CS 10: Problem solving via Object Oriented Programming

String Finding



• Implement finding substrings

Agenda

1. Boyer-Moore algorithm

2. Tries

Matching/recognizing patterns in sequences is a common CS problem

Example: Find pattern in DNA data

AGGACGCCGCATTGACCATCTATGAGATGCTCCAGAACATCTTTGCTATTTTCAG ACAAGATTCATCTAGCACTGGCTGGAATGAGACTATTGTTGAGAACCTCCTGGCT AATGTCTATCATCAGATAAACCATCTGAAGACAGTCCTGGAAGAAAAACTGGAGA AAGAAGATTTCACCAGGGGAAAACTCATGAGCAGTCTGCACCTGAAAAGATATTA ATGACCAACAAGTGTCTCCTCCAAATTGCTCTCCTGTTGTGCTTCTCCACTACAG CTCTTTCCATGAGCTACAACTTGCTTGGATTCCTACAAAGAAGCAGCAACTTTCA GTGTCAGAAGCTCCTGTGGCAATTGAATGGGAGGCTTGAATACTGCCTCAAGCAC AGGATGAACTTTGACATCCCTGAGGAGATTAAGCAGCTGCAGCAGTTCCAGAAGG ATGACCAACAAGTGTCTCCTCCAAATTGCTCTCCTGTTGTGCTTCTCCACTACAG CTCTTTCCATGAGCTACAACTTGCTTGGATTCCTACAAAGAAGCAGCAACTTTCA GTGTCAGAAGCTCCTGTGGCAATTGAATGGGAGGCTTGAATACTGCCTCAAGCAC AGGATGAACTTTGACATCCCTGAGGAGATTAAGCAGCTGCAGCAGTTCCAGAAGG AGGACGCCGCATTGACCATCTATGAGATGCTCCAGAACATCTTTGCTATTTCAG ACAAGATTCATCTAGCACTGGCTGGAATGAGACTATTGTTGAGAACCTCCTGGCT AATGTCTATCATCAGATAAACCATCTGAAGACAGTCCTGGAAGAAAAACTGGAGA AAGAAGATTTCACCAGGGGAAAACTCATGAGCAGTCTGCACCTGAAAAGATATTA TGGGAGGATTCTGCATTACCTGAAGGCCAAGGAGTACAGTCACTGTGCCTGGACC ATAGTCAGAGTGGAAATCCTAAGGAACTTTTACTTCATTAACAGACTTACAGGTT AGGACGCCGCATTGACCATCTATGAGATGCTCCAGAACATCTTTGCTATTTCAG ACAAGATTCATCTAGCACTGGCTGGAATGAGACTATTGTTGAGAACCTCCTGGCT AATGTCTATCATCAGATAAACCATCTGAAGACAGTCCTGGAAGAAAAACTGGAGA AAGAAGATTTCACCAGGGGAAAACTCATGAGCAGTCTGCACCTGAAAAGATATTA TGGGAGGATTCTGCATTACCTGAAGGCCAAGGAGTACAGTCACTGTGCCTGGACC ATAGTCAGAGTGGAAATCCTAAGGAACTTTTACTTCATTAACAGACTTACAGGTT

Task Find a substring in this large string

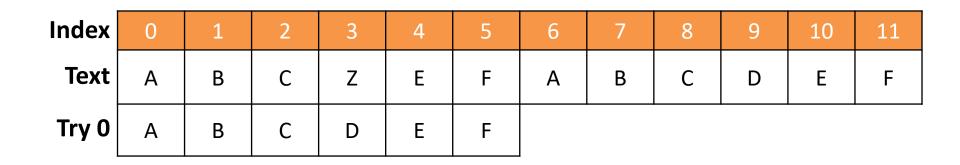
Query string of length *m*



Generally assume *m* << *n* (but doesn't have to be)

A brute force approach starts at index 0 and works forward

Find query of length m, in text of length n



- Start query string and text at index 0
- Loop over length of query string
- Look for match
- Move query string right one space if find mismatch

