQueue.java

- V I

```
108
        // Swap two locations i and j in ArrayList a.
        private static <E> void swap(ArrayList<E> a, int i, int j) {
1099
110
            E temp = a.get(i); //temporarily hold item at index i
            a.set(i, a.get(j)); //set item at index i to item at index j
111
112
            a.set(j, temp); //set item at index j to temp
        }
113
114
115
        // Return the index of the left child of node i.
1169
        private static int leftChild(int i) {
117
            return 2*i + 1;
118
        }
119
120
        // Return the index of the right child of node i.
1219
        private static int rightChild(int i) {
122
            return 2*i + 2;
        }
123
124
125
        // Return the index of the parent of node i
126
        // (Parent of root will be -1)
        private static int parent(int i) {
1270
128
            return (i-1)/2;
129
        }
120
```

insert() adds a new item to the end and swaps with parent if needed

HeapMinPriorityQueue.java

```
чυ
       public void insert(E element) {
41⊝
           heap.add(element); // Put new value at end;
42
           int loc = heap.size()-1; // and get its location
43
44
45
           // Swap with parent until parent not larger
           while (loc > 0 && heap.get(loc).compareTo(heap.get(parent(loc))) < 0) {</pre>
46
               swap(heap, loc, parent(loc));
47
               loc = parent(loc);
48
49
           }
       }
50
```

extractMin() gets the root at index 0, moves last to root, and "re-heapifies"

HeapMinPriorityQueue.java

```
249
       public E extractMin() {
25
           if (heap.size() <= 0)</pre>
26
               return null;
27
           else {
               E minVal = heap.get(0); //min will be at node 0
28
29
               heap.set(0, heap.get(heap.size()-1)); // Move last to position 0
               heap.remove(heap.size()-1); //remove last item to maintain shape prope
30
               minHeapify(heap, 0); //recursively swap to maintain order property
31
32
               return minVal; //return min value
33
           }
       }
34
```

minHeapify() recursively enforces Shape and Order Properties

HeapMinPriorityQueue.java

107

```
79∍
        private static <E extends Comparable<E>> void
80
        minHeapify(ArrayList<E> a, int i) {
81
            int left = leftChild(i): // index of node i's left child
            int right = rightChild(i); // index of node i's right child
82
            int smallest; // will hold the index of the node with the smallest eleme
83
84
            // among node i, left, and right
85
86
           // Is there a left child and, if so, does the left child have an
87
           // element smaller than node i?
88
            if (left \leq a.size()-1 & a.get(left).compareTo(a.get(i)) \leq 0)
89
                smallest = left; // yes, so the left child is the largest so far
90
            else
91
                smallest = i:
                                 // no, so node i is the smallest so far
92
93
            // Is there a right child and, if so, does the right child have an
94
            // element smaller than the larger of node i and the left child?
95
            if (right <= a.size()-1 && a.get(right).compareTo(a.get(smallest)) < 0)
96
                smallest = right; // yes, so the right child is the largest
97
98
            // If node i holds an element smaller than both the left and right
           // children, then the min-heap property already held, and we need do
99
100
            // nothing more. Otherwise, we need to swap node i with the larger
            // of the two children, and then recurse down the heap from the larger children.
101
102
            if (smallest != i) {
103
                swap(a, i, smallest); //put smallest in spot i, largest in spot smalles
                minHeapify(a, smallest); //maintain heap starting from smallest index (
104
105
            }
        }
106
```

Run time analysis shows Priority Queue heap implementation better than previous

| | | Unsorted | Sorted |
|-----------|------|-----------|-----------|
| Operation | Неар | ArrayList | ArrayList |
| isEmpty | Θ(1) | Θ(1) | Θ(1) |

isEmpty()

• Each implement just checks size of ArrayList; Θ(1)
| Operation Heap | | Unsorted ArrayList | Sorted ArrayList |
|----------------|-----------------------|-----------------------|---------------------|
| isEmpty | Θ(1) | Θ(1) | Θ(1) |
| insert | O(log ₂ n) | Θ(1) | O(n) |

insert()

- Heap: insert at end Θ(1), then may have to bubble up height of tree; O(log₂ n)
- Unsorted ArrayList: just add on end of ArrayList; Θ(1)
- Sorted ArrayList: have to find place to insert O(n), then do insert, moving all other items; O(n)

| | | Unsorted | Sorted |
|-----------|-----------------------|--------------|-----------|
| Operation | Неар | ArrayList | ArrayList |
| isEmpty | Θ(1) | Θ(1) | Θ(1) |
| insert | O(log ₂ n) | Θ(1) | O(n) |
| minimum | Θ(1) | Θ (n) | Θ(1) |

minimum()

- Heap: return item at index 0 in ArrayList; Θ(1)
- Unsorted ArrayList: search Arraylist; Θ(n)
- **Sorted ArrayList:** return last item in ArrayList; Θ(1)

| | | Unsorted | Sorted |
|------------|-----------------------|--------------|-----------|
| Operation | Неар | ArrayList | ArrayList |
| isEmpty | Θ(1) | Θ(1) | Θ(1) |
| insert | O(log ₂ n) | Θ(1) | O(n) |
| minimum | Θ(1) | Θ (n) | Θ(1) |
| extractMin | O(log ₂ n) | Θ (n) | Θ(1) |

extractMin()

- Heap: return item at index 0, then replace with last item, then bubble down height of tree; O(log₂ n)
- Unsorted ArrayList: search Arraylist, Θ(n), remove, then move all other items; O(n)
- **Sorted ArrayList:** return last item in ArrayList; Θ(1)

| | | Unsorted | Sorted |
|------------|-----------------------|--------------|-----------|
| Operation | Неар | ArrayList | ArrayList |
| isEmpty | Θ(1) | Θ(1) | Θ(1) |
| insert | O(log ₂ n) | Θ(1) | O(n) |
| minimum | Θ(1) | Θ (n) | Θ(1) |
| extractMin | O(log ₂ n) | Θ (n) | Θ(1) |

With Unsorted ArrayList or Sorted ArrayList, can't escape paying O(n) (either insert or extractMin) Heap must pay $O(\log_2 n)$, but that is much better than O(n) when n is large Remember $O(\log_2 n)$ where n = 1 million is 20 (one billion is 30)



- 1. Priority Queue ADT
- 2. Implementation choices
- 3. Java's built-in PriorityQueue

Java implements a *PriorityQueue*, but with non-standard names

Java's PriorityQueue Operations

- *isEmpty == isEmpty*
- insert == add
- minimum == peek
- extractMin == remove

Why remove() instead of extractMin()? We will control if the min or max gets removed (next slides show how)

If we use our own Objects in *PriorityQueue*, need to provide way to compare objects

Student.java

Three ways to compare objects in Java's Priority Queue:

- Method 1: Objects stored in Priority Queue provide a compareTo() method
- Method 2: Instantiate a custom Comparator and pass to Priority Queue constructor
- Method 3: Use anonymous function in Priority Queue declaration

Use Student object to demonstrate the three Priority Queue methods

Student.java

```
11 public class Student implements Comparable<Student> {
12
       private String name;
13
       private int year;
14
15⊝
       public Student(String name, int year) {
16
            this.name = name;
17
           this.year = year;
       }
18
19
200
       /**
21
        * Comparable: just use String's version (lexicographic)
22
        */
230
       @Override
24
       public int compareTo(Student s2) {
25
            return name.compareTo(s2.name);
26
       }
27
289
       @Override
       public String toString() {
29
30
            return name + " '"+year;
31
       }
```

Method 1: Objects in Priority Queue provide *compareTo()* method

Student.java

| 33⊜ | <pre>public static void main(String[] args) {</pre> |
|-----|--|
| 34 | //create ArrayList of students and add some |
| 35 | <pre>ArrayList<student> students = new ArrayList<student>();</student></student></pre> |
| 36 | <pre>students.add(new Student("charlie", 18));</pre> |
| 37 | <pre>students.add(new Student("alice", 20));</pre> |
| 38 | <pre>students.add(new Student("bob", 19));</pre> |
| 39 | <pre>students.add(new Student("elvis", 21));</pre> |
| 40 | <pre>students.add(new Student("denise", 20));</pre> |
| 41 | <pre>System.out.println("original:" + students);</pre> |
| 42 | |
| 43 | // Three methods for using Comparator |
| 44 | |
| 45 | // Method 1: |
| 46 | // Create Java PriorityQueue and use Student |
| 47 | // class's compareTo method (lexicographic order) |
| 48 | // this is used if comparator not passed to PriorityQueue constructor |
| 49 | PriorityQueue <student> pq = new PriorityQueue<student>();</student></student> |
| 50 | pq.addAll(students); //add all Students in ArrayList in one statement |
| 51 | |
| 52 | <pre>//remove until empty (this essentially sorting!)</pre> |
| 53 | <pre>System.out.println("\nlexicographic:");</pre> |
| 54 | <pre>while (!pq.isEmpty()) System.out.println(pq.remove());</pre> |
| 55 | |
| 56 | |

