

CS 10:


Problem solving via Object Oriented  
Programming

**Abstraction**

# Main goals

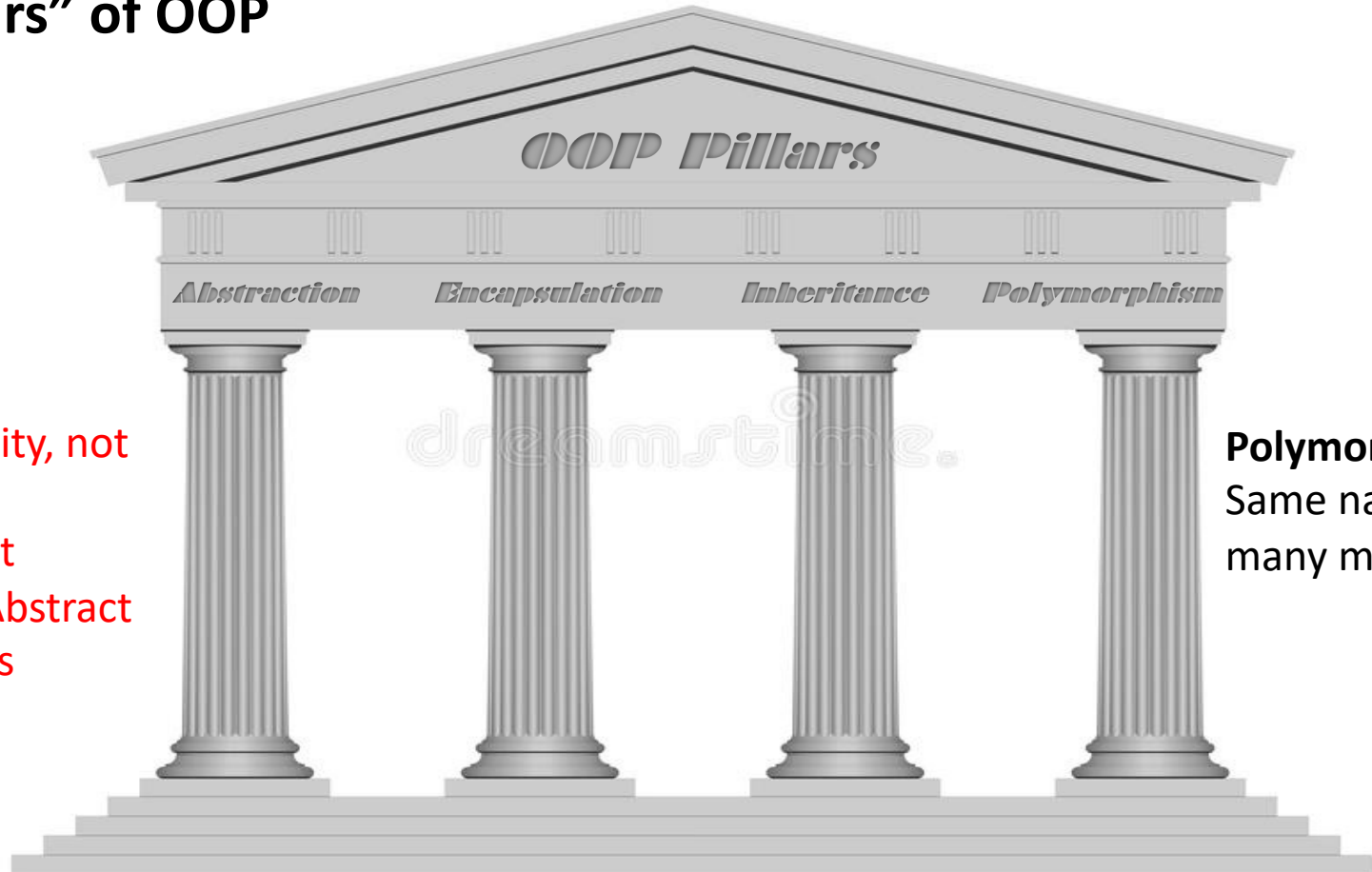
- Define Abstract Data Types (ADTs)
- Characterize runtime complexity

# Agenda

- 
1. ADTs
  2. Generics
  3. Java provided List implementation
  4. Run-time complexity
  5. Asymptotic notation

# OOP relies on four main pillars to create robust, adaptable, and reusable code

## Four “pillars” of OOP



### Abstraction

- Name functionality, not how to implement
- Leads to Abstract Data Types (ADTs)

**Polymorphism**  
Same name,  
many meanings

### Encapsulation

- Bind code and data into one thing called an object
- Code called methods in OOP (not functions)

### Inheritance

- Create specialty versions that “inherit” functionality of parent
- Reduces code

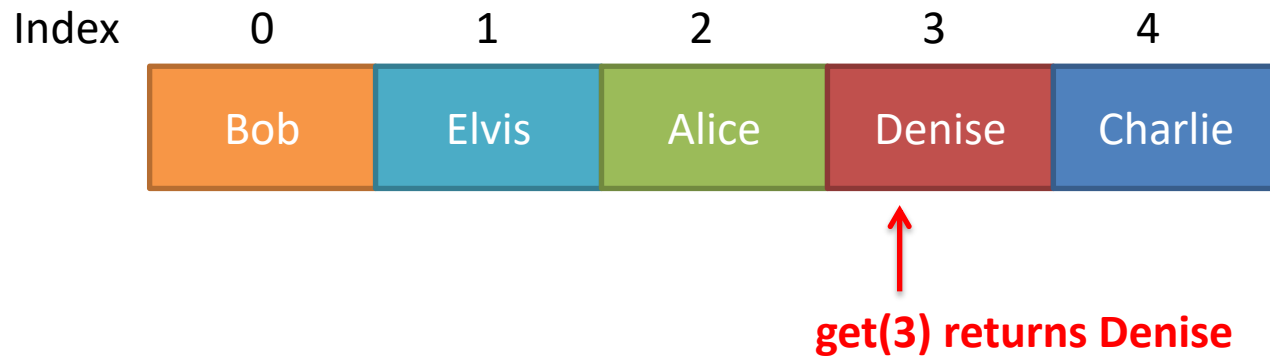
# Example: List

List holds multiple elements (items) referenced by position in List



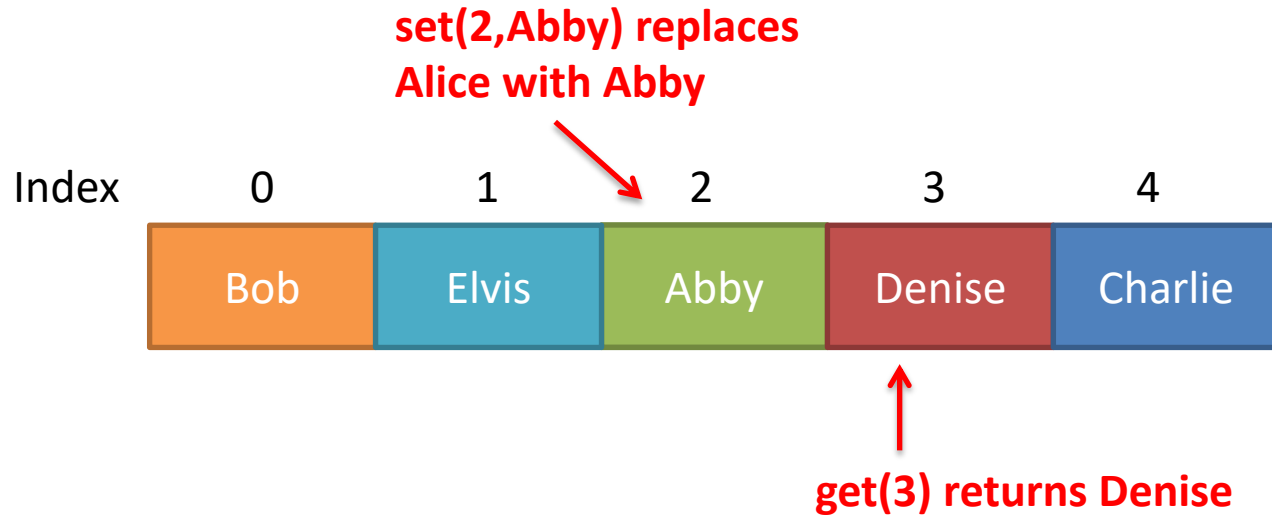
# Example: List ADT

List holds multiple elements (items) referenced by position in List



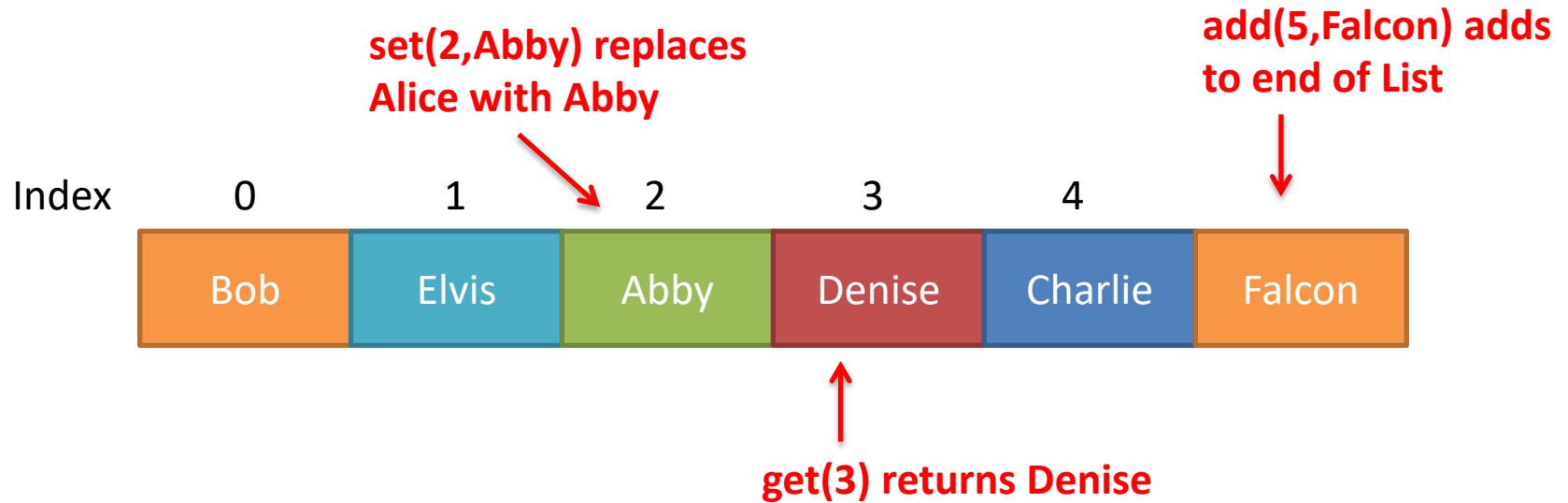
# Example: List ADT

List holds multiple elements (items) referenced by position in List



# Example: List ADT

List holds multiple elements (items) referenced by position in List



How many ways to implement a list?



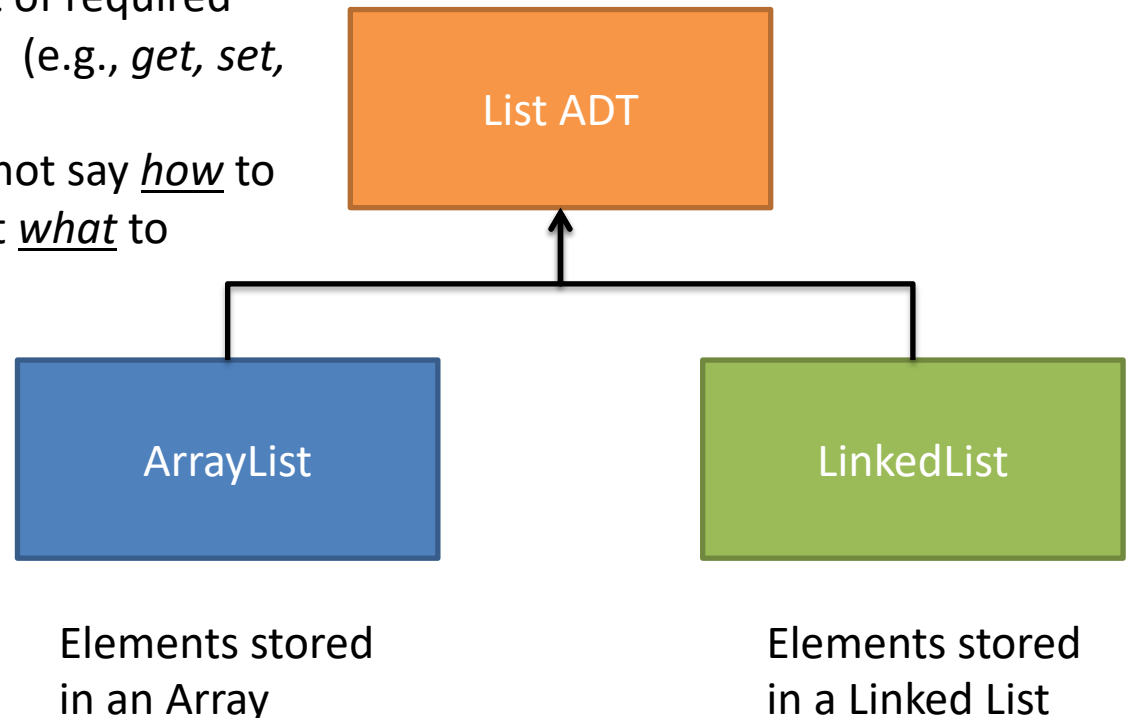
# ADTs can be implemented differently, but must provide common functionality

## Java Interface:

- ADT defines set of required ADT operations (e.g., *get*, *set*, *add*, *remove*,...)
- Interface does not say *how* to implement, just *what* to implement

## Implementation:

- Code to implement operations that are defined by interface
- Can be written using different data structures
- MUST implement all functionality defined by interface
- But you can include other functionality



Java has both ArrayList and LinkedList implementations of List  
**We will write our own**

# The List ADT defines required operations, but not how to implement them

## List ADT

### Operation

`size()`

`isEmpty()`

`get(i)`

`set(i, e)`

`add(i, e)`

`remove(i)`

### Description

Return number of items in List

True if no items in List, otherwise false

Return the item at index *i*

Replace the item at index *i* with item *e*

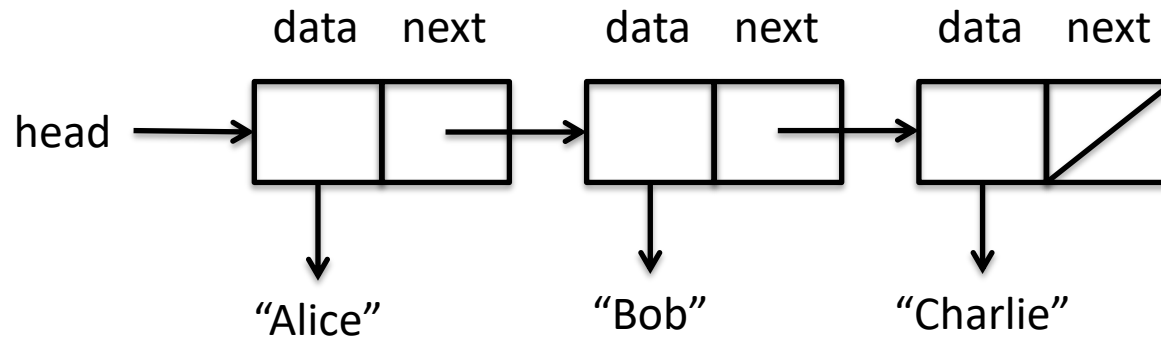
Insert item *e* at index *i*, moving all subsequent items one index larger