Compare each character in text and query string, move right if match

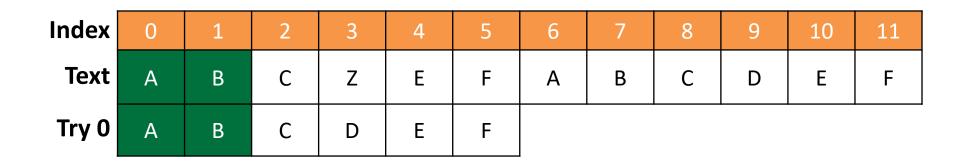
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Find query of length m, in text of length n



- Start query string and text at index 0
- Loop over length of query string
- Look for match
- Move query string right one space if find mismatch

If find characters that do not match, move query right one space in text and try again

Find query of length m, in text of length n

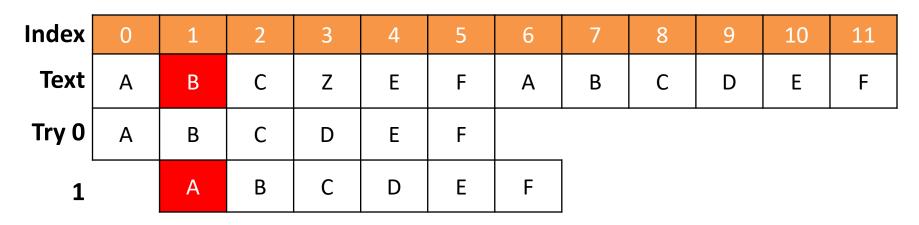


Mismatch, slide query one space right and try again

- Start query string and text at index 0
- Loop over length of query string
- Look for match
- Move query string right one space if find mismatch

Another mismatch, move query right one space again

Find query of length m, in text of length n

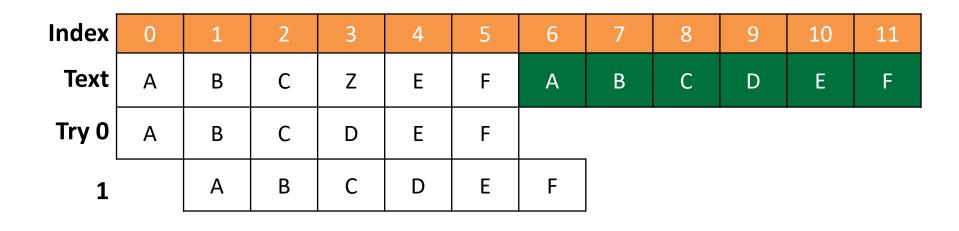


Mismatch, slide query one space right and try again (and again...)

- Start query string and text at index 0
- Loop over length of query string
- Look for match
- Move query string right one space if find mismatch

Continue until hit end of text less length of query string or find match

Find query of length m, in text of length n



n-m

...



Match found after n-m+1 checks Each check of length m Run time complexity O(nm)

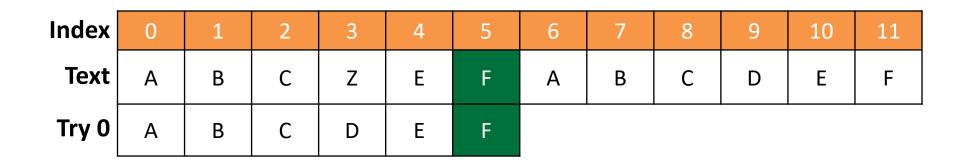
A brute force approach is inefficient, O(nm)

BoyerMoore.java

```
17⊖
       public static int findBruteForce(char[] text, char[] pattern) {
           System.out.println("Brute force looking for " + String.valueOf(pattern) + " in " + String.valueOf(text));
18
19
           int n = text.length;
           int m = pattern.length;
20
21
22
           // Test for empty string
23
           if (m == 0) return 0;
24
25
           //brute force it -- loop over all characters in text O(n)
           for (int i=0;i<=n-m;i++) { //index into the text</pre>
26
27
                //loop over all characters in pattern while characters match O(m)
28
               int k = 0; //index into the pattern
                while (k<m && text[i+k] == pattern[k]) {</pre>
29
30
                    k++;
                3
31
32
               //if at end of pattern, then found match starting at index i in text
33
               if (k==m) {
34
                    System.out.println("\tFound match at index " + i);
35
                    return i:
                }
36
37
           3
38
           //match not found
39
           System.out.println("\tNo match found");
40
            return -1;
41
       }
42
```