🛐 Problems @ Javadoc 🗟 Declaration 📮 Console 🕱 🎋 Debug 🎋 Expressions 👰 Error Log 🍃 Call Hierarchy

<terminated> Student [Java Application] /Library/Java/JavaVirtualMachines/jdk1.8.0_112.jdk/Contents/Home/bin/java (Jan 10, 2018, 11:02:00 AM)
Original:[charlie '18, alice '20, bob '19, elvis '21, denise '20]

lexicographic: alice '20 bob '19 charlie '18 denise '20 elvis '21

If we use our own PriorityQueue, we need to provide way to compare objects

Student.java

Three ways to compare objects in Java's Priority Queue:

- Method 1: Objects stored in PriorityQueue provide a compareTo() method
- Method 2: Instantiate a custom Comparator and pass to Priority Queue constructor
 - Method 3: Use anonymous function in Priority Queue declaration

Method 2: Define custom Comparator and pass to Priority Queue constructor

Student.java

50

What if Object has *compareTo()* but you want a different order?

```
57
            // Method 2:
58
           // Use a custom Comparator.compare (length of name) instead
59
           // of using the element's compareTo function
60
           // Java will use this to compare two Students (here on length of name)
            class NameLengthComparator implements Comparator<Student> {
61∘
                public int compare(Student s1, Student s2) {
<u> 62</u>∍
63
                    return s1.name.length() - s2.name.length();
64
                3
65
66
            Comparator<Student> lenCompare = new NameLengthComparator();
            pq = new PriorityQueue<Student>(lenCompare); //passing Comparator to PriorityQueue
67
68
            pg.addAll(students); //add all students to PriorityOueue
           System.out.println("\nlength:");
69
70
            //remove until empty (sorting)
           while (!pq.isEmpty()) System.out.println(pq.remove());
71
72
73
74
75
76
77
78
79
80
81
       }
82 }
83
```

👔 Problems @ Javadoc 🗓 Declaration 📮 Console 🕱 🕸 Debug 🎋 Expressions 🔮 Error Log 🍃 Call Hierarchy

<terminated> Student [Java Application] /Library/Java/Java/JavaVirtualMachines/jdk1.8.0_112.jdk/Contents/Home/bin/java (Jan 10, 2018, 11:21:36 AM)

length: bob '19 elvis '21 alice '20 denise '20 charlie '18

Output sorted by length of name

If we use our own PriorityQueue, we need to provide way to compare objects

Student.java

- Three ways to compare objects in Java's Priority Queue:
- Method 1: Objects stored in Priority Queue provide a compareTo() method
- Method 2: Instantiate a custom Comparator and pass to Priority Queue constructor



Method 3: Use anonymous function in Priority Queue declaration

Student.java

| | 12 | |
|---|-------------------------------------|--|
| | 73 | //Method 3: |
| | 74 | // Use a custom Comparator via Java 8 anonymous function (here based on year) |
| | 75 | <pre>// pass Comparator to PriorityQueue constructor</pre> |
| | 76 | <pre>pq = new PriorityQueue<student>((Student s1, Student s2) -> s2.year - s1.year);</student></pre> |
| | 77 | pq.addAll(students); //add all students to Priority Queue |
| | 78 | <pre>System.out.println("\nyear:");</pre> |
| | 79 | <pre>//remove until empty (sorting)</pre> |
| | 80 | <pre>while (!pq.isEmpty()) System.out.println(pq.remove());</pre> |
| | 81 } | |
| | 82 } | |
| Ľ | 83 | |
| | 🚹 Problems @ Javad | loc 🖳 Declaration 📃 Console 🕱 🔆 Debug 🏘 Expressions 🕙 Error Log 🎲 Call Hierarchy |
| < | <terminated> Student [</terminated> | ava Application] /Library/Java/JavaVirtualMachines/jdk1.8.0_112.jdk/Contents/Home/bin/java (Jan 10, 2018, 11:21:36 AM) |
| 3 | year: | |
| (| elvis '21 | |
| 0 | denise '20 | |
| 0 | alice '20 | |
| ł | bob '19 | |
| | charlie '1 | 8 |
| 1 | | - |

PS-3



https://www.cs.dartmouth.edu/cs10/PS-3.html

Summary

- Priority queue have elements returned according to value (min or max)
 - Can implement with unsorted array and sorted array, each with different complexities
- Heaps are based on binary trees and have two main properties
 - Shape
 - Order
- Priority queue implemented with heap can be very efficient
- To use priority queues, objects need to have way to compare with each other
 - Three methods possible

Additional Resources

| Choice | Fit | Notes |
|-------------|--------------|--|
| Stack/Queue | \mathbf{X} | Elements ordered by arrival time Can only access one element (top or front) Element with higher priority that arrives out of sequence can not be reached |

| Choice | Fit | Notes |
|-------------|--------------|--|
| Stack/Queue | \mathbf{X} | Elements ordered by arrival time Can only access one element (top or front) Element with higher priority that arrives out of sequence can not be reached |
| Мар | × | Have to know the Key in order to find item In scheduling example, would have to check each minute 0 through 7 |

| Choice | Fit | Notes |
|---------------|---------|--|
| Stack/Queue | | Elements ordered by arrival time Can only access one element (top or front) Element with higher priority that arrives out of sequence can not be reached |
| Мар | × | Have to know the Key in order to find item In scheduling example, would have to check each minute 0 through 7 |
| Unsorted List | Ok ? | <i>insert()</i> fast, Θ(1) <i>extractMin()</i> slow – search entire List for min Key, Θ(n) |

| Choice | Fit | Notes |
|---------------|--------------|--|
| Stack/Queue | \mathbf{X} | Elements ordered by arrival time Can only access one element (top or front) Element with higher priority that arrives out of sequence can not be reached |
| Мар | \mathbf{X} | Have to know the Key in order to find item In scheduling example, would have to check each minute 0 through 7 |
| Unsorted List | Ok ? | <i>insert()</i> fast, Θ(1) <i>extractMin()</i> slow – search entire List for min Key, Θ(n) |
| Sorted List | Ok ? | <i>extractMin()</i> fast, Θ(1) <i>insert()</i> slow – find right place, make hole, O(n) |

| Choice | Fit | Notes |
|--------------------|---------|---|
| Stack/Queue | | Elements ordered by arrival time Can only access one element (top or front) Element with higher priority that arrives out of sequence can not be reached |
| Мар | × | Have to know the Key in order to find item In scheduling example, would have to check each minute 0 through 7 |
| Unsorted List | Ok ? | <i>insert()</i> fast, Θ(1) <i>extractMin()</i> slow – search entire List for min Key, Θ(n) |
| Sorted List | Ok ? | <i>extractMin()</i> fast, Θ(1) <i>insert()</i> slow – find right place, make hole, O(n) |
| Binary Search Tree | Неар | Not bad, but we do not enforce balance on BST <i>extractMin() O(h)</i> (could be better than O(n), but not necessarily) We will do better next class using a Heap |

We can implement a PriorityQueue with an unsorted ArrayList

Unsorted ArrayList implementation

| 15 | 6 | 9 | 27 |
|----|---|---|----|
|----|---|---|----|

Keep elements unsorted in ArrayList

isEmpty() is Θ(1) with an unsorted ArrayList

Unsorted ArrayList implementation

isEmpty()

| 15 | 6 | 9 | 27 |
|----|---|---|----|
|----|---|---|----|

isEmpty - just check ArrayList size() method

| Operation | Run | Notes |
|-----------|------|------------------|
| | time | |
| isEmpty | Θ(1) | Checks size == 0 |

insert() is also $\Theta(1)$ with an unsorted ArrayList

Unsorted ArrayList implementation

insert(12)

| 15 | 6 | 9 | 27 | 12 |
|----|---|---|----|----|
|----|---|---|----|----|

insert – just add element to end of ArrayList

| Operation | Run time | Notes |
|-----------|-------------|---------------------------|
| isEmpty | Θ(1) | Checks size == 0 |
| insert | Θ(1) | Add on to end (amortized) |