Remove and return item at index *i*, move all subsequent items one index smaller

# The List ADT could be implemented with a singly linked list OR an array; either works

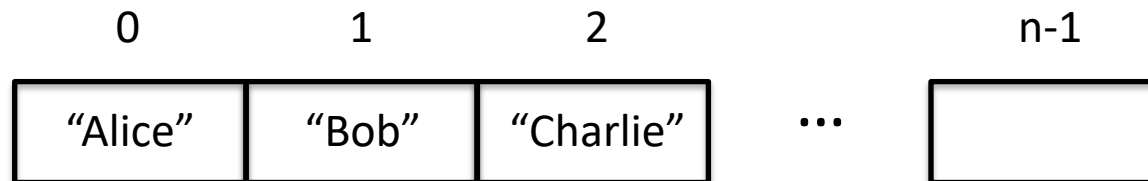
## Examples of List implementation

### Singly linked list



- Each implementation has pros and cons
- We are creating our own versions to get familiar with how they work

### Array



# Why not just classes?

- Inheritance
  - Multiple inheritance forbidden because of ambiguity
- Interface
  - Can implement multiple interfaces
  - No ambiguity

# Interfaces go in one file, implementations go in another file(s)



## Interface file

Specifies required operations

`SimpleList.java`

Uses keyword `interface`



## Linked list implementation

`SinglyLinked.java`

**OR**



## Array implementation

**Implementation file**  
Actually implements required operations using a specific data structure

Use keyword `implements` to implement an interface

# SimpleList.java is an interface that specifies what operations MUST be implemented

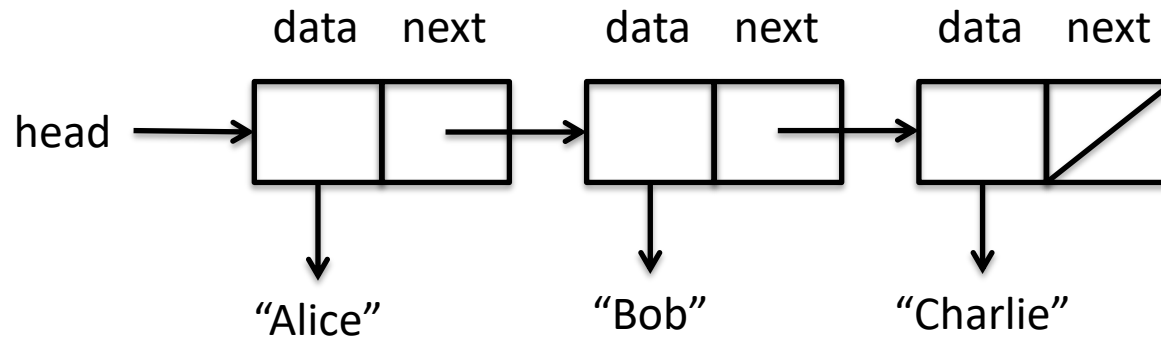
## SimpleList.java

```
public interface SimpleList<T> extends Iterable<T> {  
    /**  
     * Returns # elements in the List (they are indexed 0..size-1)  
     */  
    public int size();  
  
    /**  
     * Returns true if there are no elements in the List, false otherwise  
     * @return true or false  
     */  
    public boolean isEmpty();  
  
    /**  
     * Adds the item at the index, which must be between 0 and size  
     */  
    public void add(int idx, T item) throws Exception;  
  
    /**  
     * Add item at end of List  
     */  
    public void add(T item) throws Exception;  
  
    /**  
     * Removes and returns the item at the index, which must be between 0 and size-1  
     */  
    public T remove(int idx) throws Exception;  
  
    /**  
     * Returns the item at the index, which must be between 0 and size-1  
     */  
    public T get(int idx) throws Exception;  
  
    /**  
     * Replaces the item at the index, which must be between 0 and size-1  
     */  
    public void set(int idx, T item) throws Exception;
```

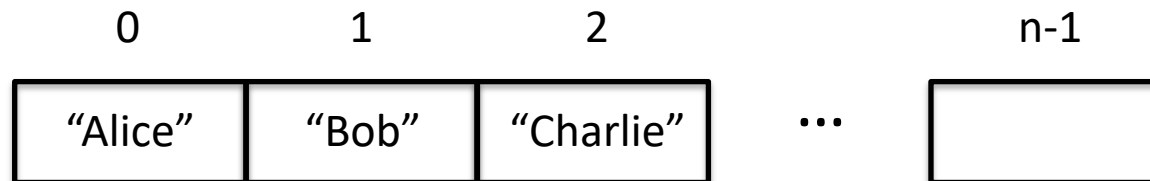
# The List ADT could be implemented with a singly linked list OR an array; either works

## Examples of List implementation

### Singly linked list



### Array



# Agenda

1. ADTs

 2. Generics

3. Java provided List implementation

4. Run-time complexity


5. Asymptotic notation



# Generics allow a variable to stand in for a Java type

```
public interface SimpleList<T> {  
    public T get(int idx) throws Exception;  
    public void add(int idx, T item) throws Exception;
```

# Agenda

1. ADTs
2. Generics
-  3. Java provided List implementation
4. Run-time complexity
5. Asymptotic notation

# ArrayListDemo.java: ArrayLists can hold multiple objects; provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```



**ArrayList list**

1

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```



**ArrayList list**

1	2
---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```



**ArrayList list**



# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```



**ArrayList list**

1	3	2
---	---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```



**Output**  
[1, 3, 2]

**ArrayList list**

1	3	2
---	---	---



# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```



**Output**  
[1, 3, 2]

**ArrayList list**

1	3	2
---	---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

## Output

[1, 3, 2]

3

## ArrayList list

1	3	2
---	---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

## Output

[1, 3, 2]

3

## ArrayList list

1	3	2
---	---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

## Output

[1, 3, 2]

3

[1, 2]

## ArrayList list

1	2
---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

## Output

[1, 3, 2]

3

[1, 2]

## ArrayList list

1	2
---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

## Output

[1, 3, 2]

3

[1, 2]

## ArrayList list

1	4
---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

## Output

[1, 3, 2]

3

[1, 2]

[1, 4]

## ArrayList list

1	4
---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

• **Where is the last item stored?**

## Output

[1, 3, 2]

3

[1, 2]

[1, 4]

2

## ArrayList list

1	4
---	---



# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

- **Where is the last item stored?**
- ***size()-1* due to zero-based indexing**

## Output

[1, 3, 2]

3

[1, 2]

[1, 4]

2

## ArrayList list

1	4
---	---

# Lists can hold any kind of object, not just autoboxed versions of primitive data types

```
public class StudentTrackerAppList {  
    public static void main(String[] args) {  
        List<Student> students = new ArrayList<Student>();  
        students.add(new Student("Alice", "f00xyz"));  
        students.add(new GraduateStudent("Bob", "f00123"));  
        students.add(new InternationalStudent("Charlie", "f00abc"));  
    }  
}
```

# Lists do not declare a maximum size unlike arrays

```
public class StudentTrackerAppList {  
    public static void main(String[] args) {  
        List<Student> students = new ArrayList<Student>();  
        students.add(new Student("Alice", "f00xyz"));  
        students.add(new GraduateStudent("Bob", "f00123"));  
        students.add(new InternationalStudent("Charlie", "f00abc"));  
    }  
}
```

```
public class StudentTrackerApp {  
    public static void main(String[] args) {  
        int numberOfStudents = 3;  
        Student[] students = new Student[numberOfStudents];  
        students[0] = new Student("Alice", "f00xyz");  
        students[1] = new GraduateStudent("Bob", "f00123");  
        students[2] = new InternationalStudent("Charlie", "f00abc");  
    }  
}
```

# For-each loops are available for Lists, like they are with arrays

```
public class StudentTrackerAppList {
    public static void main(String[] args) {
        List<Student> students = new ArrayList<Student>();
        students.add(new Student("Alice", "f00xyz"));
        students.add(new GraduateStudent("Bob", "f00123"));
        students.add(new InternationalStudent("Charlie", "f00abc"));

        //print students using for-each loop
        System.out.println("Before studying");
        for (Student student : students) {
            System.out.println(student);
        }
    }
}
```

```
public class StudentTrackerApp {
    public static void main(String[] args) {
        int numberOfStudents = 3;
        Student[] students = new Student[numberOfStudents];
        students[0] = new Student("Alice", "f00xyz");
        students[1] = new GraduateStudent("Bob", "f00123");
        students[2] = new InternationalStudent("Charlie", "f00abc"));

        //print students using for-each loop
        System.out.println("Before studying");
        for (Student student : students) {
            System.out.println(student);
        }
    }
}
```

# Use *size* to get the number of items in a List

```
public class StudentTrackerAppList {  
    public static void main(String[] args) {  
        List<Student> students = new ArrayList<Student>();  
        students.add(new Student("Alice", "f00xyz"));  
        students.add(new GraduateStudent("Bob", "f00123"));  
        students.add(new InternationalStudent("Charlie", "f00abc"));
```

```
//print students using for-each loop  
System.out.println("Before studying");  
for (Student student : students) {  
    System.out.println(student);  
}
```

```
//randomly select students to study to simulate an actual application  
for (int i = 0; i < 10; i++) {  
    //pick random student  
    int index = (int) (Math.random() * students.size());  
  
    //add random studying time between 0 and 5 hours  
    double time = Math.random() * 5;  
    students.get(index).study(time);  
}
```

```
public class StudentTrackerApp {  
    public static void main(String[] args) {  
        int numberOfStudents = 3;  
        Student[] students = new Student[numberOfStudents];  
        students[0] = new Student("Alice", "f00xyz");  
        students[1] = new GraduateStudent("Bob", "f00123");  
        students[2] = new InternationalStudent("Charlie", "f00abc");
```

```
//print students using for-each loop  
System.out.println("Before studying");  
for (Student student : students) {  
    System.out.println(student);  
}
```

```
//randomly select students to study to simulate an actual application  
for (int i = 0; i < 10; i++) {  
    //pick random student  
    int index = (int)(Math.random() * numberOfStudents);  
  
    //add random studying time between 0 and 5 hours  
    double time = Math.random() * 5;  
    students[index].study(time);  
}
```

# Use *get* to retrieve an item at a given index

```
public class StudentTrackerAppList {  
    public static void main(String[] args) {  
        List<Student> students = new ArrayList<Student>();  
        students.add(new Student("Alice", "f00xyz"));  
        students.add(new GraduateStudent("Bob", "f00123"));  
        students.add(new InternationalStudent("Charlie", "f00abc"));
```

```
        //print students using for-each loop  
        System.out.println("Before studying");  
        for (Student student : students) {  
            System.out.println(student);  
        }
```

```
        //randomly select students to study to simulate an actual application  
        for (int i = 0; i < 10; i++) {  
            //pick random student  
            int index = (int) (Math.random() * students.size());
```

```
            //add random studying time between 0 and 5 hours  
            double time = Math.random() * 5;  
            students.get(index).study(time);  
        }
```

```
public class StudentTrackerApp {  
    public static void main(String[] args) {  
        int numberOfStudents = 3;  
        Student[] students = new Student[numberOfStudents];  
        students[0] = new Student("Alice", "f00xyz");  
        students[1] = new GraduateStudent("Bob", "f00123");  
        students[2] = new InternationalStudent("Charlie", "f00abc");
```

```
        //print students using for-each loop  
        System.out.println("Before studying");  
        for (Student student : students) {  
            System.out.println(student);  
        }
```

```
        //randomly select students to study to simulate an actual application  
        for (int i = 0; i < 10; i++) {  
            //pick random student  
            int index = (int)(Math.random() * numberOfStudents);
```

```
            //add random studying time between 0 and 5 hours  
            double time = Math.random() * 5;  
            students[index].study(time);  
        }
```

# C-style for loops are also available, use *get* with them

```
public class StudentTrackerAppList {  
    public static void main(String[] args) {  
        List<Student> students = new ArrayList<Student>();  
        students.add(new Student("Alice", "f00xyz"));  
        students.add(new GraduateStudent("Bob", "f00123"));  
        students.add(new InternationalStudent("Charlie", "f00abc"));
```

```
        //print students using for-each loop  
        System.out.println("Before studying");  
        for (Student student : students) {  
            System.out.println(student);  
        }
```

```
        //randomly select students to study to simulate an actual application  
        for (int i = 0; i < 10; i++) {  
            //pick random student  
            int index = (int) (Math.random() * students.size());
```

```
            //add random studying time between 0 and 5 hours  
            double time = Math.random() * 5;  
            students.get(index).study(time);  
        }
```

```
        //print students using C-style for loop  
        System.out.println("After studying");  
        for (int i = 0; i < students.size(); i++) {  
            System.out.println(students.get(i));  
        }
```

```
public class StudentTrackerApp {  
    public static void main(String[] args) {  
        int numberOfStudents = 3;  
        Student[] students = new Student[numberOfStudents];  
        students[0] = new Student("Alice", "f00xyz");  
        students[1] = new GraduateStudent("Bob", "f00123");  
        students[2] = new InternationalStudent("Charlie", "f00abc");
```

```
        //print students using for-each loop  
        System.out.println("Before studying");  
        for (Student student : students) {  
            System.out.println(student);  
        }
```

```
        //randomly select students to study to simulate an actual application  
        for (int i = 0; i < 10; i++) {  
            //pick random student  
            int index = (int)(Math.random() * numberOfStudents);
```

```
            //add random studying time between 0 and 5 hours  
            double time = Math.random() * 5;  
            students[index].study(time);  
        }
```

```
        //print students using C-style for loop  
        System.out.println("After studying");  
        for (int i = 0; i < students.size(); i++) {  
            System.out.println(students[i]);  
        }
```

# C-style for loops are also available, use *get* with them

```
public class StudentTrackerAppList {
    public static void main(String[] args) {
        List<Student> students = new ArrayList<Student>();
        students.add(new Student("Alice", "f00xyz"));
        students.add(new GraduateStudent("Bob", "f00123"));
        students.add(new InternationalStudent("Charlie", "f00abc"));

        //print students using for-each loop
        System.out.println("Before studying");
        for (Student student : students) {
            System.out.println(student);
        }

        //randomly select students to study to simulate an actual application
        for (int i = 0; i < 10; i++) {
            //pick random student
            int index = (int) (Math.random() * students.size());

            //add random studying time between 0 and 5 hours
            double time = Math.random() * 5;
            students.get(index).study(time);
        }


        //print students using C-style for loop
        System.out.println("After studying");
        for (int i = 0; i < students.size(); i++) {
            System.out.println(students.get(i));
        }
    }
}
```

## Output

```
Before studying
Name: Alice (f00xyz)
    Graduation year: null
    Hours studying: 0.0
    Hours in class: 0.0
Name: Bob (f00123)
    Graduation year: null
    Hours studying: 0.0
    Hours in class: 0.0
    Hours in the lab: 0.0
    Department: null
    Advisor: null
Name: Charlie (f00abc)
    Graduation year: null
    Hours studying: 0.0
    Hours in class: 0.0
    Home country: null
Hi Mom! It's Bob. I'm studying!
Hi Mom! It's Alice. I'm studying!
Hi Mom! It's Bob. I'm studying!
Hi Mom! It's Bob. I'm studying!
Hi Mom! It's Charlie. I'm studying!
Hi Mom! It's Bob. I'm studying!
Hi Mom! It's Alice. I'm studying!
Hi Mom! It's Alice. I'm studying!
Hi Mom! It's Bob. I'm studying!
Hi Mom! It's Alice. I'm studying!
After studying
Name: Alice (f00xyz)
    Graduation year: null
    Hours studying: 6.590768116487223
    Hours in class: 0.0
<snip>
```



# Agenda

1. ADTs
2. Generics
3. Java provided List implementation
-  4. Run-time complexity
5. Asymptotic notation

# How long does it take to find an item in a List?



Assume there are  $n$  items in the List (index 0 ...  $n-1$ )

Find index of “Paula” in List

What pseudo code would you use:

for  $i = 0 \dots n-1$

    get item at index  $i$

    if item is equal to search value

        return index  $i$

    return -1 (or otherwise indicate search term not in List)

How long to find the item?