Boyer-Moore algorithm is more efficient and works backwards

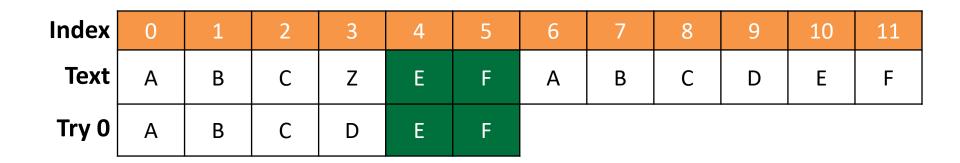
Find query of length m(=6), in text of length n(=12)



- Start at index i=m-1
- Loop backward over query string, starting at k=m-1
- If match decrement both i and k
- If mismatch:
 - If text not in query string, move query past current index updating i=i+m and resetting k
 - If text in query string, move query to last occurrence of text

Boyer-Moore algorithm is more efficient and works backwards

Find query of length m, in text of length n



- Start at index i=m-1
- Loop backward over query string, starting at k=m-1
- If match decrement both i and k
- If mismatch:
 - If text not in query string, move query past current index, updating i=i+m and resetting k
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Boyer-Moore algorithm is more efficient and works backwards

Find query of length m, in text of length n



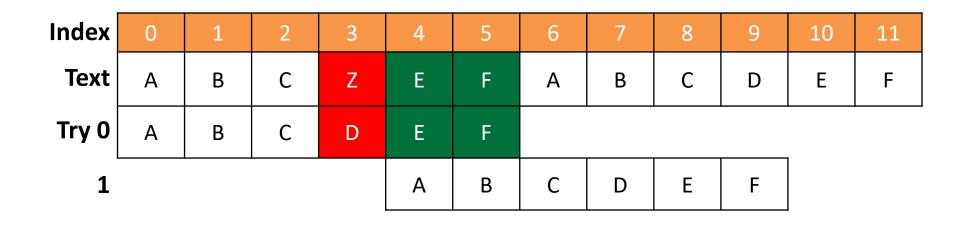
- Z not in query, so any matches prior to Z must all fail
- No need to check those
- Move query string one space past character not in query string (Z here)
 - Avoids checks at indices 0-2
- Loop backward over query string, starting at k=m-1
- If match decrement both i and k

Start at index i=m-1

• If mismatch:

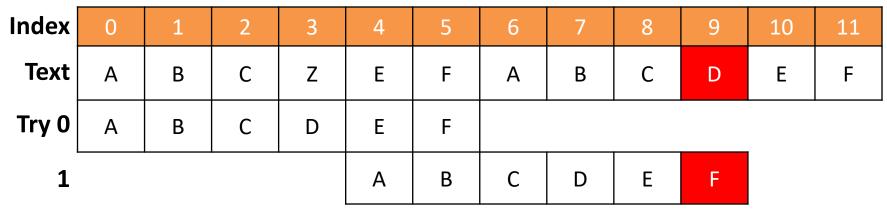
- If text not in query string, move query past current index, updating i=i+m and resetting k
- If text in query string, move query to last occurrence of text

Find query of length m, in text of length n



- Start at index i=m-1
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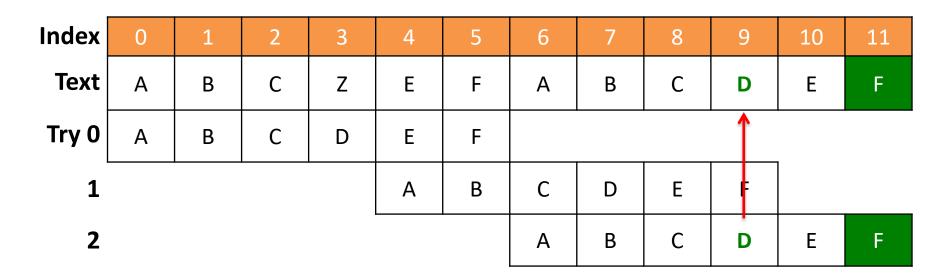
Find query of length m, in text of length n