Unsorted ArrayList implementation

extractMin()

Check 15

| 15 | 6 | 9 | 27 | 12 |
|----|---|---|----|----|
|----|---|---|----|----|

extractMin – loop to find smallest and move last item to smallest index to fill hole

Operation Run Notes time isEmpty Checks size == 0 $\Theta(1)$ insert Add on to end (amortized) $\Theta(1)$ minimum Must loop through all elements to find smallest Θ(n) extractMin Loop through all elements and move to fill hole Θ(n)

Unsorted ArrayList implementation

extractMin()

Check 6

Smallest 15

extractMin – loop to find smallest and move last item to smallest index to fill hole

Operation Run Notes time

is Empty $\Theta(1)$ Checks size == 0

insert Θ(1) Add on to end (amortized)

^{minimum} Θ(n) Must loop through all elements to find smallest

extractMin Θ(n) Loop through all elements and move to fill hole

Unsorted ArrayList implementation

extractMin()

Check 9

Smallest 6



extractMin – loop to find smallest and move last item to smallest index to fill hole

OperationRunNotestimeisEmptyΘ(1)Checks size == 0

insert Θ(1) Add on to end (amortized)

^{minimum} Θ(n) Must loop through all elements to find smallest

extractMin Θ(n) Loop through all elements and move to fill hole

Unsorted ArrayList implementation

extractMin()

Check 27

Smallest 6



extractMin – loop to find smallest and move last item to smallest index to fill hole

Operation Notes Run time isEmpty Checks size == 0 $\Theta(1)$ insert Add on to end (amortized) $\Theta(1)$ minimum Must loop through all elements to find smallest Θ(n) extractMin Loop through all elements and move to fill hole Θ(n)

Unsorted ArrayList implementation

extractMin()

Check 12

Smallest 6



extractMin – loop to find smallest and move last item to smallest index to fill hole

Operation Notes Run time isEmpty Checks size == 0 $\Theta(1)$ insert Add on to end (amortized) $\Theta(1)$ minimum Must loop through all elements to find smallest Θ(n) extractMin Loop through all elements and move to fill hole Θ(n)



extractMin – loop to find smallest and move last item to smallest index to fill hole

Operation Notes Run time isEmpty Checks size == 0 $\Theta(1)$ insert Add on to end (amortized) $\Theta(1)$ minimum Must loop through all elements to find smallest Θ(n) extractMin Loop through all elements and move to fill hole Θ(n)



Return 6 <u>Fill hole with last item</u> No need to slide items left Nice We will use this trick again with Heaps

extractMin – loop to find smallest and move last item to smallest index to fill hole

| Operation | Run time | Notes |
|------------|-------------|---|
| isEmpty | Θ(1) | Checks size == 0 |
| insert | Θ(1) | Add on to end (amortized) |
| minimum | Θ(n) | Must loop through all elements to find smallest |
| extractMin | Θ(n) | Loop through all elements and move to fill hole |

We can implement a PriorityQueue with an unsorted ArrayList

ArrayListMinPriorityQueue.java

```
8 public class ArrayListMinPriorityQueue<E extends Comparable<E>>>
 9 implements MinPriorityOueue<E> {
10
       private ArrayList<E> list; // list of elements
11
129
       /**
13
        * Constructor
14
        */
       public ArrayListMinPriorityQueue() {
15⊝
           list = new ArrayList<E>();
16
17
       }
18
19∍
       /**
        * Is the priority queue empty?
20
21
        * @return true if the queue is empty, false if not empty.
22
        */
239
       public boolean isEmpty() {
24
           return list.size() == 0;
25
       }
26
279
       /**
        * Insert an element into the priority queue.
28
        * Keep in decreasing order
29
30
        * @param element the element to insert
31
        */
329
       public void insert(E element) {
           list.add(element);
33
34
       }
25
```

We can implement a PriorityQueue with an unsorted ArrayList

ArrayListMinPriorityQueue.java

```
private int indexOfMinimum() {
400
           // Search through the entire array for the smallest element.
41
42
           int smallestIndex = 0;
43
           for (int i = 1; i < list.size(); i++) {</pre>
44
                // If the current smallest is greater than the element at index i,
45
                // then make the element at index i the new smallest.
46
                if (list.get(smallestIndex).compareTo(list.get(i)) > 0)
47
                    smallestIndex = i;
48
           }
49
50
51
           return smallestIndex;
52
       }
53
54
55⊝
       /**
56
        * Return the element with the minimum key, and remove it from the aueue.
57
        * @return the element with the minimum key, or null if queue empty.
58
        */
59∍
       public E extractMin() {
60
           if (list.size() <= 0)</pre>
61
                return null;
62
           else {
                int smallest = indexOfMinimum(); // index of the element with the
63
                E minElement = list.get(smallest); // the actual element
64
65
                // Move the element in the last position to this position.
66
                // Faster than removing from the middle.
67
               list.set(smallest, list.get(list.size()-1));
68
69
70
                // We no longer have an element in that last position.
               list.remove(list.size()-1);
71
72
73
                // Return the element with the minimum key.
74
                return minElement;
75
           }
76
       }
```

There are several ways to implement a PriorityQueue, today we look at two

1. Unsorted List



We can improve *extractMin()* by using a sorted List, but inserts take more time

Sorted ArrayList implementation

| 27 | 15 | 9 | 6 |
|----|----|---|---|
|----|----|---|---|

Keep elements sorted in ArrayList with smallest always at end

isEmpty() is $\Theta(1)$ with a sorted ArrayList

Sorted ArrayList implementation

isEmpty()

| 27 | 15 | 9 | 6 |
|----|----|---|---|
|----|----|---|---|

isEmpty() - just check ArrayList size() method

| Operation | Run time | Notes |
|-----------|-------------|-------------------------------|
| isEmpty | Θ(1) | Return size, same as unsorted |
insert() is O(n) with a sorted ArrayList

Sorted ArrayList implementation

insert(12)

| 27 | 15 | 9 | 6 | 12 |
|----|----|---|---|----|
|----|----|---|---|----|

insert() – need to loop backward to find slot for new element, then move other elements right

OperationRun
timeNotes
timeisEmpty $\Theta(1)$ Return size, same as unsortedinsertO(n)Insert in place and move other items right

insert() is O(n) with a sorted ArrayList

Sorted ArrayList implementation

insert(12)



insert() – need to loop backward to find slot for new element, then move other elements right

OperationRun
timeNotes
timeisEmpty $\Theta(1)$ Return size, same as unsortedinsertO(n)Insert in place and move other items right

minimum() and *extractMin()* improve to Θ(1) with a sorted ArrayList

Sorted ArrayList implementation

extractMin()

| 27 | 15 | 12 | 9 | 6 |
|----|----|----|---|---|
|----|----|----|---|---|

extractMin() - just remove the last element

| Operation | Run time | Notes |
|------------|-------------|--|
| isEmpty | Θ(1) | Return size, same as unsorted |
| insert | O(n) | Insert in place and move other items right |
| minimum | Θ(1) | Get last element |
| extractMin | Θ(1) | Get last element, no need to move items |

minimum() and *extractMin()* improve to Θ(1) with a sorted ArrayList

Sorted ArrayList implementation

extractMin()



| 27 15 | 12 | 9 |
|-------|----|---|
|-------|----|---|

extractMin() - just remove the last element

| Operation | Run time | Notes |
|------------|-------------|--|
| isEmpty | Θ(1) | Return size, same as unsorted |
| insert | O(n) | Insert in place and move other items right |
| minimum | Θ(1) | Get last element |
| extractMin | Θ(1) | Get last element, no need to move items |

SortedArrayList implementation improves *extractMin()*, but at expense of *insert()*

SortedArrayListMinPriorityQueue.java

```
public void insert(E element) {
<u> 33</u>∍
             int p: // Current position in the list.
 34
 35
 36
             //loop backward from end toward front
 37
             //continue if new element larger than current element
 38
             for (p = \text{list.size}); p > 0 \& \text{list.get}(p-1).compareTo(element) < 0; p--)
 39
                  ;
 40
 41
             //add new element at index found
             list.add(p, element);
 42
 43
         }
 44
 45
         /**
 46∍
          * Return the element with the minimum key, without removing it from the queue.
 47
          * @return the element with the minimum key, or null if queue empty.
 48
          */
 49

    50

         public E minimum() {
 51
             if (list.size() == 0)
 52
                 return null:
 53
             else
                 return list.get(list.size() - 1); // Last item is smallest
 54
 55
         }
 56
 57⊝
         /**
 58
          * Return the element with the minimum key, and remove it from the queue.
          * @return the element with the minimum key, or null if queue empty.
 59
          */
 60
▲ 61<sup>☉</sup>
         public E extractMin() {
             if (list.size() == 0)
 62
                 return null:
 63
 64
             else {
                                                      // Shrink the size
 65
                 return list.remove(list.size()-1); // and return the smallest element
 66
             }
         }
 67
 68
```

Implementations have different strengths, but limited practical difference

| Operation | Unsorted | Sorted |
|------------|----------|--------|
| isEmpty | Θ(1) | Θ(1) |
| insert | Θ(1) | O(n) |
| minimum | Θ(n) | Θ(1) |
| extractMin | Θ(n) | Θ(1) |

- Generally have the same number of inserts as extracts, so often no real difference, unless just looking for min without extracting
- We will do better next class when we look at heaps!