Operations to count

- Assign value to variable
- Following an object reference to heap memory
- Performing arithmetic operation (e.g., add two numbers)
- Compare two numbers (if statement)
- Access element in array
- Calling or returning from a method

# Often run-time will depend on the number of elements an algorithm must process

**Constant time – does not depend on number of items**

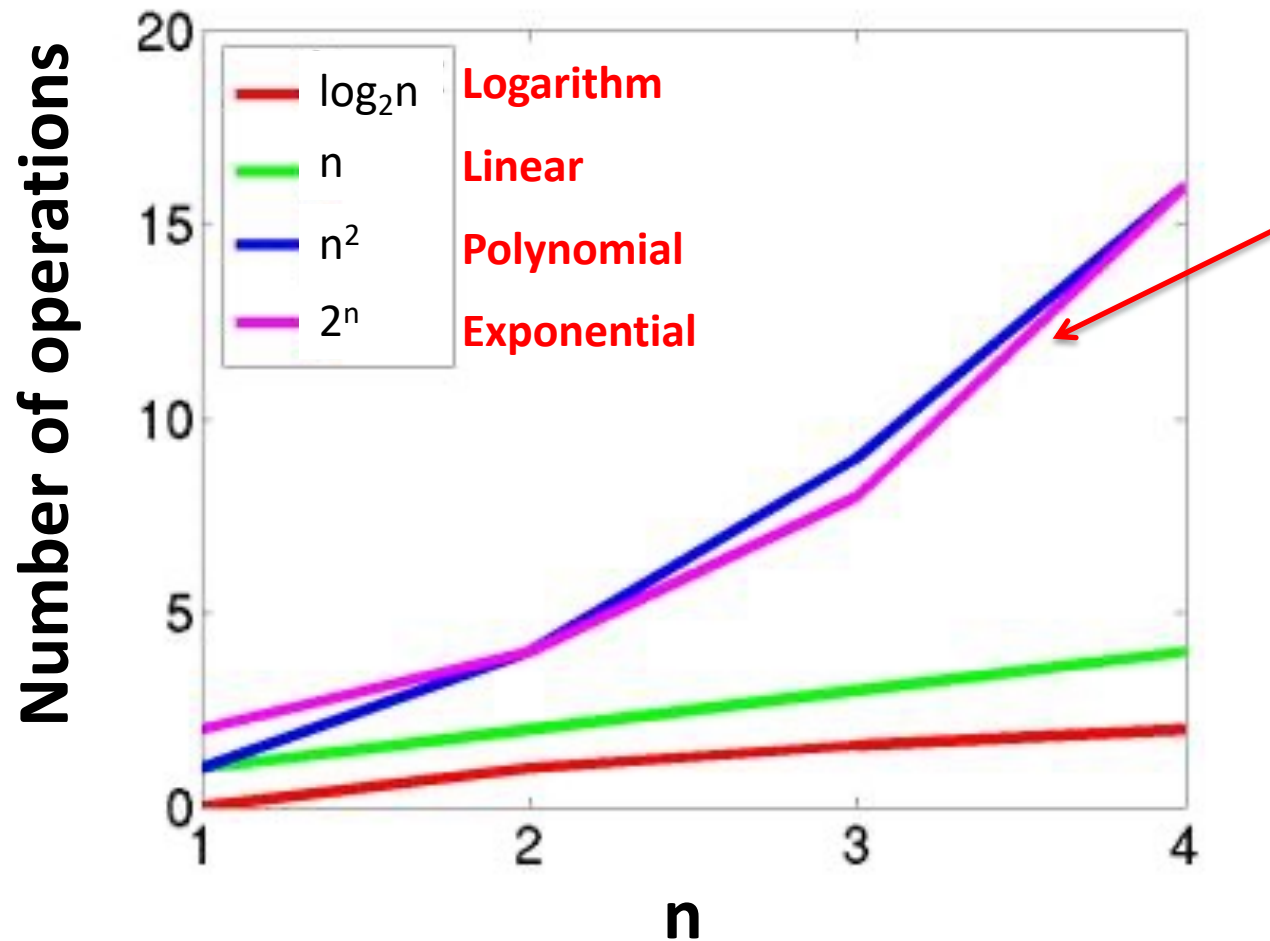
**Linear time – directly depends on number of items**

**Polynomial time – depends on a polynomial function of number of items**

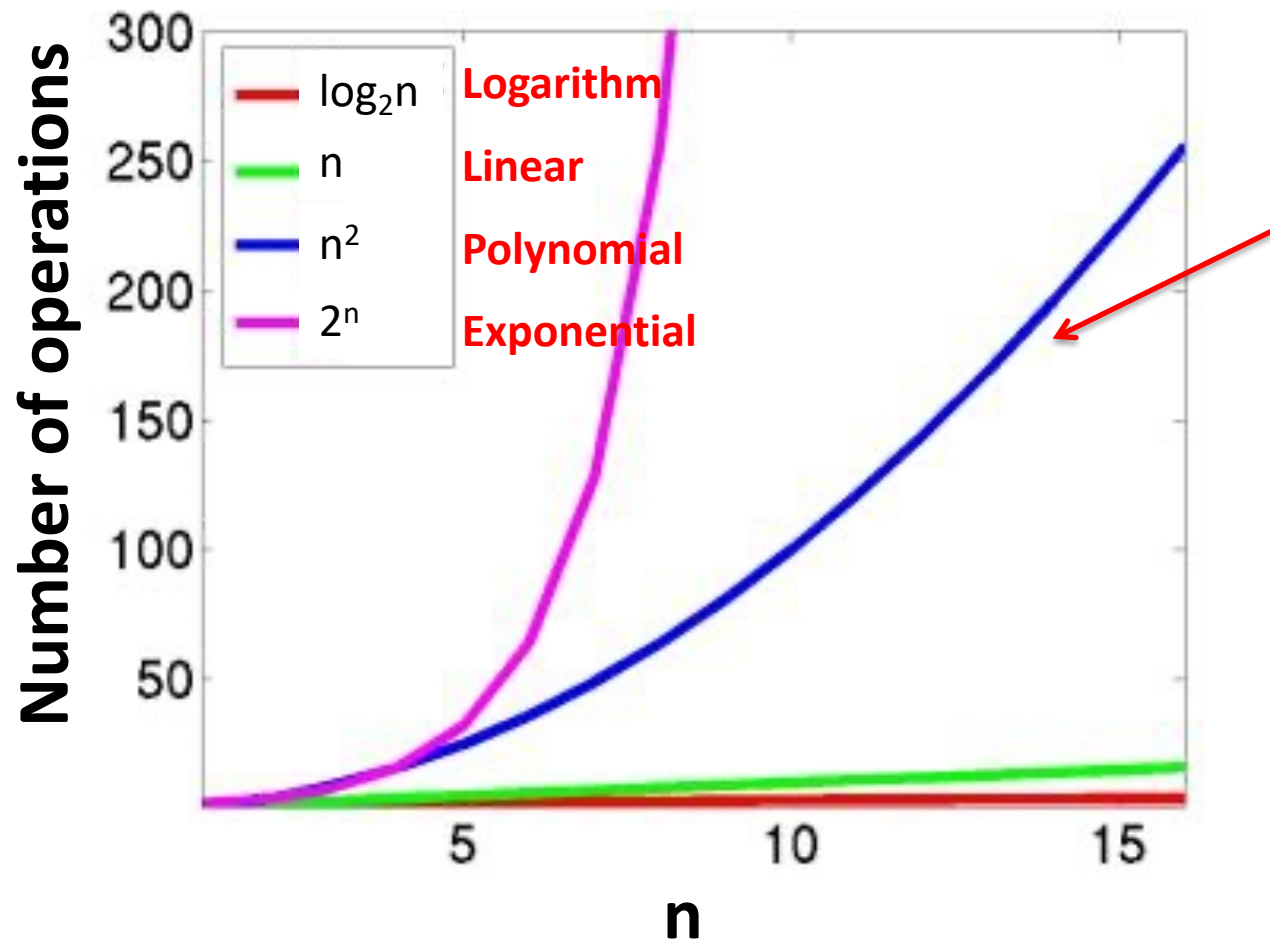
**Logarithm time – avoids operations on some items**

**Exponential time – base raised to power**

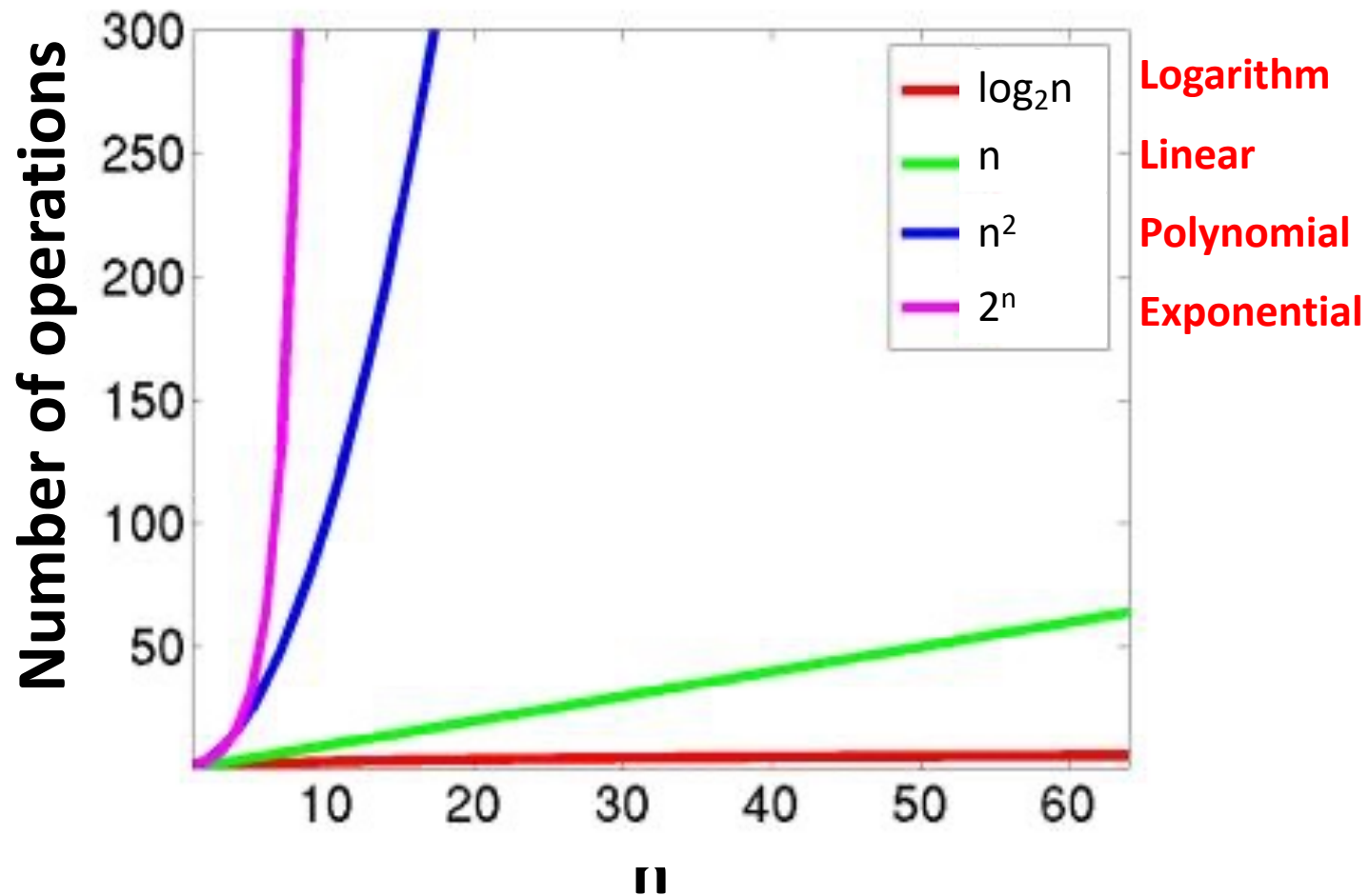
For small numbers of items, run time does not differ by much