Mismatch, but D in query string so move the last occurrence of D in query to this index

- Start at index i=m-1
- Loop backward over query string, starting at k=m-1
- If match decrement both i and k
- If mismatch:
 - If text not in query string, move query past current index, updating i=i+m and resetting k
 - If text in query string, move query to last occurrence of text

Find query of length m, in text of length n



Boyer-Moore

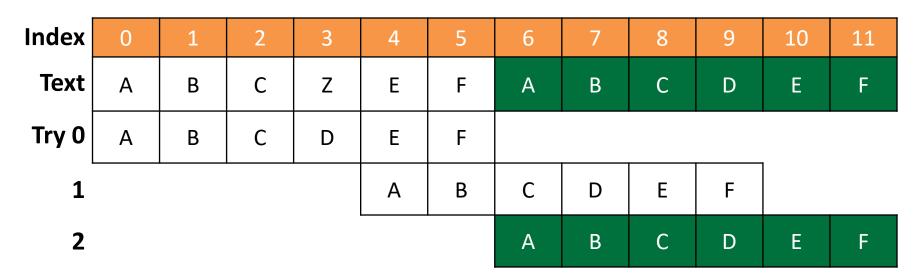
• Start at index i=m-1

If had moved to <u>first</u> occurrence of text in query string, might

to move to <u>last</u> occurrence

- Loop backward over query string, starting at k=m-1cause a move too far right, have
- If match decrement both i and k
- If mismatch:
 - If text not in query string, move query past current index, updating i=i+m and resetting k
 - If text in query string, move query to last occurrence of text

Find query of length m, in text of length n



Boyer-Moore

- Start at index i=m-1
- Loop backward over query string, starting at k=m-1
- If match decrement both i and k
- If mismatch:
 - If text not in query string, move query past current index, updating i=i+m and resetting k
 - If text in query string, move query to last occurrence of text

Match found

3 checks vs. 7 for brute force Not greatly different for small strings, but very different for large strings!

Boyer-Moore can be O(n)

- Our version is simplified version of original Boyer-Moore
- Full Boyer-Moore algorithm is O(m+n), but since normally n >> m, O(n) on "reasonable" text (e.g., not long strings of same character)
- Does require pre-processing step to store last index of each character in query. Easy way:
 - Loop over each character in query string
 - Store characters in Map with current index as value
 - At end, Map will have the last index for each character

Boyer-Moore algorithm

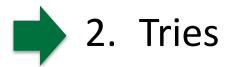
BoyerMoore.java

```
49⊝
       public static int findBoyerMoore(char[] text, char[] pattern) {
         System.out.println("Boyer-Moore looking for " + String.valueOf(pattern) + " in " + String.valueOf(text));
50
51
         int n = text.length;
52
         int m = pattern.length;
53
54
         // Test for empty string
55
         if (m == 0) return 0;
56
57
         // Initialization, create Map of last position of each character = O(n)
58
         Map<Character, Integer> last = new HashMap<>();
59
         for (int i = 0; i < n; i++) {
             last.put(text[i], -1); // set all chars, by default, to -1
60
61
         3
62
         for (int i = 0; i < m; i++) {</pre>
63
             last.put(pattern[i], i); // update last seen positions
64
         3
65
66
         // Start with the end of the pattern aligned at index m-1 in the text.
67
         int i = m - 1; // index into the text
68
         int k = m - 1; // index into the pattern
69
         while (i < n) {
70
             if (text[i] == pattern[k]) { // match! return i if complete match; otherwise, keep checking.
71
                 if (k == 0) {
72
                     System.out.println("\tFound match at index " + i);
73
                      return i; // done!
74
                 }
75
                 i--; k--;
76
             3
77
             else { // jump step + restart at end of pattern
78
                 i += m - Math.min(k, 1 + last.get(text[i])); //move in text
79
                 k = m - 1; //move to end of pattern
             }
80
81
82
         System.out.println("\tNo match found");
83
         return -1; // not found
84
     }
```

54



1. Boyer-Moore algorithm



How would you implement autocomplete?