MinPriorityQueue.java

ANNOTATED SLIDES

MinPriorityQueue.java specifies interface

As with BST, elements

MinPriorityQueue.java

```
must extend Comparable
                                                                        Allows Java to compare
 6 public interface MinPriorityQueue<E extends Comparable<E>> {
 7⊝
       /**
                                                                         elements and determine
 8
        * Is the priority queue empty?
        * @return true if the priority queue is empty, false if not empty. which one is smaller
 9
        */
10
                                                                         Uses compareTo()
       public boolean isEmpty();
11
                                                                         method on element
12
13⊝
       /**
                                                                         objects
14
        * Insert an element into the queue.

    Can make a Max Priority

15
        * @param element thing to insert
16
        */
                                                                         Queue by reversing the
17
       public void insert(E element);
                                                                         compareTo() method
18
       /**
19⊝
        * Return the element with the minimum key, without removing it from the queue.
20
21
        * @return the element with the minimum key in the priority queue
22
        */
                                                                         Note: no ability to get
23
       public E minimum();
                                                                         items by index!
24
25⊝
       /**
26
        * Return the element with the minimum key, and remove it from the queue.
27
        * @return the element with the minimum key in the priority queue
28
        */
                                                                         Can only extract smallest
29
       public E extractMin();
                                                                         (or largest) item
                                                                                                80
30 }
```

ArrayListMinPriorityQueue.java

ANNOTATED SLIDES

We can implement a PriorityQueue with an unsorted ArrayList

•

ArrayListMinPriorityQueue.java

```
8 public class ArrayListMinPriorityQueue<E extends Comparable<E>>>
 9 implements MinPriorityOueue<E> {
       private ArrayList<E> list; // list of elements
10
11
129
       /**
13
        * Constructor
14
        */
15⊝
       public ArrayListMinPriorityQueue() {
           list = new ArrayList<E>();
16
17
       }
18
       /**
199
20
        * Is the priority queue empty?
                                                false if not empty.
21
        * @return true if the queue is empty.
22
        */
       public boolean isEmpty() {
239
24
           return list.size() == 0;
25
       }
26
270
       /**
        * Insert an element into the priority queue.
28
        * Keep in decreasing order
29
30
        * @param element the element to insert
31
        */
329
       public void insert(E element) {
33
           list.add(element);
34
       }
25
```

- Implements MinPriorityQueue interface using ArrayList
 - Store elements in ArrayList called *list*
- Elements must provide compareTo()
 because we say E extends
 Comparable
- isEmpty() just checks ArrayList size()
 method
- Inserting is easy, just tack new element on to end of ArrayList

We can implement a PriorityQueue with an unsorted ArrayList

ArrayListMinPriorityQueue.java

```
private int indexOfMinimum() {
400
41
           // Search through the entire array for the smallest element.
                                                                            Loop through all elements,
42
           int smallestIndex = 0;
43
                                                                            compare (using compareTo()) with
           for (int i = 1; i < list.size(); i++) {</pre>
44
               // If the current smallest is greater than the element at index i,
45
                                                                             smallest so far, return index of
               // then make the element at index i the new smallest.
46
               if (list.get(smallestIndex).compareTo(list.get(i)) > 0)
47
                                                                            smallest element Θ(n)
                   smallestIndex = i;
48
           }
49
50
51
           return smallestIndex;
52
       }
53
54
                                                                                    extractMin() finds smallest
55⊝
       /**
                                                                                    index with call to indexOfMin()
56
        * Return the element with the minimum key, and remove it from the queue.
57
        * @return the element with the minimum key, or null if queue empty.
58
        */
59<sup>o</sup>
       public E extractMin() {
60
           if (list.size() <= 0)</pre>
61
               return null;
62
           else {
               int smallest = indexOfMinimum(); // index of the element with the
63
                                                                                   Store smallest element
               E minElement = list.get(smallest); // the actual element
64
65
66
               // Move the element in the last position to this position.
               // Faster than removing from the middle.
67
                                                                                  Move last element into index
68
               list.set(smallest, list.get(list.size()-1));
69
                                                                                  of smallest to avoid creating a
70
               // We no longer have an element in that last position.
              list.remove(list.size()-1);
71
                                                                                   hole
72
               // Return the element with the minimum key.
73
74
               return minElement;
                                                                   Remove last item and then
                                                                                                                            83
75
           }
76
       }
                                                                   return smallest element
77
```

SortedArrayListMinPriorityQueue.java

ANNOTATED SLIDES

SortedArrayList implementation improves *extractMin()*, but at expense of *insert()*

SortedArrayListMinPriorityQueue.java

Store elements in ArrayList called list



HeapMinPriorityQueue.java

ANNOTATED SLIDES



NOTE: example was for a MAX Priority Queue, this code implements a <u>MIN</u> Priority Queue

Easy to change to this code to a MAX Priority Queue

Helper functions make finding parent and children easy

HeapMinPriorityQueue.javaHelper functions108// Swap two locations i and j in ArrayList a.

```
// Swap two locations i and j in ArrayList a.
        private static <E> void swap(ArrayList<E> a, int i, int j) {
1099
110
            E temp = a.get(i); //temporarily hold item at index i
            a.set(i, a.get(j)); //set item at index i to item at index j
111
            a.set(j, temp); //set item at index j to temp
112
        }
113
114
115
        // Return the index of the left child of node i.
1169
        private static int leftChild(int i) {
117
            return 2*i + 1;
                                                 leftChild(), rightChild() and parent()
118
        }
                                                 calculate positions of nodes relative to i
119
        // Return the index of the right child of node i.
120
        private static int rightChild(int i) {
1219
122
            return 2*i + 2;
123
        }
124
        // Return the index of the parent of node i
125
        // (Parent of root will be -1)
126
        private static int parent(int i) {
1279
128
            return (i-1)/2;
```

129

}

insert() adds a new item to the end and swaps with parent if needed

HeapMinPriorityQueue.java



• Start at newly added item's index

```
τυ
       public void insert(E element)
41⊝
           heap.add(element);
42
                                       // Put new value at end;
           int loc = heap.size()-1;
43
                                       // and get its location
44
45
           // Swap with parent until parent not larger
           while (loc > 0 && heap.get(loc).compareTo(heap.get(parent(loc))) < 0) {</pre>
46
                swap(heap, loc, parent(loc));
47
                loc = parent(loc);
48
49
            }
       }
50
```

insert() adds a new item to the end and repeatedly swaps with parent if needed

HeapMinPriorityQueue.java



```
• Start at newly added item's index
```

NOTE: reverse compareTo
inequality to implement a
// Put new value at end; MAX Priority Queue

```
41⊕
42
43
44
45
46
```

47

48 49

50

}

чυ

```
// Swap with parent until parent not larger
while (loc > 0 && heap.get(loc).compareTo(heap.get(parent(loc))) < 0) {
    swap(heap, loc, parent(loc));
}</pre>
```

// and get its location

loc = parent(loc);
}

public void insert(E element)

int loc = heap.size()-1;

heap.add(element);

```
• Swap if not root (loc==0) and element < parent
```

- Continue to "bubble up" inserted node until reach root or element > parent
- At most O(h) swaps (if new node goes all the way up to root)
- Due to Shape Property, max h is log₂ n, so O(log₂ n)

extractMin() gets the root at index 0, moves last to root, and "re-heapifies"