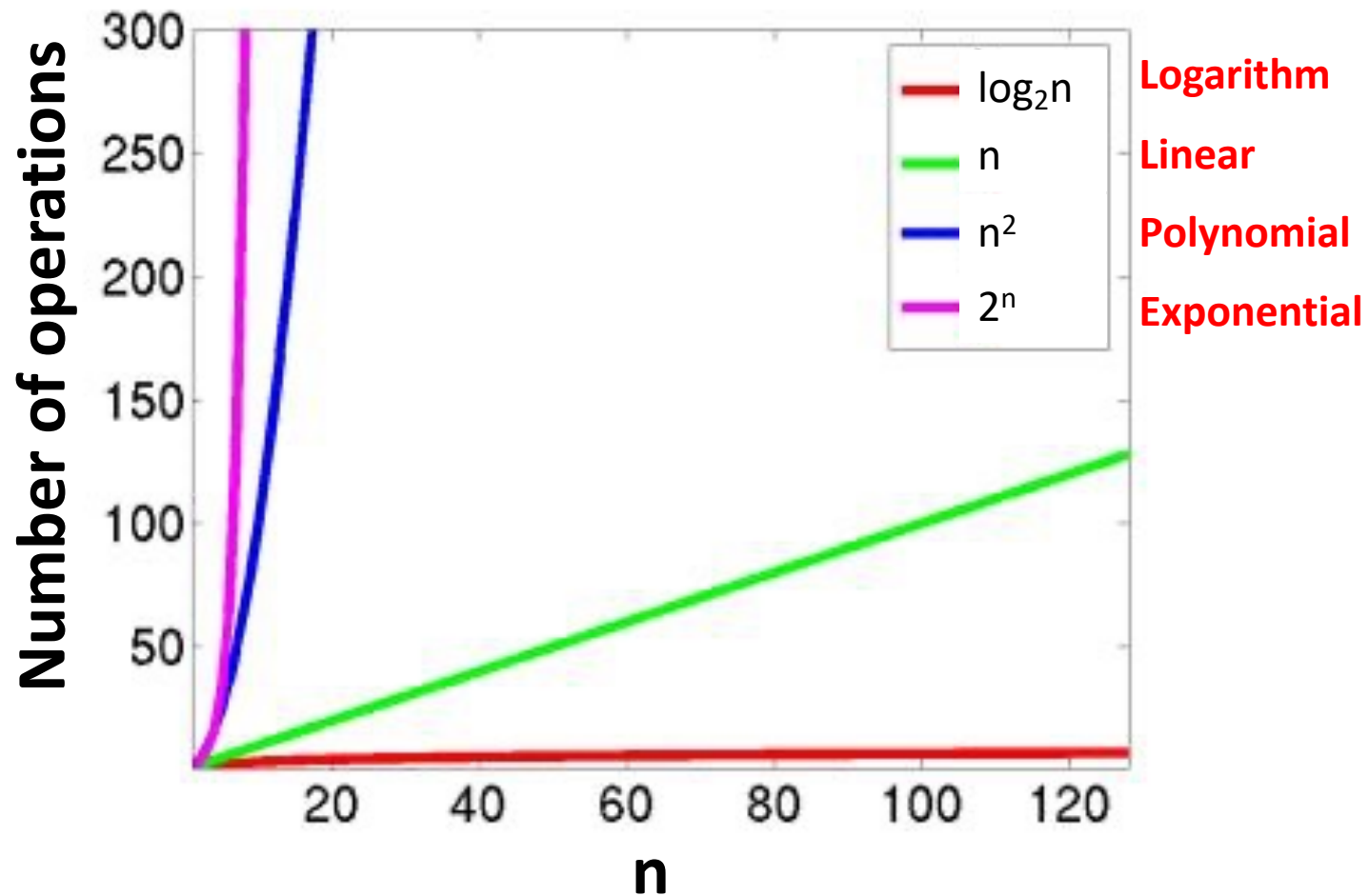
# As $n$ grows, number of operations between different algorithms begins to diverge



# Even with only 60 items, there is a large difference in number of operations



# Eventually, even with speedy computers, some algorithms become impractical



# Sometimes complexity can hurt us, sometimes it can help us



## Hurts us

Can't brute force chess  
algorithm  $2^n$




## Helps us

Can't crack password  
algorithm  $2^n$

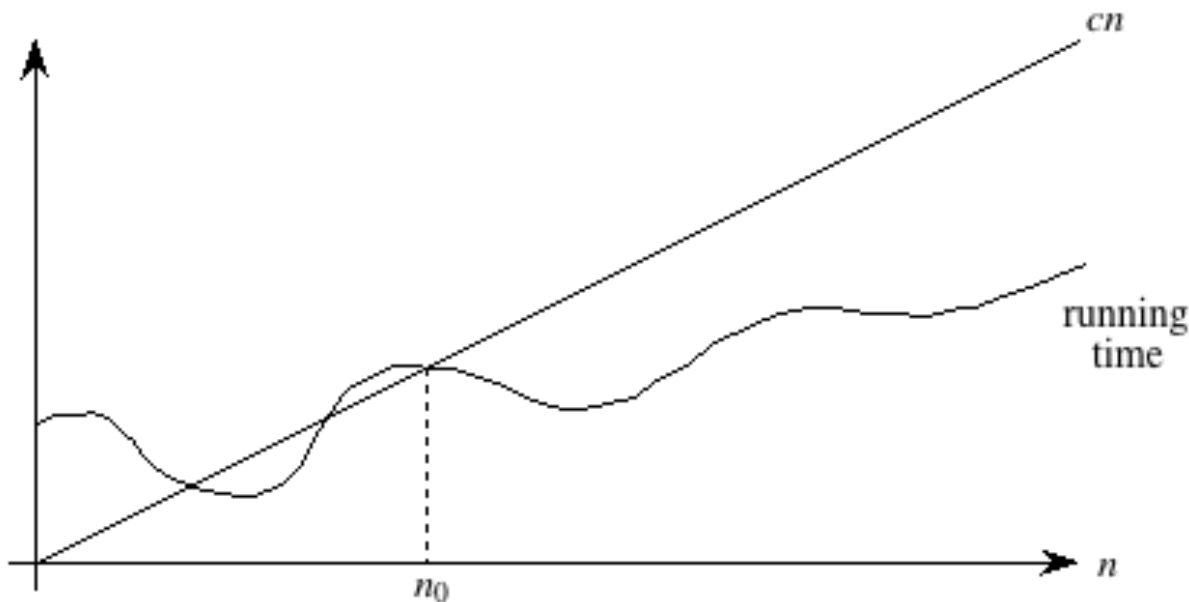


# Agenda

1. ADTs
2. Generics
3. Java provided List implementation
4. Run-time complexity
-  5. Asymptotic notation

# Computer scientists describe upper bounds on orders of growth with “Big Oh” notation

**O** gives an asymptotic upper bounds

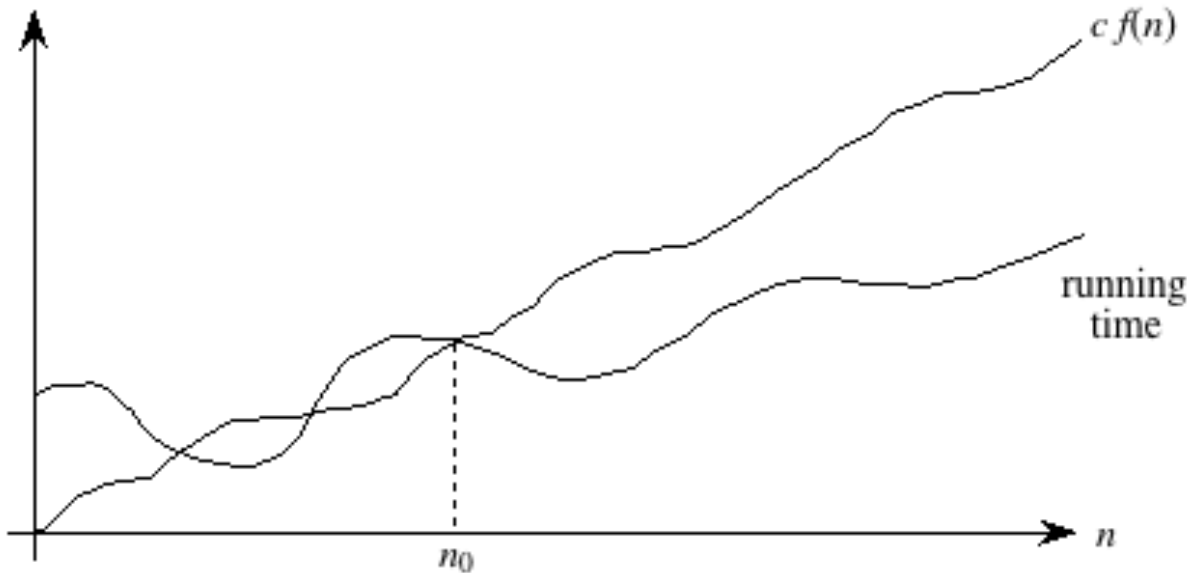


Run-time complexity is  $O(n)$  if there exists constants  $n_0$  and  $c$  such that:

- $\forall n \geq n_0$
- run time of size  $n$  is at most  $cn$ , upper bound

# We can extend Big Oh to any, not necessarily linear, function

**O** gives an asymptotic upper bounds

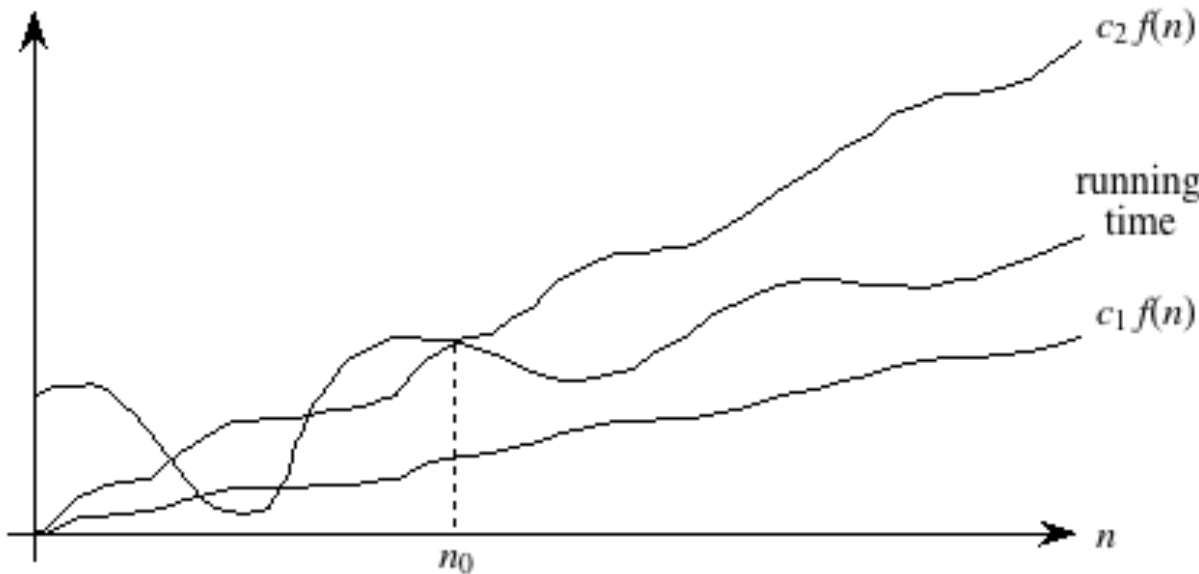


Run-time complexity is  $O(f(n))$  if there exists constants  $n_0$  and  $c$  such that:

- $\forall n \geq n_0$
- run time of size  $n$  is at most  $cf(n)$ , upper bound
- $O(f(n))$  is the worst case performance for large  $n$ , but actual performance could be better

# Run time can also be $\Omega$ (Big Omega), where run time grows at least as fast

$\Omega$  gives an asymptotic lower bounds



Run-time complexity is  $\Omega(f(n))$  if there exists constants  $n_0$  and  $c_1$  such that:

- $\forall n \geq n_0$
- run time of size  $n$  is at least  $c_1 f(n)$ , lower bound
- $\Omega(n)$  is the best case performance for large  $n$ , but actual performance can be worse

# Comparison

Example: find specific item in a list

Example: find largest item in a list

# Comparison

Example: find specific item in a list

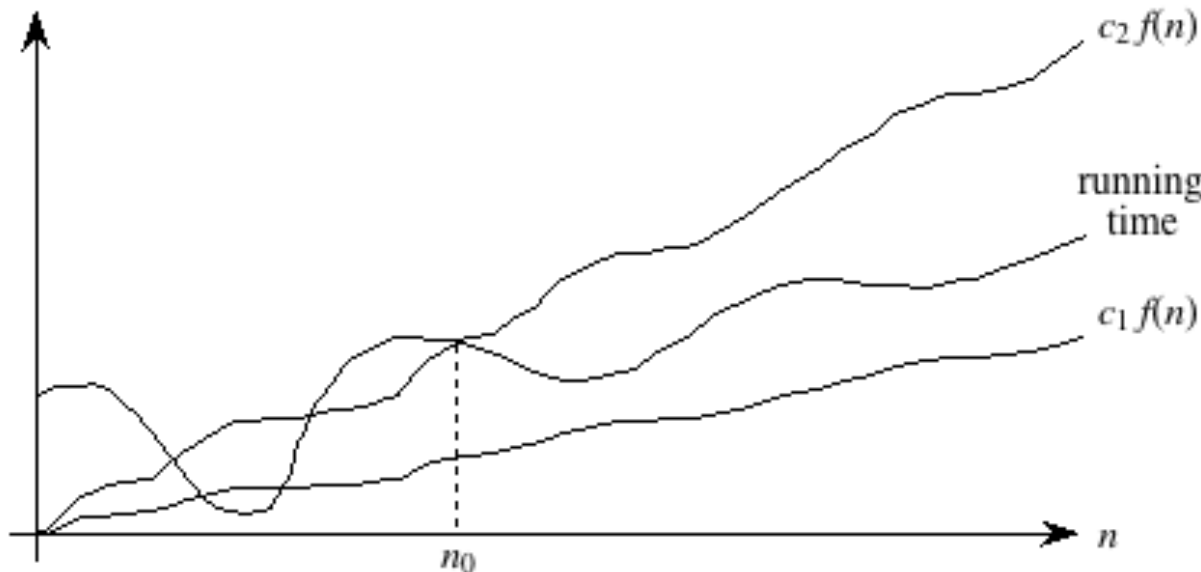
- Might find item on first try
- Might not find it at all (must check all  $n$  items in list)
- Worst case (upper bound) is  $O(n)$

Example: find largest item in a list

- Must check each  $n$  items
- Largest item could be at end of list, can't stop early
- Can't do better than  $\Omega(n)$

# We use $\Theta$ (Big Theta) for tight bounds when we can define $O$ and $\Omega$

$\Theta$  gives an asymptotic tight bounds



Run-time complexity is  $\Theta(f(n))$  if there exists constants  $n_0$  and  $c_1$  and  $c_2$  such that:

- $\forall n \geq n_0$
- run time of size  $n$  is at least  $c_1 f(n)$  and at most  $c_2 f(n)$
- $\Theta(n)$  gives a tight bound, which means run time will be within a constant factor
- Generally we will use either  $O$  or  $\Theta$

# Comparison: which has a tight bound?

Example: find specific item in a list

- Might find item on first try
- Might not find it at all (must check all  $n$  items in list)
- Worst case (upper bound) is  $O(n)$

Example: find largest item in a list

- Must check each  $n$  items
- Largest item could be at end of list, can't stop early
- Can't do better than  $\Omega(n)$