- Consider autocomplete text boxes
- A user starts typing, autocomplete shows possible words user might want given only a couple of characters
- How would you implement that?
- One way is with a Trie (pronounced "try" to differentiate from Tree, comes from "re<u>trie</u>ve")

Google

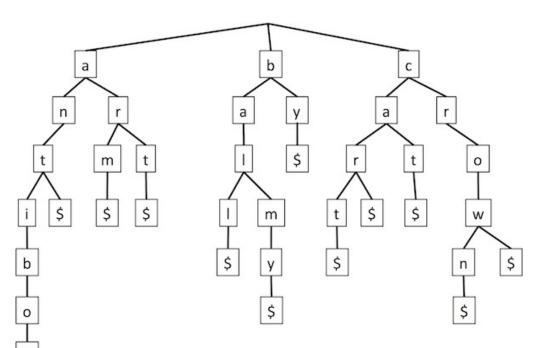
compu

computer computers for change computer desk computershare computer repair computer science compulsory computer barn computer monitor computer games

Typed in "compu" into Google, Google guesses what I want

Tries can find all substrings in text that <u>begin</u> with a prefix string

Alphabet of d characters, and string length n

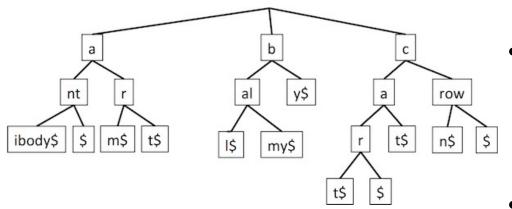


Height is length of longest string
Can be used to implement Set or
Map, not just autocomplete

- Trie is a multi-way tree where each node is a letter
- Store set of words S in Trie with one node per letter and one leaf for each word
- To match prefix, start at root and follow children until find stop character (\$)
- Example: type "ca" and find cart, car, and cat
- To find string of length *m*, must go down m levels
- If alphabet has d = |Σ| characters, then O(dm) to find or insert

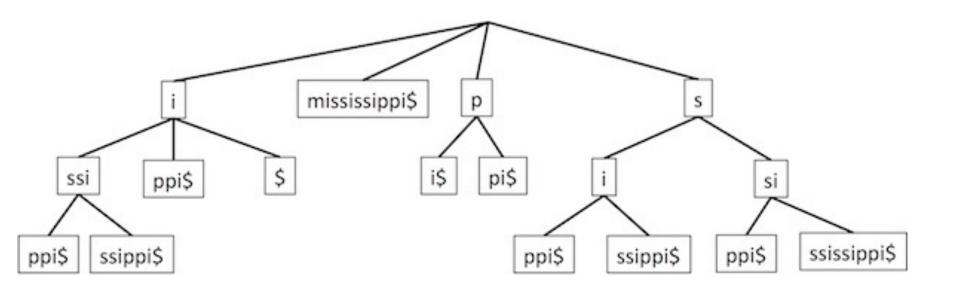
Compressed tries save memory

Alphabet of d characters, and string length n



- Compressed trie stores substrings if no branches (e.g., no branches after "ant" so put "ibody" in one node, not five)
- Number of nodes reduced from O(|n|) – total length of strings in set of words S, to O(|s|) – number of words in S
- Saves memory, book shows how to store indices
- Can be used for sorting
 - Add all words into trie
 - Do a pre-order traversal