HeapMinPriorityQueue.java



Where will smallest element be?

minHeapify() recursively enforces Shape and Order Properties

HeapMinPriorityQueue.java

| 79⊜ | privo | te static <e comparable<e="" extends="">> void</e> |
|-----|-------|--|
| 80 | minHe | apify(ArrayList <e> a, int i) {</e> |
| 81 | i | <pre>nt left = leftChild(i); // index of node i's left child</pre> |
| 82 | i | nt right = rightChild(i); // index of node i's right child Get left and right child |
| 83 | i | nt smallest; // will hold the index of the node with the smallest elem |
| 84 | / | / among node i, left, and right |
| 85 | | |
| 86 | / | / Is there a left child and, if so, does the left child have an • Find the smallest node |
| 87 | / | / element smaller than node i? |
| 88 | i | f (left <= a.size()-1 && a.get(left).compareTo(a.get(i)) < 0) |
| 89 | | smallest = left; // yes, so the left child is the largest so far node. and the (possibly) |
| 90 | e | lse |
| 91 | | <pre>smallest = i; // no, so node i is the smallest so far two children</pre> |
| 92 | | Track smallest index in |
| 93 | / | / Is there a right child and, if so, does the right child have an |
| 94 | / | / element smaller than the larger of node i and the left child? smallest variable |
| 95 | i | f (right <= a.size()-1 && a.get(right).compareTo(a.get(smallest)) < 0) |
| 96 | | <pre>smallest = right; // yes, so the right child is the largest</pre> |
| 97 | | If starting index is |
| 98 | / | / If node i holds an element smaller than both the left and right |
| 99 | / | / children, then the <u>min</u> -heap property already held, and we need do not the sinallest , |
| 100 | / | / nothing more. Otherwise, we need to swap node i with the larger then swap node at |
| 101 | / | / of the two children, and then recurse down the heap from the larger chil |
| 102 | i | f (smallest != i) { Starting index with |
| 103 | | <pre>swap(a, i, smallest); //put smallest in spot i, largest in spot smallest node</pre> |
| 104 | | minHeapify(a, smallest); //maintain heap starting from smallest index (|
| 105 | } | • Bubble down node |
| 106 | } | At most $O(n) = O(log_2 n)$ operations from smallest index |
| 107 | | nom smalest mack |

a = heap, i = starting index

Heap Sort

SUPPLEMENTAL MATERIAL

Using a heap, we can sort items "in place" in a two-stage process

Heap sort

Given array in unknown order

- 1. Build max heap in place using array given
 - Start with last non-leaf node, max heapify node and children
 - Move to next to last non-leaf node, max heapify again
 - Repeat until at root
 - NOTE: heap is not necessarily sorted, only know for sure that parent > children and max is at root
- 2. Extract max (index 0) and swap with item at end of array, then rebuild heap not considering last item

Does not require additional memory to sort

Build heap given unsorted array

Array



Conceptual heap tree



Non heap!

- Start at last non-leaf and heapify
- Repeat for other non-leaf nodes

Build heap given unsorted array

Array





Last non-leaf will be parent of last leaf

- Start at last non-leaf and heapify
- Repeat for other non-leaf nodes

Build heap given unsorted array

Array

Conceptual heap tree



Max heapify Swap 4 and 5

- Start at last non-leaf and heapify
- Repeat for other non-leaf nodes

Build heap given unsorted array

Array

Conceptual heap tree



- Start at last non-leaf and heapify
- Repeat for other non-leaf nodes

Build heap given unsorted array

Array



- Start at last non-leaf and heapify
- Repeat for other non-leaf nodes

Build heap given unsorted array

Array



Max heapify Swap 2 and 7

- Start at last non-leaf and heapify
- Repeat for other non-leaf nodes

Build heap given unsorted array

Array

Conceptual heap tree



Max heapify Swap 2 and 7

- Start at last non-leaf and heapify
- Repeat for other non-leaf nodes

Build heap given unsorted array

Array



- Start at last non-leaf and heapify
- Repeat for other non-leaf nodes

Build heap given unsorted array

Array

Conceptual heap tree



Max heapify In order, no need to swap

- Start at last non-leaf and heapify
- Repeat for other non-leaf nodes

Build heap given unsorted array

Array



Conceptual heap tree



Given array in unsorted order First build a heap in place

- Start at last non-leaf and heapify
- Repeat for other non-leaf nodes

Now it's a max heap! Satisfies Shape and Order Properties

After building the heap, parents are larger than children, but items may not be sorted

Array

| 9 7 5 2 6 4 |
|-------------|
|-------------|

Heap array after construction

Conceptual heap tree



Heap order is maintained here

Looping over array does not give elements in sorted order

Traversing tree doesn't work either

- Preorder = 9,7,2,6,5,4
- Inorder = 2,7,6,9,4,5
- Post order = 2,6,7,4,5,9

Step 2: Repeatedly *extractMax()* and store at end, rebuild heap on n-1 items

Heap on left, sorted on right

Array

Conceptual heap tree



extractMax() = 9 Swap with last item in array

Step 2: Repeatedly *extractMax()* and store at end, rebuild heap on n-1 items

Heap on left, sorted on right

Array

Conceptual heap tree



extractMax() = 9 Swap with last item in array

Step 2: Repeatedly *extractMax()* and store at end, rebuild heap on n-1 items

Heap on left, sorted on right



Conceptual heap tree



Rebuild heap on n-1 items
Heap on left, sorted on right





Heap on left, sorted on right



Swap 4 with largest child 7



Max heapify Swap 7 and 4

Heap on left, sorted on right





Max heapify Swap 7 and 4

Heap on left, sorted on right



Swap 4 with largest child 6 Conceptual heap tree



Max heapify Swap 4 and 6

Heap on left, sorted on right



Conceptual heap tree
7
6
5

Max heapify Swap 4 and 6

4

Heap on left, sorted on right



Conceptual heap tree



Heap built

Heap on left, sorted on right



Heap array

Conceptual heap tree



extractMax() = 7 Swap with last item in array

Heap on left, sorted on right



Heap array

Swap 4 with largest child 6



Max heapify Swap 4 and 6

Heap on left, sorted on right



Heap array



Heap built

Heap on left, sorted on right



Heap array

Swap 2 with largest child 5 Conceptual heap tree



Max heapify Swap 5 and 2

extractMax() = 6 Swap with last item in array

Heap on left, sorted on right



Heap array

Conceptual heap tree



Heap built

Heap on left, sorted on right



Heap array

Conceptual heap tree



extractMax() = 5 Swap with last item in array

Heap on left, sorted on right



Heap array

Rebuild heap on n-4 items

Conceptual heap tree



Max heapify Swap 4 and 2

Heap on left, sorted on right



Heap array

Conceptual heap tree



Heap built

Heap on left, sorted on right



Conceptual heap tree



Heap array

extractMax() = 4 Swap with last item in array

Heap on left, sorted on right

Sorted 2 4 5 6 7 9 Conceptual heap tree

Heap array

Done Items sorted in place **No extra memory used**

Heapsort.java: First build heap, then extractMin, rebuilt heap...

```
9 public class Heapsort<E extends Comparable<E>> {
       //no constructor! instead we sort arrays in place
10
11
       /**
129
        * Sort the array a[0..n-1] *inplace* using the heapsort algorithm.
13
14
        */
15⊝
       public void sort(E[] a, int n) {
           heapsort(a, n - 1);
16
17
       }
18
19⊝
       /**
20
        * Sort the array a[0..lastLeaf] by the heapsort algorithm.
21
        */
229
       private void heapsort(E[] a, int lastLeaf) {
23
           // First, turn the array a[0..lastLeaf] into a max-heap.
24
           buildMaxHeap(a, lastLeaf);
25
26
          // Once the array is a max-heap, repeatedly swap the root
27
          // with the last leaf, putting the largest remaining element
28
          // in the last leaf's position, declare this last leaf to no
29
          // longer be in the heap, and then fix up the heap.
           while (lastLeaf > 0) {
30
31
               swap(a, 0, lastLeaf); // swap the root with the last leaf
                                          // the last leaf is no longer in the heap
32
               lastLeaf--;
33
               maxHeapify(a, 0, lastLeaf); // fix up what's left
34
           }
35
       }
```