# Comparison: which has a tight bound?

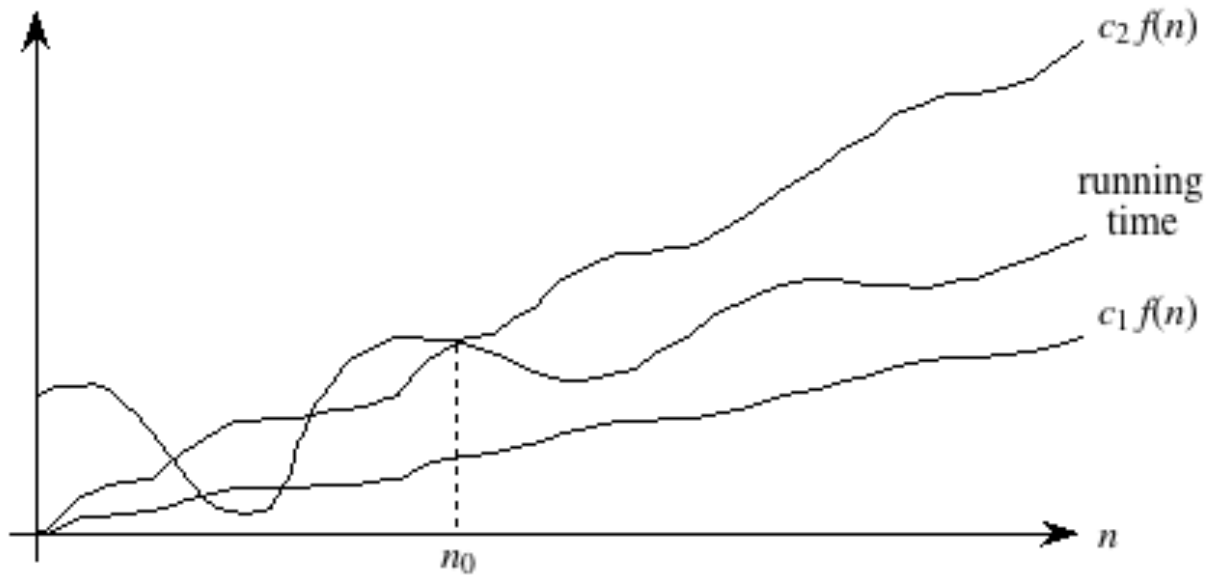
Example: find specific item in a list

- Might find item on first try
- Might not find it at all (must check all  $n$  items in list)
- Worst case (upper bound) is  $O(n)$

Example: find largest item in a list

- Must check each  $n$  items
- Largest item could be at end of list, can't stop early
- Can't do better than  $\Omega(n)$
  
- Worst case: must check each item, so  $O(n)$
- Because  $\Omega(n)$  and  $O(n)$  we say it is  $\Theta(n)$

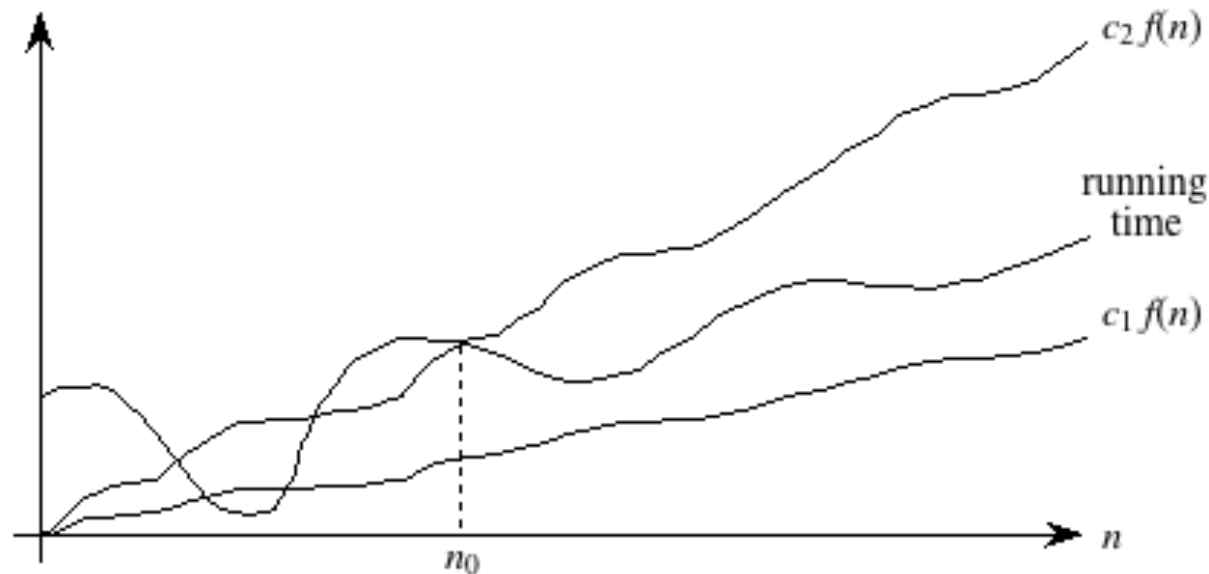
These concepts are applicable for memory complexity as well



# We ignore constants and low-order terms in asymptotic notation

Constants don't matter, just adjust  $c_1$  and  $c_2$

Low order terms don't matter either



# Summary

- Abstract data types
  - Represent data at high-level
  - Hide the way data are represented
- Generics for allowing a variable to stand in for a Java type in an interface
- ArrayList from Java
- Runtime and memory complexity analysis
  - Asymptotic notation
    - $O(1)$  constant,  $O(\log(n))$  logarithm,  $O(n)$  linear,  $O(n^2)$  polynomial,  $O(2^n)$  exponential

# Next

- Singly linked list implementation

# Additional Resources

## Annotated slides

**ADT**

# Abstract Data Types specify operations on a data set that defines overall behavior

## Abstract Data Types (ADTs)

- ADTs specify a set of *operations* (e.g., *get*, *set*, *add*, ...) that define how the ADT behaves *on a collection* of data elements
- At the ADT level we don't know (and don't really care) what data structure is used to store elements (e.g., linked list or array or something else, it doesn't matter at an abstract level)
- Also do not care about what kind of data the ADT holds (e.g., Strings, integers, Objects) – the ADT works the same way regardless of what type of data it holds
- **Big idea: hide the way data is represented and manipulated while allowing others to work with the data in a consistent manner**



# The List ADT defines required operations, but not how to implement them

## List ADT

**Big idea: List works the same regardless of what data it holds**

### Operation

### Description

`size()`

Return number of items in List

`isEmpty()`

True if no items in List, otherwise false

`get(i)`

Return the item at index  $i$

`set(i, e)`

Replace the item at index  $i$  with item  $e$

`add(e)`

Add item  $e$  to end of the list

`add(i, e)`

Insert item  $e$  at index  $i$ , moving all subsequent items one index larger

`remove(i)`

Remove and return item at index  $i$ , move all subsequent items one index smaller

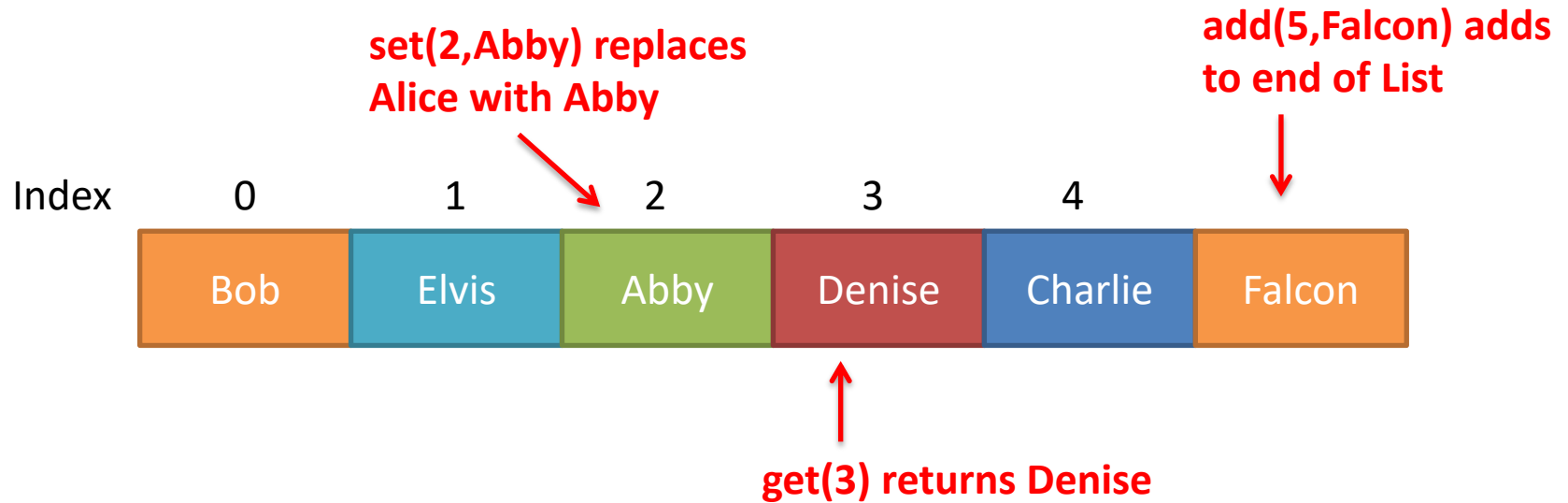
These operations MUST be implemented to complete the ADT

Free to implement other methods, but must have these

**We never say how many items the list can hold; it grows as needed**

# Example: List ADT defines a set of operations

List holds multiple elements (items) referenced by position in List



- **ADT defines these operations (and others)**
- **What data structure does it use? Array? Linked List?**
  - We don't know and don't care at the abstract level, we just care that the operations (get, set, add, ...) work as expected
- **What type of elements are these? Strings, Student Objects?**
  - See answer above – we don't care
  - The type of element does not affect how the ADT works!

# SimpleList.java is an interface that specifies what operations MUST be implemented

```
public interface SimpleList<T> extends Iterable<T> {  
    /**  
     * Returns # elements in the List (they are indexed 0..size-1)  
     */  
    public int size();  
  
    /**  
     * Returns true if there are no elements in the List, false otherwise  
     * @return true or false  
     */  
    public boolean isEmpty();  
  
    /**  
     * Adds the item at the index, which must be between 0 and size  
     */  
    public void add(int idx, T item) throws Exception;  
  
    /**  
     * Add item at end of List  
     */  
    public void add(T item) throws Exception;  
  
    /**  
     * Removes and returns the item at the index, which must be between 0 and size-1  
     */  
    public T remove(int idx) throws Exception;  
  
    /**  
     * Returns the item at the index, which must be between 0 and size-1  
     */  
    public T get(int idx) throws Exception;  
  
    /**  
     * Replaces the item at the index, which must be between 0 and size-1  
     */  
    public void set(int idx, T item) throws Exception;
```

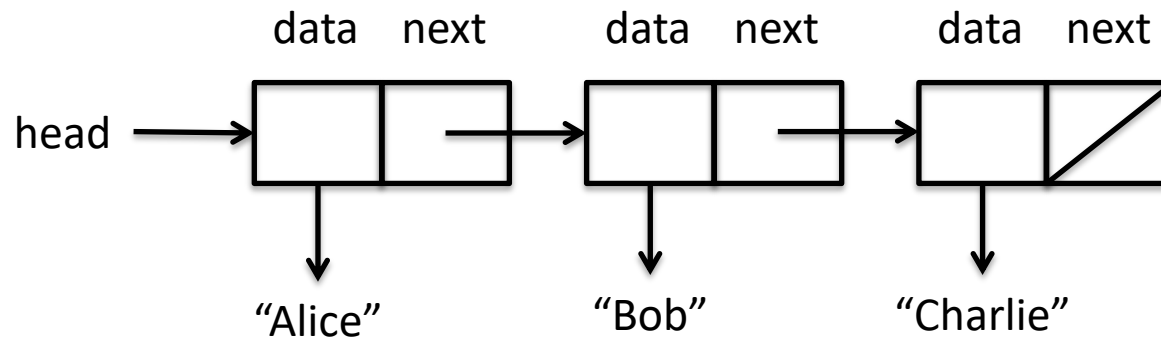
Interface keyword tells Java this is an interface (we will see Iterable and Exception in Day6)

- Methods defined to include parameters and return types (called a “signature”)
- If you are going to implement SimpleList, then you MUST implement these methods
- How you implement is your business
- Java’s List interface has a few more methods, ours simplifies things a little
- Why bother with an interface?

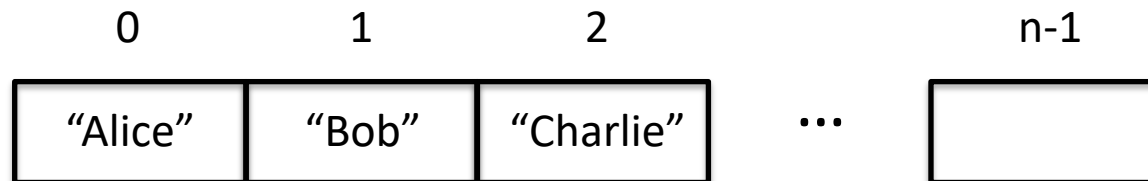
# The List ADT could be implemented with a singly linked list OR an array; either works

## Examples of List implementation

### Singly linked list



### Array



- We will implement List ADT both ways
- Each implementation has pros and cons
- Java has built-in version of the List ADT – ArrayList and LinkedList
- We will create our own two versions to contrast approaches

# GENERICICS

# Generics allow a variable to stand in for a Java type

```
public interface SimpleList<T> {  
    public T get(int idx) throws Exception;  
    public void add(int idx, T item) throws Exception;
```

- T stands for whatever object type we instantiate
- With `SimpleList<Student> list = new ArrayList<Student>();` then T always stands for Student
- `SimpleList<Point>` then T always stands for Point
- Allows us to write one implementation that works regardless of what kind of object we store in our data set
- Must use autobox version of primitives (Integer, Double, etc)
- By convention we name type of variables with a single uppercase letter, often T for “type”, later we’ll use K for key and V for value

ArrayListDemo.java

# **JAVA PROVIDED LIST IMPLEMENTATION**

# ArrayListDemo.java: ArrayLists can hold multiple objects; provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

Java provides the `ArrayList`  
We will write our own version  
of the *List* ADT using:

- Array
- Linked list

- **Declare object of type *List* on left hand side**
- **On right hand side, *new* instantiates an object of type *ArrayList***
- **Later if we decide a *LinkedList* implementation of the *List* ADT would be better, we simply change from *ArrayList* to *LinkedList***
- **In following code, we just call methods defined by the *List* ADT**
- **Here Java will use the *ArrayList* implementation**
- **If we changed *ArrayList* to *LinkedList*, Java would use the *LinkedList* implementation, but the result would be the same**



# ArrayListDemo.java: ArrayLists can hold multiple objects; provide useful methods

```
import java.util.ArrayList;
import java.util.List;
```