Tries works on prefixes, we can also work on suffixes with a Suffix trie



Suffix tries

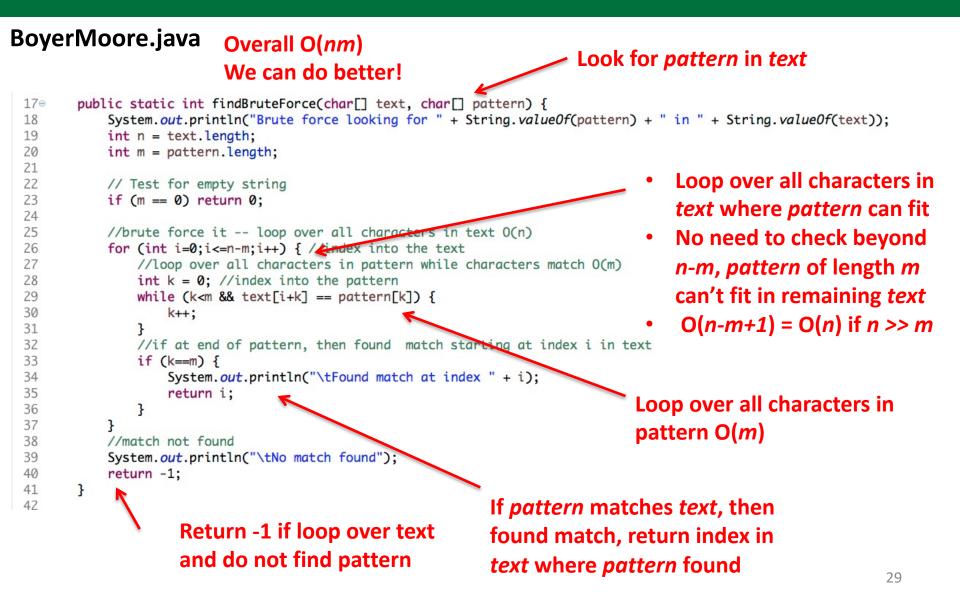
- Store data by suffixes (end of words)
- Add node for each substring X[j..n-1], for j=0,1,..n-1
- Use compressed trie (algorithm complicated, stores in O(n) time)
- Search for suffixes; start at root and work downward
- See course web page for more details

Additional Resources

Brute force and Boyer Moore

ANNOTATED SLIDES

A brute force approach is inefficient, O(nm)



Boyer-Moore algorithm

BoyerMoore.java

Look for *pattern* in *text*

```
public static int findBoyerMoore(char[] text, char[] pattern) {
49⊝
        System.out.println("Boyer-Moore looking for " + String.valueOf(pattern) + " in " + String.valueOf(text));
50
51
        int n = text.length;
52
        int m = pattern.length;
53
                                                                                Preprocess: create Map last
54
        // Test for empty string
55
        if (m == 0) return 0:
                                                                                and set all distinct characters
56
57
        // Initialization, create Map of last position of each character = 0(r
                                                                                in text to -1
58
        Map<Character. Integer> last = new HashMap<>();
59
        for (int i = 0; i < n; i++) {
60
            last.put(text[i], -1); // set all chars, by default, to -1
61
        3
                                                                                Update to hold last occurrence
62
        for (int i = 0; i < m; i++) {</pre>
63
            last.put(pattern[i], i); // update last seen positions
                                                                                of character in pattern
64
        3
65
66
        // Start with the end of the pattern aligned at index m-1 in the text.
67
        int i = m - 1; // index into the text
68
        int k = m - 1; // index into the pattern
                                                                       Loop backward over pattern
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        while (i < n) {
            if (text[i] == pattern[k]) // match! return i if complete match; otherwise, keep checking.
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                if (k == 0) {
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                   System.out.println("\tFound match at index " + i);
                                                                    Return index in text if
73
                   return i; // done!
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                }
                                                                    pattern found
75
                i--; k--;
76
            3
77
            else { // jump step + restart at end of pattern
78
               i += m - Math.min(k, 1 + last.get(text[i])); //move in text
79
                k = m - 1; //move to end of pattern
80
            3
                                                                 Jump past character not in pattern (i += m-0)
81
82
                                                                  or move by min of index into query (k) and
        System.out.println("\tNo match found");
83
        return -1: // not found
84
    }
                                                                  last position of text character in pattern<sub>30</sub>
                    Return -1 if not found
```