~ ~

Heapsort.java: First build heap, then extractMin, rebuilt heap...

```
private void maxHeapify(E[] a, int i, int lastLeaf) {
42⊝
           int left = leftChild(i); // index of node i's left child
43
                                      // index of node i's right chil
           int right = rightChild(i);
44
45
           int largest:
                                         // will hold the index of the n
46
           // Is there a left child and, if so, does the left child have
47
           if (left <= lastLeaf && a[left].compareTo(a[i]) > 0)
48
               largest = left; // yes, so the left child is the largest
49
50
           else
51
               largest = i;
                              // no, so node i is the largest so far
52
53
           // Is there a right child and, if so, does the right child ha
           // element larger than the larger of node i and the left chil
54
           if (right <= lastLeaf && a[right].compareTo(a[largest]) > 0)
55
               largest = right; // yes, so the right child is the larges
56
57
           /*
58
            * If node i holds an element larger than both the left and r
59
            * children, then the max-heap property already held, and we
60
            * nothing more. Otherwise, we need to swap node i with the l
61
            * of the two children, and then recurse down the heap from t
62
63
            * child.
            */
64
           if (laraest != i) {
65
66
               swap(a, i, largest);
67
               maxHeapify(a, largest, lastLeaf);
68
           }
69
       }
70
71⊝
       /**
72
        * Form array a[0..lastLeaf] into a max-heap.
73
        */
74⊝
       private void buildMaxHeap(E[] a, int lastLeaf) {
           int lastNonLeaf = (lastLeaf - 1) / 2; // nodes lastNonLeaf+1
75
76
           for (int j = lastNonLeaf; j \ge 0; j--)
               maxHeapify(a, j, lastLeaf);
77
78
       3
```

Heapsort in two steps

Given array in unknown order

- 1. Build max heap in place using array given
 - Start with last non-leaf node, max heapify node and children
 - Move to next to last non-leaf node, max heapify again
 - Repeat until at root
 - NOTE: heap is not necessarily sorted, only know parent > children and max is at root
- 2. Extract max (index 0) and swap with item at end of array, then rebuild heap not considering last item

Does not require additional memory to sort

Run time:

Building heap is O(n) – see course web page (most nodes are leaves) Each extractMax/swap might need $O(log_2 n)$ operations to restore Heap Make n-1 = O(n) extractMax/swaps to get array in sorted order Total run time is $O(n) + O(n \log_2 n) = O(n \log_2 n)$

Heapsort.java

ANNOTATED SLIDES

Heapsort.java: First build heap, then extractMin, rebuilt heap...

```
Code very similar to
 9 public class Heapsort<E extends Comparable<E>> {
                                                               HeapMinPriorityQueue.java
       //no constructor! instead we sort arrays in place
10
11
129
       /**
13
        * Sort the array a[0..n-1] *inplace* using the heapsort algorithm.
                                                         Sort() method calls helper with
14
        */
15⊝
       public void sort(E[] a, int n) { .
                                                         size of heap to consider
           heapsort(a, n - 1);
16
                                                         Initially consider each element
17
       }
18
19∍
       /**
20
        * Sort the array a[0..lastLeaf] by the heapsort algorithm.
21
        */
                                                                    First build heap from root to
229
       private void heapsort(E[] a, int lastLeaf) {
                                                                    last element to be considered
           // First, turn the array a[0..lastLeaf] into a max-heap.
23
                                                                    (initially last element, then n-2,
           buildMaxHeap(a, lastLeaf);
24
25
           // Once the array is a max-heap, repeatedly swap the root
26
           // with the last leaf, putting the largest remaining element
// in the last leaf's position, declare this last leaf to not at root, (lastLeaf > 0)
27
28
                                                                       Swap root and last element
29
           // longer be in the heap, and then fix up the heap.
30
           while (lastLeaf > 0) {
31
               swap(a, 0, lastLeaf);
                                          // swap the root with the last leaf
32
                                            // the last leaf is no longer in the heap
               lastLeaf--;
33
               maxHeapify(a, 0, lastLeaf); // fix up what's left
                                                                       Reduce size of heap to consider
34
           }
                                                                       Rebuild smaller heap
35
       }
                                                                                                  129
~ ~
                                                                       Done when at root
```

Heapsort.java: First build heap, then extractMin, rebuilt heap...

private void maxHeapify(E[] a, int i, int lastLeaf) { 42⊝ int left = leftChild(i); // index of node i's left child 43 // index of node i's right chel int right = rightChild(i); 44 // will hold the index of the n 45 int largest: 46 // Is there a left child and, if so, does the left child have 47 if (left <= lastLeaf && a[left].compareTo(a[i]) > 0) 48 largest = left; // yes, so the left child is the largest 49 50 else 51 largest = i; // no, so node i is the largest so far 52 53 // Is there a right child and, if so, does the right child ha // element larger than the larger of node i and the left chil 54 if (right <= lastLeaf && a[right].compareTo(a[largest]) > 0) 55 largest = right; // yes, so the right child is the larges 56 57 /* 58 * If node i holds an element larger than both the left and r 59 * children, then the max-heap property already held, and we 60 * nothing more. Otherwise, we need to swap node i with the l 61 * of the two children, and then recurse down the heap from t 62 63 * child. */ 64 if (laraest != i) { 65 66 swap(a, i, largest); 67 maxHeapify(a, largest, lastLeaf); 68 } 69 } 70 /** 71⊝ * Form array a[0..lastLeaf] into a max-heap. 72 73 */ private void buildMaxHeap(E[] a, int lastLeaf) { 74⊝ 75 int lastNonLeaf = (lastLeaf - 1) / 2; // nodes lastNonLeaf+1 76 for (int $j = lastNonLeaf; j \ge 0; j--$) maxHeapify(a, j, lastLeaf); 77 78 3

Finds largest between *i* and two children

If *largest* not *i*, swap *i* and *largest* Recursively call *maxHeapify()* to bubble down *i* to right place

- buildHeap() builds heap from last non-leaf node (parent of last leaf)
- Calls *maxHeapify()* on each non-leaf node until hit root ¹³⁰

Student.java – Method 1 with compareTo

ANNOTATED SLIDES

Use Student object to demonstrate the three Priority Queue methods

| Stude | ent.java | Student class implements |
|------------------------------------|--|---|
| 11 pu 12 13 14 | blic class Student implements Compar private String name; private int year; Student store student's name | able <student> {Comparable soes data about a me and yearPriorityQueue holding Student objects can compare students</student> |
| 15⊖ 16 17 18 19 20⊝ | <pre>public Student(String name, int ye this.name = name; this.year = year; } /**</pre> | ar) { If we are going to use <i>Student</i> in a PriorityQueue, need a way to tell which ones are bigger, the same, or smaller than other Students |
| 21 22 23© | <pre>* Comparable: just use String's v */ @Override</pre> | ersion (lexicographic) This approach sorts increasing alphabetically by student name |
| 24 25 26 27 | <pre>public int compareTo(Student s2) { return name.compareTo(s2.name) }</pre> | Here we use the built in String compareTo() method to evaluate Students based on name (could reverse compareTo() for descending order) |
| 28⊖ 29 30 31 | <pre>@Override public String toString() { return name + " '"+year; }</pre> | If this name < s2.name return negative If this name equals s2.name return 0 ¹³² If this name > s2.name return positive |

Method 1: Objects in Priority Queue provide *compareTo()* method

Student.java

| 330 | <pre>public static void main(String[] args) {</pre> | |
|----------------|---|--|
| 34 | //create ArravList of students and add some | |
| 35 | ArrayList <student> students = new ArrayList<student>():</student></student> | |
| 36 | <pre>students.add(new Student("charlie", 18));</pre> | |
| 37 | <pre>students.add(new Student("alice", 20));</pre> | |
| 38 | <pre>students.add(new Student("bob", 19));</pre> | |
| 39 | <pre>students.add(new Student("elvis", 21));</pre> | |
| 40 | <pre>students.add(new Student("denise", 20));</pre> | |
| 41 | <pre>System.out.println("original:" + students);</pre> | |
| 42 | | |
| 43 | // Three methods for using Comparator | |
| 44 | | |
| 45 | // Method 1: | |
| 46 | // Create Java PriorityQueue and use Student | |
| 47 | // class's compareTo method (lexicographic order) | |
| 48 | // this is used if comparator not passed to PriorityQueve constructor | |
| 49 | PriorityQueue <student> pg = new PriorityQueue<student>();</student></student> | |
| 50 | pg.addAll(students); //add all Students in ArrayList in one statement | |
| 51 | | |
| 52 | <pre>//remove until empty (this essentially sortingl)</pre> | |
| 53 | <pre>System.out.println("\nlexicographic:");</pre> | |
| 54 | <pre>while (!pq.isEmpty()) System.out.println(pq.remove());</pre> | |
| 55 | | |
| 56 | | |
| Problems |) Javadoc 👰 Declaration 📮 Console 🕱 🎋 Debug 🏘 Expressions 🔮 Error Log 🎇 Constitierarchy | |
| terminated> St | Jdent [Java Application] /Library/Java/JavaVirtualMachines/jdk1.8.0_112.jdk/Contents/Home/bin/java (Jan 12.2018, 11:02:00 AM) | |
| urigina | L'Elemente 10, allee 20, DOD 13, elvis 21, dempe 20] | |

lexicographic: Output in alphabetical order
alice '20
bob '19
charlie '18
denise '20
elvis '21