**Must import *ArrayList* (code is not in our project)**

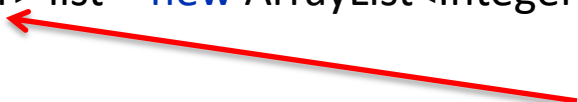
- **IntelliJ Settings/Preferences**
- **Select Editor->General->Auto Import**
- **Check the "Add unambiguous imports on the fly"**

```
public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

# ArrayListDemo.java: ArrayLists can hold multiple objects; provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```



- Provide type of objects ArrayList will hold in <> brackets (can't be primitive)
- Integer is the object version of int
- Lists can hold only one type of object (unlike Python)
- Lists are called generic containers because they can hold any type of object (Integers, Doubles, Strings, Students)
- Don't need to specify length of List, it can grow as need (unlike an array)

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

- ***add(E elmt)*** appends item to end of *List*
  - ***E = type (Integer here)***
  - ***elmt = object (element) to add to the end of the List***
- **Note: this call does not specify an index to the new item, so add at the end**

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```



- ***add(E elmt)*** appends item to end of *List*
  - ***E = type (Integer here)***
  - ***elmt = object (element) to add to the end of the List***
- **Note: this call does not specify an index to the new item, so add at the end**

**ArrayList list**

1

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```




- ***add(E elmt)*** appends item to end of *List*
  - ***E*** = type (Integer here)
  - ***elmt*** = object (element) to add to the end of the *List*
- **Note:** this call does not specify an index to the new item, so add at the end

**ArrayList list**



# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
         list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```


- *add(int i, E elmt)* adds item at index *i*
- *Lists* are zero indexed (start at index 0, unlike Matlab)
- Items slide right to make room

**ArrayList list**



# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
         list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

- *add(int i, E elmt)* adds item at index *i*
- *Lists* are zero indexed (start at index 0, unlike Matlab)
- Items slide right to make room

**ArrayList list**

1	3	2
---	---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

**Printing a List calls *toString* behind the scenes**  
**The designers of Java have already written this method for the ArrayList class**

**Output**  
[1, 3, 2]

**ArrayList list**

1	3	2
---	---	---



# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

- **ArrayLists provide random access (can get item from anywhere)**
- ***get(int i)* returns item at index *i***
- **Remember zero-based indexing!**

**Output**  
[1, 3, 2]

**ArrayList list**

1	3	2
---	---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

- **ArrayLists provide random access (can get item from anywhere)**
- ***get(int i)* returns item at index *i***
- **Remember zero-based indexing!**

## Output

[1, 3, 2]

3

## ArrayList list

1	3	2
---	---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

- Can remove item from anywhere in List
- *remove(int i)* removes item at index *i* and “pushes” remaining items left

## Output

[1, 3, 2]

3

## ArrayList list

1	3	2
---	---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

- **Can remove item from anywhere in List**
- ***remove(int i)* removes item at index *i* and “pushes” remaining items left**

## Output

[1, 3, 2]

3

[1, 2]

## ArrayList list

1	2
---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

***set(int i, E elmt) sets the item at index i to elmt***  
***Overwrites value at index i***

**Output**

[1, 3, 2]

3

[1, 2]

**ArrayList list**

1	2
---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

***set(int i, E elmt) sets the item at index i to elmt***  
***Overwrites value at index i***

**Output**

[1, 3, 2]

3

[1, 2]

**ArrayList list**

1	4
---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

## Output

[1, 3, 2]

3

[1, 2]

[1, 4]

## ArrayList list

1	4
---	---

# ArrayListDemo.java: ArrayLists can hold multiple objects, provide useful methods

```
import java.util.ArrayList;
import java.util.List;

public class ArrayListDemo {
    public static void main(String[] args) {
        List<Integer> list = new ArrayList<Integer>();
        list.add(1);
        list.add(2);
        list.add(1,3);
        System.out.println(list);
        Integer b = list.get(1);
        System.out.println(b);
        list.remove(1);
        System.out.println(list);
        list.set(1,4);
        System.out.println(list);
        System.out.println(list.size());
    }
}
```

- ***size()* returns the number of items stored in the *List***
- **Where is the last item stored?**
- ***size()-1* due to zero-based indexing**

## Output

[1, 3, 2]

3

[1, 2]

[1, 4]

2

## ArrayList list

1	4
---	---



# Lists can hold any kind of object, not just autoboxed versions of primitive data types

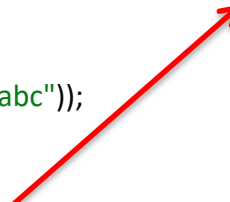
```
public class StudentTrackerAppList {  
    public static void main(String[] args) {  
        List<Student> students = new ArrayList<Student>();  
        students.add(new Student("Alice", "f00xyz"));  
        students.add(new GraduateStudent("Bob", "f00123"));  
        students.add(new InternationalStudent("Charlie", "f00abc"));  
    }  
}
```

- List to hold multiple Student objects
- Add Student to List with *add* method
- Remember because a GraduateStudent is a Student, this List can also hold GraduateStudents and any other subclasses of Student

# Lists do not declare a maximum size unlike arrays

```
public class StudentTrackerAppList {  
    public static void main(String[] args) {  
        List<Student> students = new ArrayList<Student>();  
        students.add(new Student("Alice", "f00xyz"));  
        students.add(new GraduateStudent("Bob", "f00123"));  
        students.add(new InternationalStudent("Charlie", "f00abc"));  
    }  
}
```

```
public class StudentTrackerApp {  
    public static void main(String[] args) {  
        int numberOfStudents = 3;  
        Student[] students = new Student[numberOfStudents];  
        students[0] = new Student("Alice", "f00xyz");  
        students[1] = new GraduateStudent("Bob", "f00123");  
        students[2] = new InternationalStudent("Charlie", "f00abc");  
    }  
}
```



- **Example from prior class that stored Student objects in an array**
- **Using arrays we had to declare the maximum number of Students the array could hold**
- **With a List there is no maximum number (as long as there is memory available)**

# For-each loops are available for Lists, like they are with arrays

```
public class StudentTrackerAppList {  
    public static void main(String[] args) {  
        List<Student> students = new ArrayList<Student>();  
        students.add(new Student("Alice", "f00xyz"));  
        students.add(new GraduateStudent("Bob", "f00123"));  
        students.add(new InternationalStudent("Charlie", "f00abc"));
```

```
        //print students using for-each loop  
        System.out.println("Before studying");  
        for (Student student : students) {  
            System.out.println(student);  
        }
```

```
public class StudentTrackerApp {  
    public static void main(String[] args) {  
        int numberOfStudents = 3;  
        Student[] students = new Student[numberOfStudents];  
        students[0] = new Student("Alice", "f00xyz");  
        students[1] = new GraduateStudent("Bob", "f00123");  
        students[2] = new InternationalStudent("Charlie", "f00abc");
```

```
        //print students using for-each loop  
        System.out.println("Before studying");  
        for (Student student : students) {  
            System.out.println(student);  
        }
```

**For-each loop available for arrays and Lists**



# Use *size* to get the number of items in a List

```
public class StudentTrackerAppList {  
    public static void main(String[] args) {  
        List<Student> students = new ArrayList<Student>();  
        students.add(new Student("Alice", "f00xyz"));  
        students.add(new GraduateStudent("Bob", "f00123"));  
        students.add(new InternationalStudent("Charlie", "f00abc"));
```

```
//print students using for-each loop  
System.out.println("Before studying");  
for (Student student : students) {  
    System.out.println(student);  
}
```

```
//randomly select students to study to simulate an actual application  
for (int i = 0; i < 10; i++) {  
    //pick random student  
    int index = (int) (Math.random() * students.size());  
  
    //add random studying time between 0 and 5 hours  
    double time = Math.random() * 5;  
    students.get(index).study(time);  
}
```

```
public class StudentTrackerApp {  
    public static void main(String[] args) {  
        int numberOfStudents = 3;  
        Student[] students = new Student[numberOfStudents];  
        students[0] = new Student("Alice", "f00xyz");  
        students[1] = new GraduateStudent("Bob", "f00123");  
        students[2] = new InternationalStudent("Charlie", "f00abc");
```

```
//print students using for-each loop  
System.out.println("Before studying");  
for (Student student : students) {  
    System.out.println(student);  
}
```

```
//randomly select students to study to simulate an actual application  
for (int i = 0; i < 10; i++) {  
    //pick random student  
    int index = (int)(Math.random() * numberOfStudents);  
  
    //add random studying time between 0 and 5 hours  
    double time = Math.random() * 5;  
    students[index].study(time);  
}
```

**Use *size* to get number of items in List (vs. predefined number with array)**

**Note the cast between double and int**

**Also note where the parenthesis are! Don't cast `Math.random` or you'll always get 0!**

**Why?**

**`Math.random` gives number exclusive of 1, so casting drops decimal part**

# Use *get* to retrieve an item at a given index

```
public class StudentTrackerAppList {  
    public static void main(String[] args) {  
        List<Student> students = new ArrayList<Student>();  
        students.add(new Student("Alice", "f00xyz"));  
        students.add(new GraduateStudent("Bob", "f00123"));  
        students.add(new InternationalStudent("Charlie", "f00abc"));
```

```
//print students using for-each loop  
System.out.println("Before studying");  
for (Student student : students) {  
    System.out.println(student);  
}
```

```
//randomly select students to study to simulate an actual application  
for (int i = 0; i < 10; i++) {  
    //pick random student  
    int index = (int) (Math.random() * students.size());
```

```
//add random studying time between 0 and 5 hours  
double time = Math.random() * 5;  
students.get(index).study(time);  
}
```

```
public class StudentTrackerApp {  
    public static void main(String[] args) {  
        int numberOfStudents = 3;  
        Student[] students = new Student[numberOfStudents];  
        students[0] = new Student("Alice", "f00xyz");  
        students[1] = new GraduateStudent("Bob", "f00123");  
        students[2] = new InternationalStudent("Charlie", "f00abc");
```

```
//print students using for-each loop  
System.out.println("Before studying");  
for (Student student : students) {  
    System.out.println(student);  
}
```

```
//randomly select students to study to simulate an actual application  
for (int i = 0; i < 10; i++) {  
    //pick random student  
    int index = (int)(Math.random() * numberOfStudents);
```

```
//add random studying time between 0 and 5 hours  
double time = Math.random() * 5;  
students[index].study(time);  
}
```

**Use *get* to get an item in List (vs. square brackets with array)**

# C-style for loops are also available, use *get* with them

```
public class StudentTrackerAppList {  
    public static void main(String[] args) {  
        List<Student> students = new ArrayList<Student>();  
        students.add(new Student("Alice", "f00xyz"));  
        students.add(new GraduateStudent("Bob", "f00123"));  
        students.add(new InternationalStudent("Charlie", "f00abc"));
```

```
        //print students using for-each loop  
        System.out.println("Before studying");  
        for (Student student : students) {  
            System.out.println(student);  
        }
```

```
        //randomly select students to study to simulate an actual application  
        for (int i = 0; i < 10; i++) {  
            //pick random student  
            int index = (int) (Math.random() * students.size());
```

```
            //add random studying time between 0 and 5 hours  
            double time = Math.random() * 5;  
            students.get(index).study(time);  
        }
```

```
        //print students using C-style for loop  
        System.out.println("After studying");  
        for (int i = 0; i < students.size(); i++) {  
            System.out.println(students.get(i));  
        }
```

**List use *get* to retrieve item at index (vs. square brackets with array)**

```
public class StudentTrackerApp {  
    public static void main(String[] args) {  
        int numberOfStudents = 3;  
        Student[] students = new Student[numberOfStudents];  
        students[0] = new Student("Alice", "f00xyz");  
        students[1] = new GraduateStudent("Bob", "f00123");  
        students[2] = new InternationalStudent("Charlie", "f00abc");
```

```
        //print students using for-each loop  
        System.out.println("Before studying");  
        for (Student student : students) {  
            System.out.println(student);  
        }
```

```
        //randomly select students to study to simulate an actual application  
        for (int i = 0; i < 10; i++) {  
            //pick random student  
            int index = (int)(Math.random() * numberOfStudents);
```

```
            //add random studying time between 0 and 5 hours  
            double time = Math.random() * 5;  
            students[index].study(time);  
        }
```

```
        //print students using C-style for loop  
        System.out.println("After studying");  
        for (int i = 0; i < students.size(); i++) {  
            System.out.println(students[i]);  
        }
```

# C-style for loops are also available, use *get* with them

```
public class StudentTrackerAppList {
    public static void main(String[] args) {
        List<Student> students = new ArrayList<Student>();
        students.add(new Student("Alice", "f00xyz"));
        students.add(new GraduateStudent("Bob", "f00123"));
        students.add(new InternationalStudent("Charlie", "f00abc"));

        //print students using for-each loop
        System.out.println("Before studying");
        for (Student student : students) {
            System.out.println(student);
        }

        //randomly select students to study to simulate an actual application
        for (int i = 0; i < 10; i++) {
            //pick random student
            int index = (int) (Math.random() * students.size());

            //add random studying time between 0 and 5 hours
            double time = Math.random() * 5;
            students.get(index).study(time);
        }

        //print students using C-style for loop
        System.out.println("After studying");
        for (int i = 0; i < students.size(); i++) {
            System.out.println(students.get(i));
        }
    }
}
```

## Output

```
Before studying
Name: Alice (f00xyz)
    Graduation year: null
    Hours studying: 0.0
    Hours in class: 0.0
Name: Bob (f00123)
    Graduation year: null
    Hours studying: 0.0
    Hours in class: 0.0
    Hours in the lab: 0.0
    Department: null
    Advisor: null
Name: Charlie (f00abc)
    Graduation year: null
    Hours studying: 0.0
    Hours in class: 0.0
    Home country: null
Hi Mom! It's Bob. I'm studying!
Hi Mom! It's Alice. I'm studying!
Hi Mom! It's Bob. I'm studying!
Hi Mom! It's Bob. I'm studying!
Hi Mom! It's Charlie. I'm studying!
Hi Mom! It's Bob. I'm studying!
Hi Mom! It's Alice. I'm studying!
Hi Mom! It's Alice. I'm studying!
Hi Mom! It's Bob. I'm studying!
Hi Mom! It's Alice. I'm studying!
After studying
Name: Alice (f00xyz)
    Graduation year: null
    Hours studying: 6.590768116487223
    Hours in class: 0.0
<snip>
```

# **RUN-TIME COMPLEXITY**



# How long does it take to find an item in a List?



Assume there are  $n$  items in the List (index 0 ...  $n-1$ )

Find index of "Paula" in List

What pseudo code would you use:

for  $i = 0 \dots n-1$

    get item at index  $i$

    if item is equal to search value

        return index  $i$

    return -1 (or otherwise indicate search term not in List)

How long to find the item? Should we time how long it takes?

Time would depend on

- Hardware
- Where Paula was located in the List

What is the best case?

What is the worst case?

What is the average case?

# How long does it take to find an item in a List?



Instead of timing execution we will count how many operations are needed in the worst case

- Doesn't depend on hardware or software environment
- Could use average case, but average is hard to define sometimes because it would be based on the input's distribution
- Worst case tells us it won't take longer to execute
- Allows language-independent analysis based on number of elements

## Operations to count

- Assign value to variable
- Following an object reference to heap memory
- Performing arithmetic operation (e.g., add two numbers)
- Compare two numbers (if statement)
- Access element in array
- Calling or returning from a method

# Often run-time will depend on the number of elements an algorithm must process

## Constant time – does not depend on number of items

- Returning the first element of a list takes a constant amount of time irrespective of the number of elements in the list
- Just return the first item
- No need to march down list to find the first element (*head*)
- Array *get()* implementation is also constant time (array *get()* is constant time everywhere, linked list only constant at *head*)

## Linear time – directly depends on number of items

- Example: searching for a particular value stored in a list
- Start at first item, compare value with value trying to find
- Keep going until find item, or end up at end of list
- Could get lucky and find item right away, might not find it at all
- Worst case is we check all  $n$  items

# Often run-time will depend on the number of elements an algorithm must process

## **Polynomial time – depends on a polynomial function of number of items**

- Example: nested loop in image and graphic methods
- If changing all pixels in  $n$  by  $n$  image, must do a total of  $n^2$  operations because inner and outer loops each run  $n$  times
- Normally runs slower than a constant or linear time algorithm

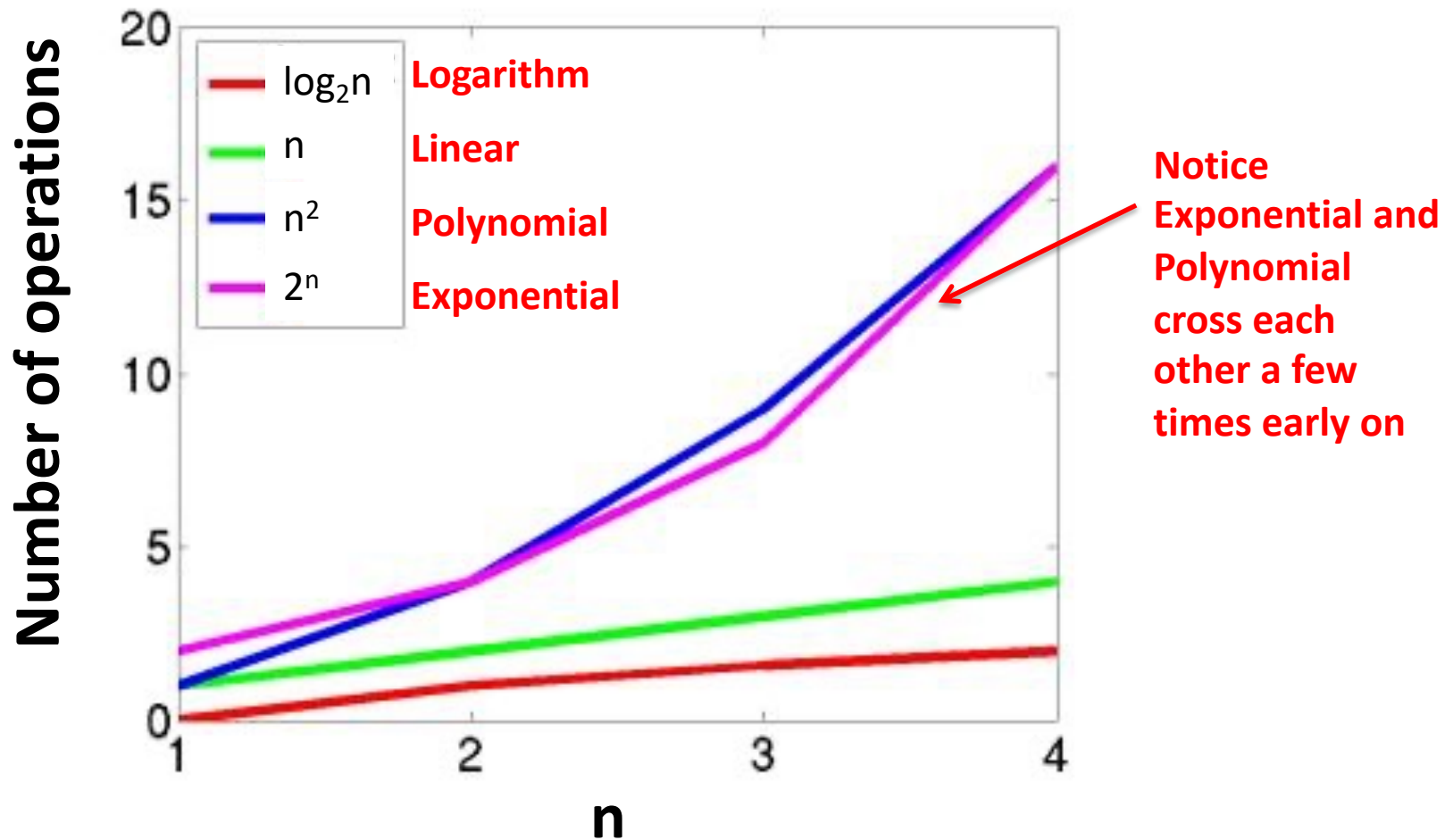
## **Logarithm time – avoids operations on some items**

- Soon we will look at binary search
- Reduces the number of items algorithm must process (don't process all  $n$  items)
- Runs faster than linear or polynomial time (slower than constant)

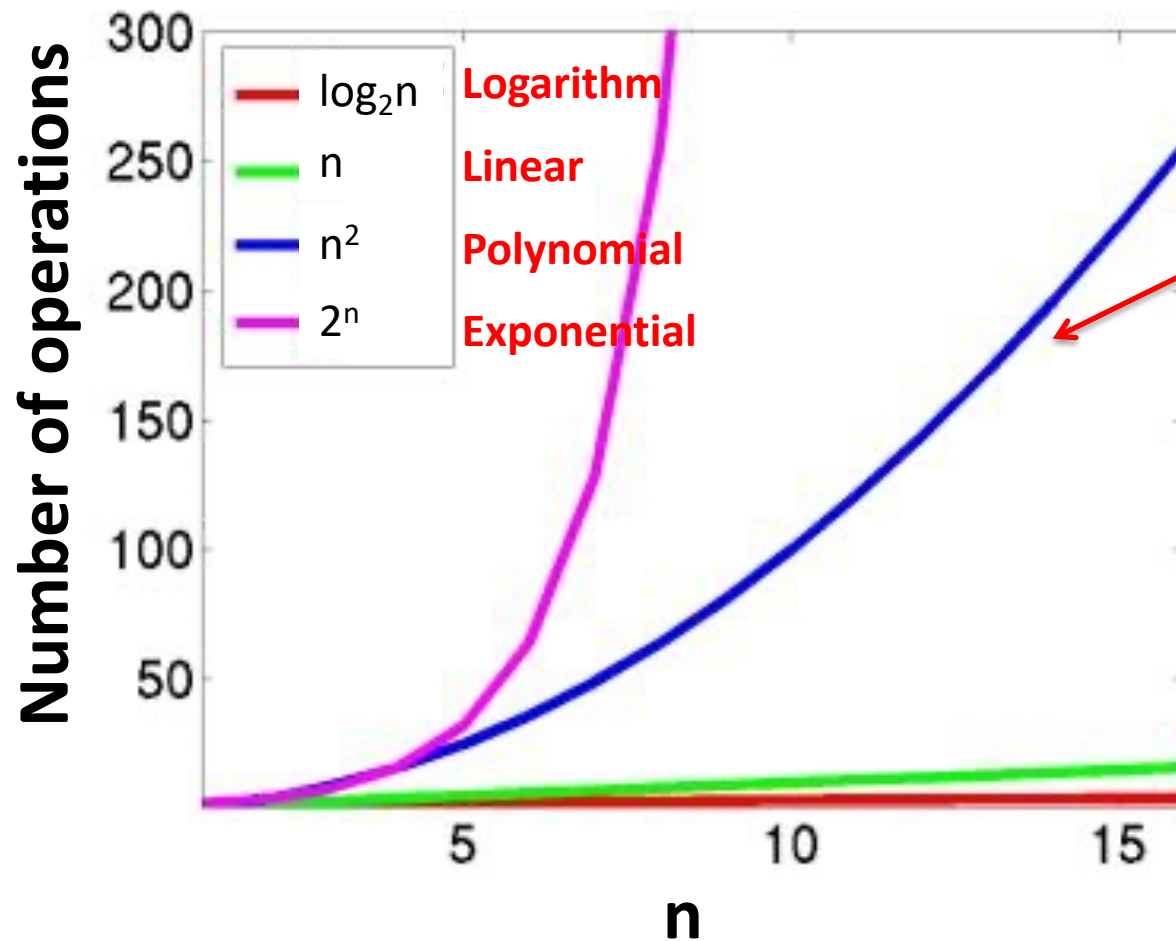
## **Exponential time – base raised to power**

- Combination problems: all possible bit combinations in  $n$  bits =  $2^n$
- SLOW!

# For small numbers of items, run time does not differ by much



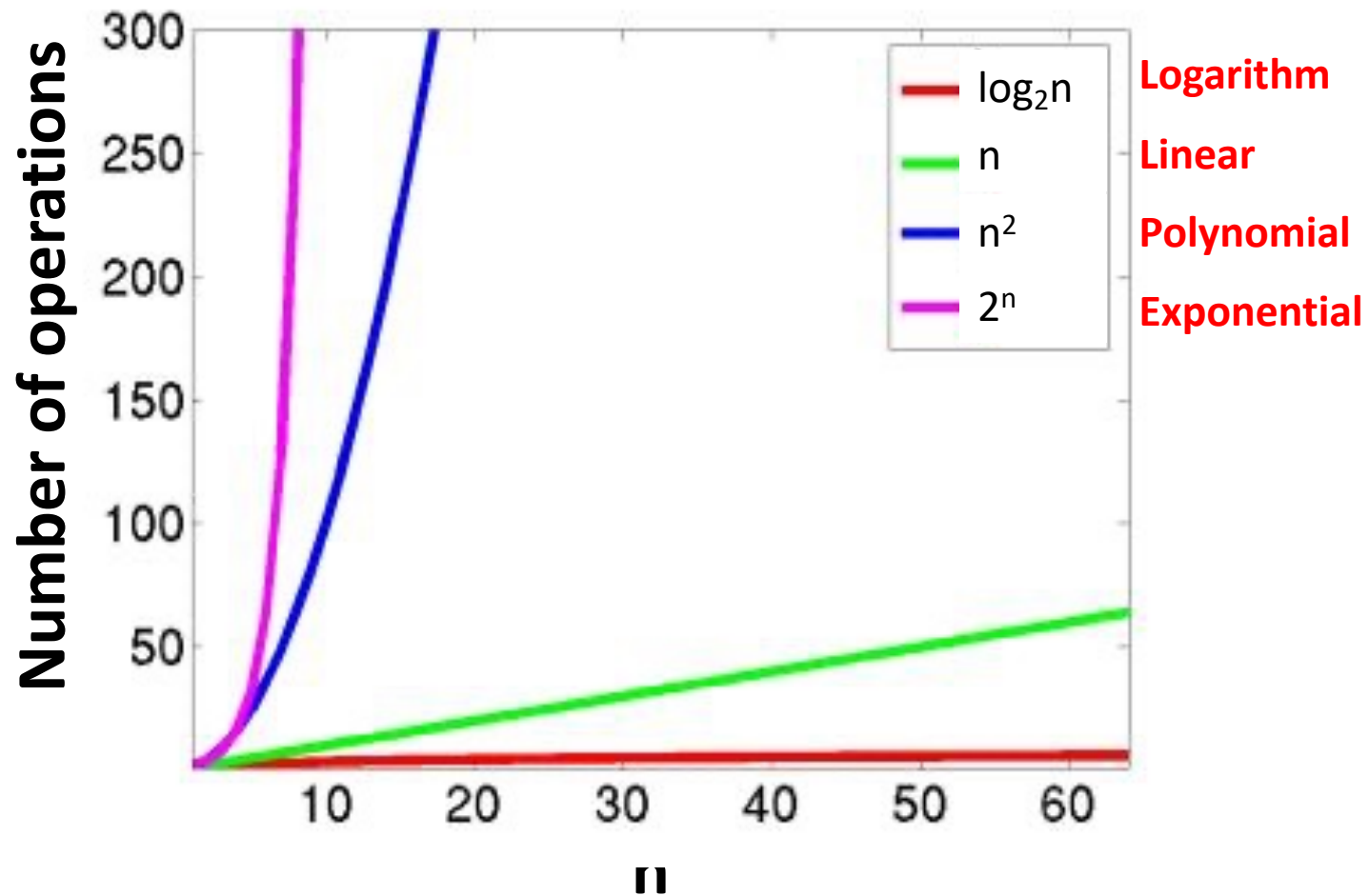
# As $n$ grows, number of operations between different algorithms begins to diverge



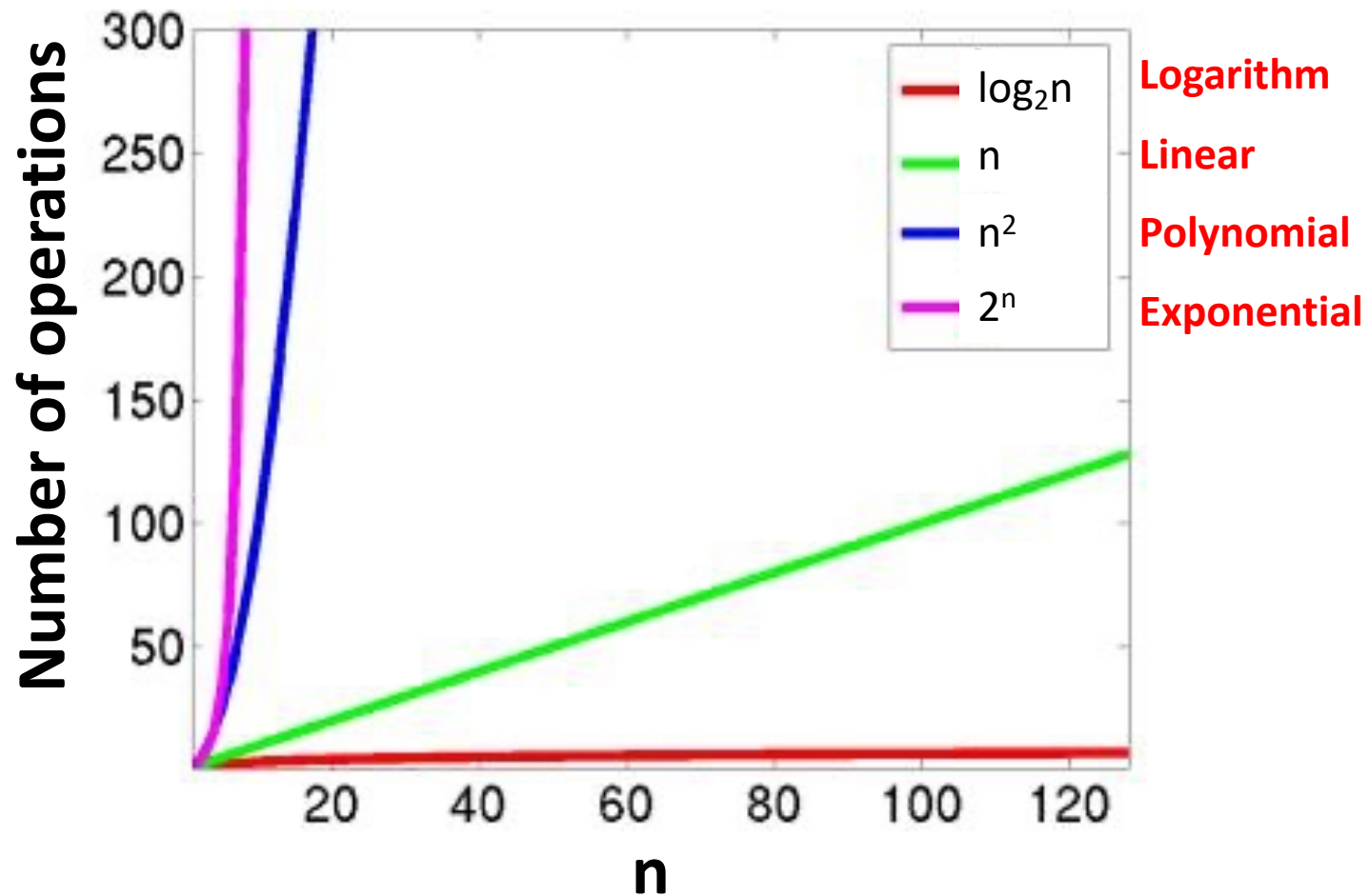
After  $n=4$   
Exponential is  
always greater  
than  
Polynomial