- Student Objects added to ArrayList in undefined order
- Student objects have name and year instance variables
 - Priority Queue created to hold Student Objects
 - No Comparator provided in constructor
 - By default PriorityQueue will use *Student* object's
 - compareTo() to find min Key
 - ArrayList of students is added to PriorityQueue with addAll() method

133

- Output in sorted order
- Each time while loop executes, removes smallest Student object using compareTo()

Student.java – Method 2 with comparator

ANNOTATED SLIDES

Method 2: Define custom Compator and pass to Priority Queue constructor

Still in main()

Student.java What if Object has *compareTo()* but • you want a different order?

Define Comparator class that 50 57 // Method 2: requires compare() method // Use a custom Comparator.compare (length of name) instead 58 // of using the element's compareTo function 59 compare() has two Student params // Java will use this to compare two Students (her length of name)* 60 61∘ class NameLengthComparator implements Comparator<Student> { Here we use length of *name* to <u></u>62∍ public int compare(Student s1, Student s2) { 63 return s1.name.length() - s2.name.length(); compare two Student Objects 64 3 65 compare() returns negative, equal, Comparator<Student> lenCompare = new NameLengthComparator(); 66 pq = new PriorityQueue<Student>(lenCompare); passing Comparator to PriorityQueue Or positive same as compareTo() 67 68 69 System.out.println("\nlength:"); **Instantiate new Comparator** //remove until empty (sorting) 70 while (!pq.isEmpty()) System.out.println(pq.remove()); 71 **Create new Priority Queue and** 72 73 //Method 3: // Use a custom Comparator via Java 8 anonymous function (here based on year) pass Comparator in constructor 74 75 // pass Comparator to PriorityOueue constructor pq = new PriorityQueue<Student>((Student s1, Student s2) -> s2.year - s1.year Then fill Priority Queue with 76 pq.addAll(students); //add all students to Priority Queu 77 students System.out.println("\nyear:"); 78 79 //remove until empty (sorting) Sort by looping until Priority 80 while (!pq.isEmpty()) System.out.println(pq.remove()); 81 3 Queue empty 82 } 83 Each time remove Student with 🛐 Problems 🕜 Javadoc 😟 Declaration 📮 Console 🕱 掾 Debug 🙀 Expressions 👰 Error Log 🎲 Call Hierarchy <terminated> Student [Java Application] /Library/Java/JavaVirtualMachines/jdk1.8.0_112.jdk/Contents/Home/bin/java (Jan 10, 2018, 11:21:36 AM)

length: bob '19 elvis '21 alice '20 denise '20 charlie '18

Output sorted by length of name

135

smallest Key as determined by

Comparator *instead of*

Student's compareTo()

Student.java – Method 3 with anonymous function

ANNOTATED SLIDES

Method 3: Use anonymous function in Priority Queue declaration

Student.java



EXAMPLE OF READING FILE

Use a BufferedReader to read a file line by line until reaching the end of file

Roster.java

```
BufferedReader input = new BufferedReader(new FileReader(fileName));
String line;
int lineNum = 0;
while ((line = input.readLine()) != null) {
   System.out.println("read @"+lineNum+"`"+line+"'");
   lineNum++;
}
```

- BufferedReader opens file with name filename
- Reading will start at beginning of file
- Each line from file stored in line in while loop
- input.readLine will return null at end of file
- Here we are just printing each line

Roster.java

117

```
769
        public static List<Student> readRoster2(String fileName) throws IOException {
 77
            List<Student> roster = new ArrayList<Student>();
 78
            BufferedReader input;
 79
 80
            // Open the file, if possible
 81
            try {
 82
                input = new BufferedReader(new FileReader(fileName));
 83
            }
 84
            catch (FileNotFoundException e) {
 85
                System.err.println("Cannot open file.\n" + e.getMessage());
 86
                return roster;
 87
 88
            // Read the file
 89
 90
            try {
 91
                // Line by line
 92
                 String line;
 93
                int lineNum = 0;
 94
                 while ((line = input.readLine()) != null) {
 95
                    System.out.println("read @"+lineNum+"`"+line+"'");
 96
                    // Comma separated
 97
                    String[] pieces = line.split(",");
                    if (pieces.length != 2) {
 98
 99
                         //did not get two elements in this line, output an error message
                         System.err.println("bad separation in line "+lineNum+":"+line);
100
                    }
101
102
                    else {
103
                         // got two elements for this line
104
                         try {
105
                             // Extract year as an integer, if possible
                             Student s = new Student(pieces[0], Integer.parseInt(pieces[1]));
106
                             System.out.println("=>"+s);
107
108
                             roster.add(s); //good student, add to roster
109
                         3
110
                         catch (NumberFormatException e) {
111
                             // couldn't parse second element as integer
                             System.err.println("bad number in line "+lineNum+":"+line);
112
113
                         }
114
                    }
115
                     lineNum++;
116
                }
```

- Many possible exceptions reading data from a file:
 - File may not be found
 - Some data might be missing (e.g., name without a year)
 - Some data might be invalid (e.g., year is not a valid Integer)

Roster.java

117

```
public static List<Student> readRoster2(String fileName) throws IOException {
 769
 77
            List<Student> roster = new ArrayList<Student>();
 78
            BufferedReader input;
 79
 80
            // Open the file, if possible
 81
            try {
                                                                                          •
 82
                 input = new BufferedReader(new FileReader(fileName));
 83
            }
 84
            catch (FileNotFoundException e) {
 85
                System.err.println("Cannot open file.\n" + e.getMessage());
                                                                                          •
 86
                return roster;
 87
 88
 89
            // Read the file
                                                                                          •
 90
            try {
                // Line by line
 91
 92
                 String line;
 93
                int lineNum = 0;
 94
                 while ((line = input.readLine()) != null) {
 95
                    System.out.println("read @"+lineNum+"`"+line+"'");
 96
                    // Comma separated
 97
                    String[] pieces = line.split(",");
                    if (pieces.length != 2) {
 98
 99
                         //did not get two elements in this line, output an error message
                         System.err.println("bad separation in line "+lineNum+":"+line);
100
                    }
101
102
                    else {
103
                         // got two elements for this line
104
                         try {
105
                             // Extract year as an integer, if possible
106
                             Student s = new Student(pieces[0], Integer.parseInt(pieces[1]));
107
                             System.out.println("=>"+s);
108
                             roster.add(s); //good student, add to roster
109
                         3
110
                         catch (NumberFormatException e) {
111
                             // couldn't parse second element as integer
                             System.err.println("bad number in line "+lineNum+":"+line);
112
113
                         }
114
                    }
115
                     lineNum++;
116
                }
```

- This method reads a comma separated variable (csv) file
- Each line should have student name and year
- Creates a Student Object from each line of the file
- Returns a List of Student
 Objects with one entry for each valid line
- File name to read is passed as
 String parameter