We will use that  
soon to define  
 $n_0$  (standby for  
more info)

# Even with only 60 items, there is a large difference in number of operations



# Eventually, even with speedy computers, some algorithms become impractical



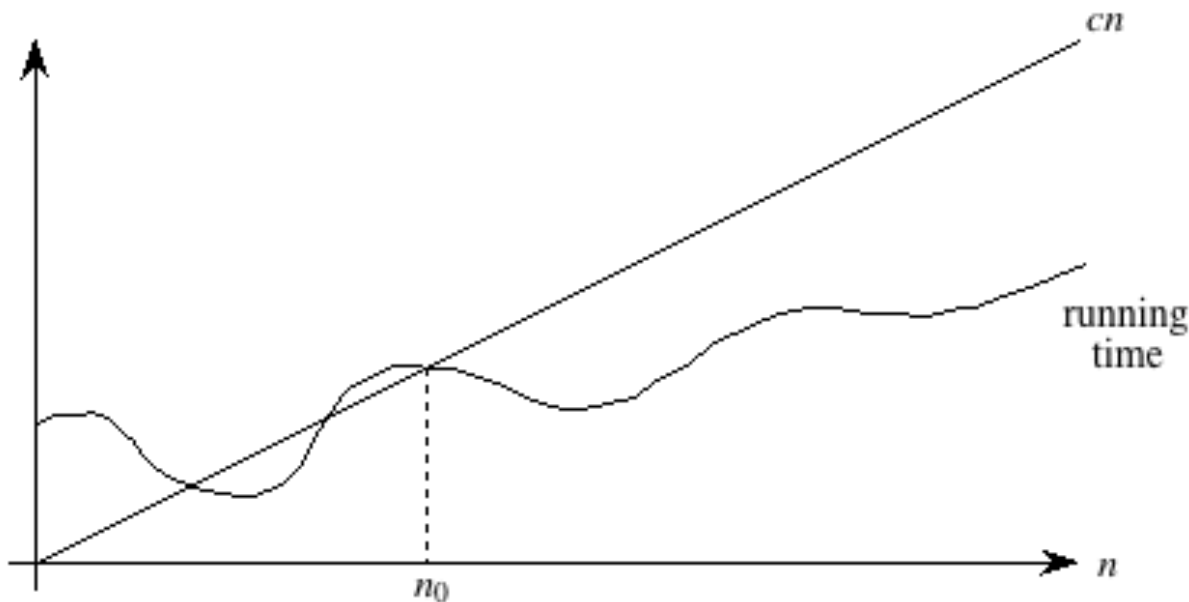


# ASYMPTOTIC NOTATION

# Computer scientists describe upper bounds on orders of growth with “Big Oh” notation

$O$  gives an asymptotic upper bounds

“Big Oh of  $n$ ”, and “Oh of  $n$ ”, and “order  $n$ ”  
all mean the same thing!



**Example: find specific item in a list**

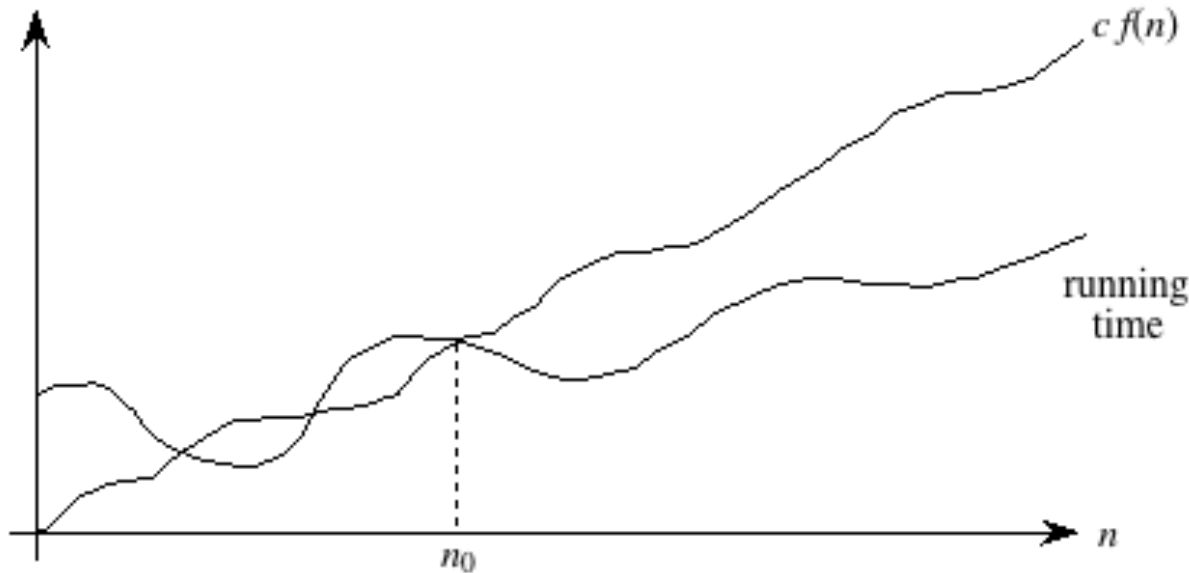
- **Might find item on first try**
- **Might not find it at all (must check all  $n$  items in list)**
- **Worst case (upper bound) is  $O(n)$**

Run-time complexity is  $O(n)$  if there exists constants  $n_0$  and  $c$  such that:

- $\forall n \geq n_0$
- run time of size  $n$  is at most  $cn$ , upper bound
- $O(n)$  is the worst case performance for large  $n$ , but actual performance could be better
- $O(n)$  is said to be “linear” time
- $O(1)$  means constant time

# We can extend Big Oh to any, not necessarily linear, function

**O** gives an asymptotic upper bounds

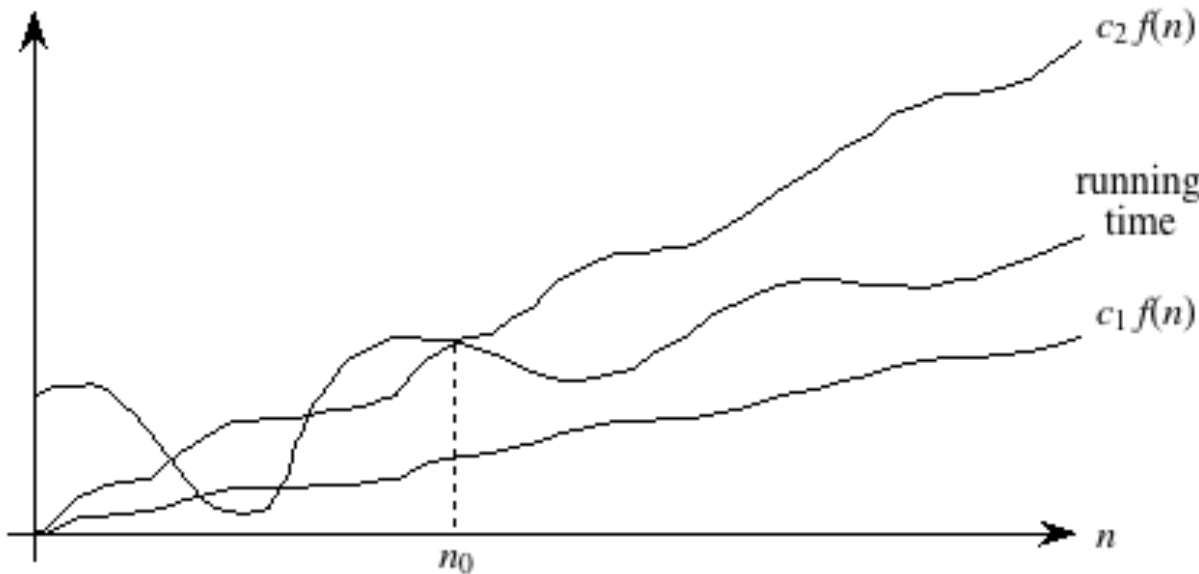


Run-time complexity is  $O(f(n))$  if there exists constants  $n_0$  and  $c$  such that:

- $\forall n \geq n_0$
- run time of size  $n$  is at most  $cf(n)$ , upper bound
- $O(f(n))$  is the worst case performance for large  $n$ , but actual performance could be better
- $f(n)$  can be a non-linear function such as  $n^2$  or  $\log(n)$
- In that case  $O(n^2)$  or  $O(\log n)$

# Run time can also be $\Omega$ (Big Omega), where run time grows at least as fast

$\Omega$  gives an asymptotic lower bounds



**Example: find largest item in a list**

- **Must check each  $n$  items**
- **Largest item could be at end of list, can't stop early**
- **Can't do better than  $\Omega(n)$**

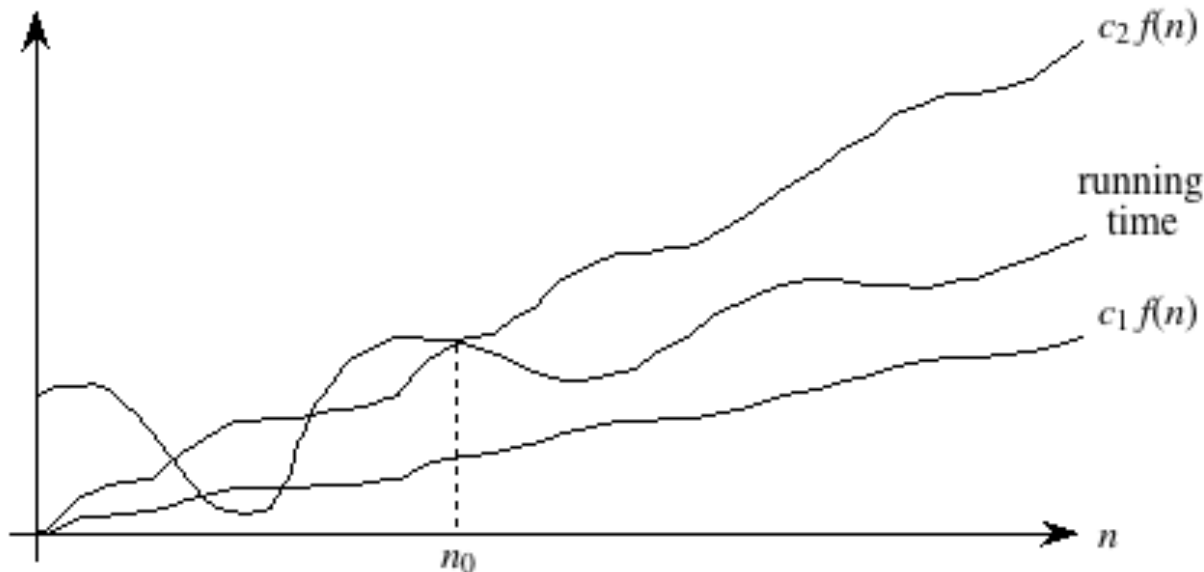
Run-time complexity is  $\Omega(f(n))$  if there exists constants  $n_0$  and  $c_1$  such that:

- $\forall n \geq n_0$
- run time of size  $n$  is at least  $c_1 f(n)$ , lower bound
- $\Omega(n)$  is the best case performance for large  $n$ , but actual performance can be worse

# We use $\Theta$ (Big Theta) for tight bounds when we can define $O$ and $\Omega$

$\Theta$  gives an asymptotic tight bounds

We can also apply these concepts to how much memory an algorithm uses (not just run-time complexity)



**Example: find largest item in a list**

- **Best case: already seen it is  $\Omega(n)$**
- **Worst case: must check each item, so  $O(n)$**
- **Because  $\Omega(n)$  and  $O(n)$  we say it is  $\Theta(n)$**

Run-time complexity is  $\Theta(f(n))$  if there exists constants  $n_0$  and  $c_1$  and  $c_2$  such that:

- $\forall n \geq n_0$
- run time of size  $n$  is at least  $c_1 f(n)$  and at most  $c_2 f(n)$
- $\Theta(n)$  gives a tight bound, which means run time will be within a constant factor
- Generally we will use either  $O$  or  $\Theta$
- **$O$ ,  $\Omega$ ,  $\Theta$  called asymptotic notation**

# We ignore constants and low-order terms in asymptotic notation

## Constants don't matter, just adjust $c_1$ and $c_2$

- Constant multiplicative factors are absorbed into  $c_1$  (and  $c_2$ )
- Example:  $1000n^2$  is  $O(n^2)$  because we can choose  $c_1$  to be 1000 (remember bounded by  $c_1n$ )
- Do care in practice – if an operation takes a constant time,  $O(1)$ , but more than 24 hours to complete, can't run it everyday

## Low order terms don't matter either

- If  $n^2+1000n$ , then choose  $c_1 = 1$ , so now  $n^2 + 1000n \geq c_1n^2$
- Now must find  $c_2$  such that  $n^2 + 1000n \leq c_2n^2$
- Subtract  $n^2$  from both sides and get  $1000n \leq c_2n^2 - n^2 = (c_2-1)n^2$
- Divide both sides by  $(c_2-1)n$  gives  $1000/(c_2-1) \leq n$
- Pick  $c_2 = 2$  and  $n_0 = 1000$ , then  $\forall n \geq n_0, 1000 \leq n$
- So,  $n^2 + 1000n \leq c_2n^2$ , try with  $n=1000$  get  $n^2 + 1000^2 = 2*n^2$
- **In practice, we simply ignore constants and low order terms**

# How to write them

Constant time  
 $O(1)$

Linear time  
 $O(n)$

Polynomial time  
 $O(n^2)$