Roster.java

117

```
public static List<Student> readRoster2(String fileName) throws IOException {
 769
 77
            List<Student> roster = new ArrayList<Student>();
 78
            BufferedReader input;
 79
 80
            // Open the file, if possible
 81
            try {
                                                                                       •
 82
                input = new BufferedReader(new FileReader(fileName));
 83
            }
 84
            catch (FileNotFoundException e) {
 85
                System.err.println("Cannot open file.\n" + e.getMessage());
 86
                return roster:
 87
                               Create new BufferedReader
 88
 89
            // Read the file
                                Catch error if file not found
 90
            try {
                // Line by line
 91
 92
                String line;
 93
                int lineNum = 0;
 94
                while ((line = input.readLine()) != null) {
 95
                    System.out.println("read @"+lineNum+"`"+line+"'");
 96
                    // Comma separated
 97
                    String[] pieces = line.split(",");
                    if (pieces.length != 2) {
 98
 99
                        //did not get two elements in this line, output an error message
                        System.err.println("bad separation in line "+lineNum+":"+line);
100
                    }
101
102
                    else {
103
                        // got two elements for this line
104
                        try {
105
                            // Extract year as an integer, if possible
                            Student s = new Student(pieces[0], Integer.parseInt(pieces[1]));
106
107
                            System.out.println("=>"+s);
108
                            roster.add(s); //good student, add to roster
109
                        3
110
                        catch (NumberFormatException e) {
111
                            // couldn't parse second element as integer
                            System.err.println("bad number in line "+lineNum+":"+line);
112
113
                        }
114
                    }
115
                    lineNum++;
116
                }
```

- This method reads a comma separated variable (csv) file
- Each line should have student name and year
- Creates a Student Object from each line of the file
- Returns a List of Student Objects with one entry for each valid line
- File name to read is passed as
 String parameter

Roster.java

117

```
public static List<Student> readRoster2(String fileName) throws IOException {
 769
 77
            List<Student> roster = new ArrayList<Student>();
 78
            BufferedReader input;
 79
 80
            // Open the file, if possible
 81
            try {
 82
                input = new BufferedReader(new FileReader(fileName));
 83
            }
 84
            catch (FileNotFoundException e) {
 85
                System.err.println("Cannot open file.\n" + e.getMessage());
 86
                return roster:
 87
                               Create new BufferedReader
 88
 89
            // Read the file
                                Catch error if file not found
 90
            try {
 91
                // Line by line
 92
                String line;
 93
                int lineNum = 0;
 94
                while ((line = input.readLine()) != null) {
                    System.out.println("read @"+lineNum+"`"+line+"'");
 95
 96
                    // Comma separated
 97
                    String[] pieces = line.split(",");
                    if (pieces.length != 2) {
 98
                        //did not get two elements in this line, output an error message
 99
                        System.err.println("bad separation in line "+lineNum+"+line);
100
                    }
101
102
                    else {
103
                        // got two elements for this line
104
                        try {
105
                            // Extract year as an integer, if possible
                            Student s = new Student(pieces[0], Integer.parseInt(pieces[1]));
106
107
                            System.out.println("=>"+s);
108
                            roster.add(s); //good student, add to roster
109
                        3
110
                        catch (NumberFormatException e) {
111
                            // couldn't parse second element as integer
                            System.err.println("bad number in line "+lineNum+":"+line);
112
113
                        }
114
                    }
115
                    lineNum++;
116
                }
```

- This method reads a comma separated variable (csv) file
- Each line should have student name and year
- Creates a Student Object from each line of the file
- Returns a List of Student Objects with one entry for each valid line
- File name to read is passed as
 String parameter
 - Read each line of file, store in *line* String
 Split() on comma, make sure we got two parts (input could be invalid)

Roster.java

117

```
769
        public static List<Student> readRoster2(String fileName) throws IOException {
 77
            List<Student> roster = new ArrayList<Student>();
 78
            BufferedReader input;
 79
 80
            // Open the file, if possible
 81
            try {
 82
                 input = new BufferedReader(new FileReader(fileName));
 83
            }
 84
            catch (FileNotFoundException e) {
 85
                System.err.println("Cannot open file.\n" + e.getMessage());
 86
                return roster;
 87
 88
            // Read the file
 89
 90
            try {
 91
                // Line by line
 92
                 String line;
 93
                int lineNum = 0;
 94
                 while ((line = input.readLine()) != null) {
 95
                     System.out.println("read @"+lineNum+"`"+line+"'");
 96
                     // Comma separated
 97
                     String[] pieces = line.split(",");
                     if (pieces.length != 2) {
 98
 99
                         //did not get two elements in this line, output an error message
                         System.err.println("bad separation in line "+lineNum+":"+line);
100
                     }
101
102
                    else {
103
                         // got two elements for this line
104
                         try {
105
                             // Extract year as an integer, if possible
                             Student s = new Student(pieces[0], Integer.parseInt(pieces[1]));
106
                             System.out.println("=>"+s);
107
108
                             roster.add(s); //good student, add to roster
109
                         7
                         catch (NumberFormatException e) {
110
111
                             // couldn't parse second element as integer
                             System.err.println("bad number in line "+lineNum+":"+line);
112
113
                         }
114
                     }
115
                     lineNum++;
116
                }
```

- Got two elements after split()
- Try to parse as *name* as
 - String and year as Integer
- Add to roster if valid student
When reading files, we need to be ready to handle many different exceptions

Roster.java

```
769
        public static List<Student> readRoster2(String fileName) throws IOException {
 77
            List<Student> roster = new ArrayList<Student>();
 78
            BufferedReader input;
 79
 80
            // Open the file, if possible
 81
            try {
 82
                 input = new BufferedReader(new FileReader(fileName));
 83
            }
 84
            catch (FileNotFoundException e) {
 85
                System.err.println("Cannot open file.\n" + e.getMessage());
 86
                return roster;
 87
 88
 89
            // Read the file
 90
            try {
 91
                // Line by line
 92
                 String line;
 93
                int lineNum = 0;
                while ((line = input.readLine()) != null) {
 94
 95
                     System.out.println("read @"+lineNum+"`"+line+"'");
 96
                     // Comma separated
 97
                     String[] pieces = line.split(",");
                     if (pieces.length != 2) {
 98
 99
                         //did not get two elements in this line, output an error message
                         System.err.println("bad separation in line "+lineNum+":"+1/ine);
100
                     }
101
102
                    else {
103
                         // got two elements for this line
104
                         try {
105
                             // Extract year as an integer, if possible
106
                             Student s = new Student(pieces[0], Integer.parseInt(pieces[1]));
                             System.out.println("=>"+s);
107
108
                             roster.add(s); //good student, add to roster
109
                         7
110
                         catch (NumberFormatException e) {
111
                             // couldn't parse second element as integer
                             System.err.println("bad number in line "+lineNum+":"+line);
112
113
                         }
114
                     }
115
                     lineNum++;
116
                }
117
            }
```

- Got two elements after split()
- Try to parse as *name* as
 - String and year as Integer
- Add to roster if valid student

- If second element not Integer:
 - Catch error
 - Print error message
 - Keep reading

When reading files, we need to be ready to handle many different exceptions

Roster.java

```
769
        public static List<Student> readRoster2(String fileName) throws IOException {
 77
            List<Student> roster = new ArrayList<Student>();
 78
            BufferedReader input;
 79
 80
            // Open the file, if possible
 81
            try {
 82
                input = new BufferedReader(new FileReader(fileName));
 83
            }
 84
            catch (FileNotFoundException e) {
 85
                System.err.println("Cannot open file.\n" + e.getMessage());
 86
                return roster;
 87
 88
            // Read the file
 89
 90
            try {
 91
                // Line by line
 92
                String line;
 93
                int lineNum = 0;
                while ((line = input.readLine()) != null) {
 94
 95
                    System.out.println("read @"+lineNum+"`"+line+"'");
 96
                    // Comma separated
 97
                    String[] pieces = line.split(",");
 98
                    if (pieces.length != 2) {
 99
                        //did not get two elements in this line, output an error message
                        System.err.println("bad separation in line "+lineNum+":"+1/ine);
100
                    }
101
102
                    else {
103
                        // got two elements for this line
104
                        try {
105
                            // Extract year as an integer, if possible
106
                            Student s = new Student(pieces[0], Integer.parseInt(pieces[1]));
107
                            System.out.println("=>"+s);
108
                            roster.add(s); //good student, add to roster
109
                        7
110
                        catch (NumberFormatException e) {
111
                            // couldn't parse second element as integer
                            System.err.println("bad number in line "+lineNum+":"+line);
112
113
                        }
114
                    }
                                    Close file in finally block (not
115
                    lineNum++;
116
                }
                                     shown) – always runs
117
            }
```

- Got two elements after split()
- Try to parse as *name* as
 - String and year as Integer
- Add to roster if valid student

- If second element not Integer:
 - Catch error
 - Print error message
 - Keep reading