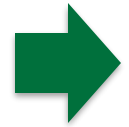


CS 10:

# Problem solving via Object Oriented Programming

## Relationships

# Agenda



1. Graphs

2. Four common representations

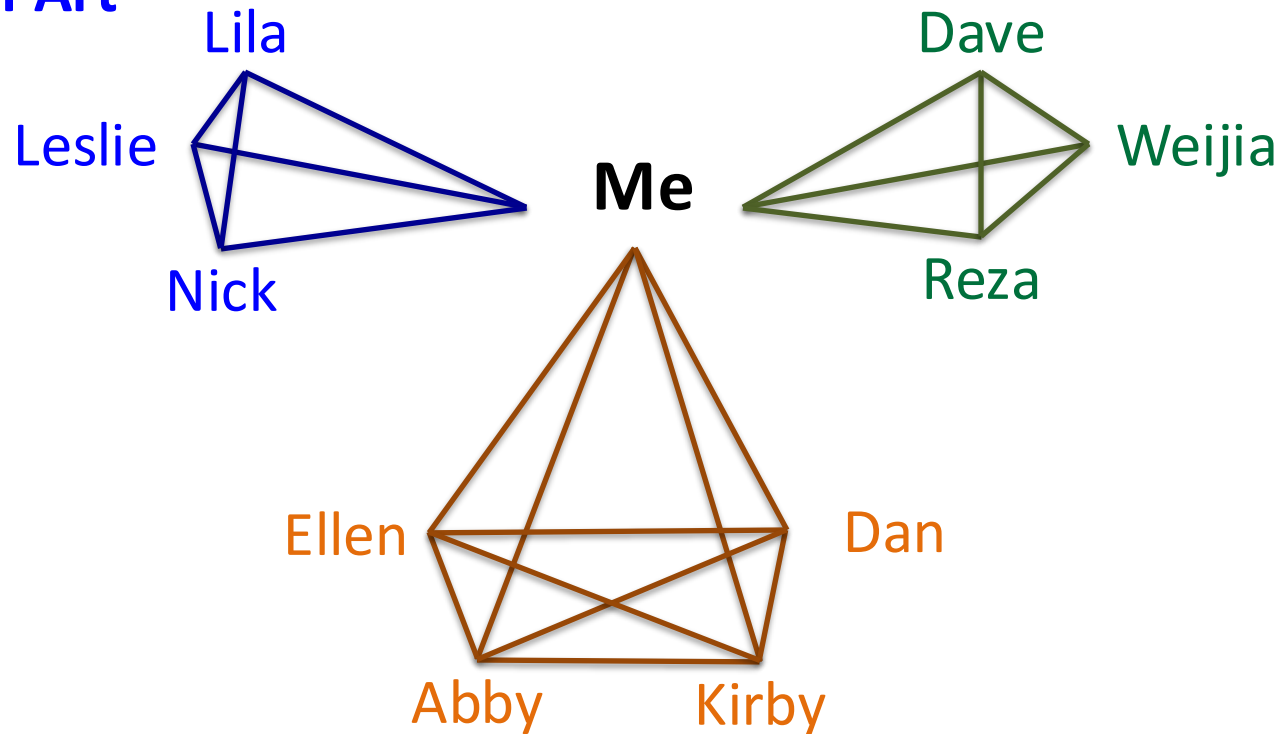
3. Implementation

# Graphs are a useful way to represent relationships between Objects

## My coworkers

The Metropolitan  
Museum of Art

Dartmouth

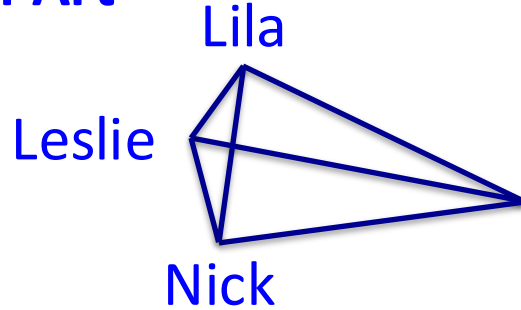


Start up

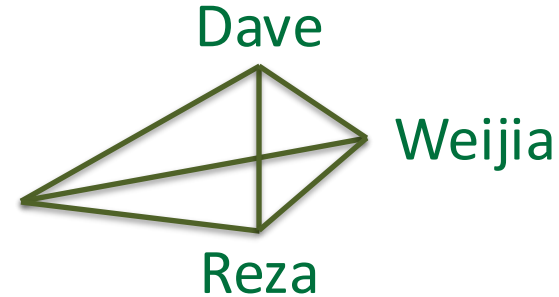
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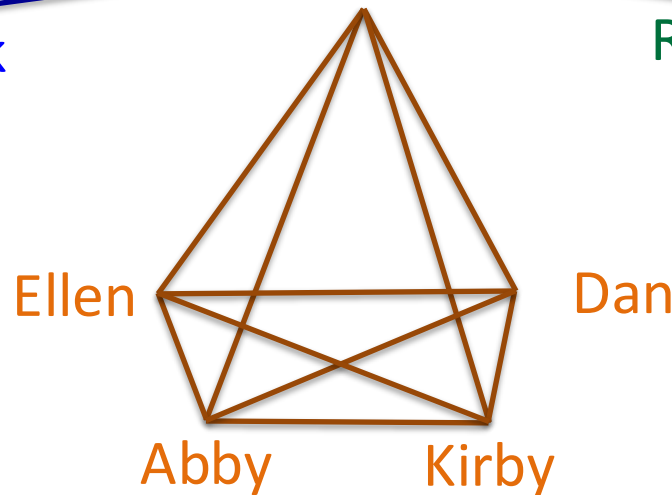
The Metropolitan  
Museum of Art



Dartmouth



- I know everyone

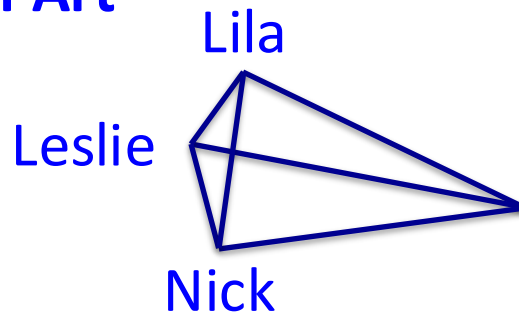


Start up

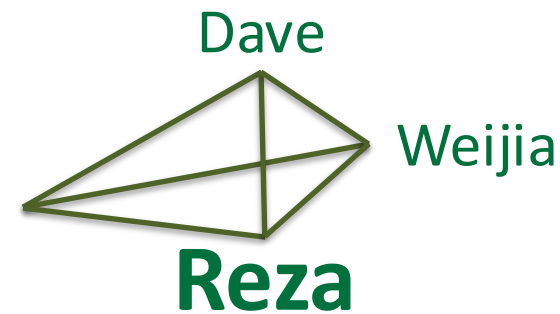
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## My coworkers

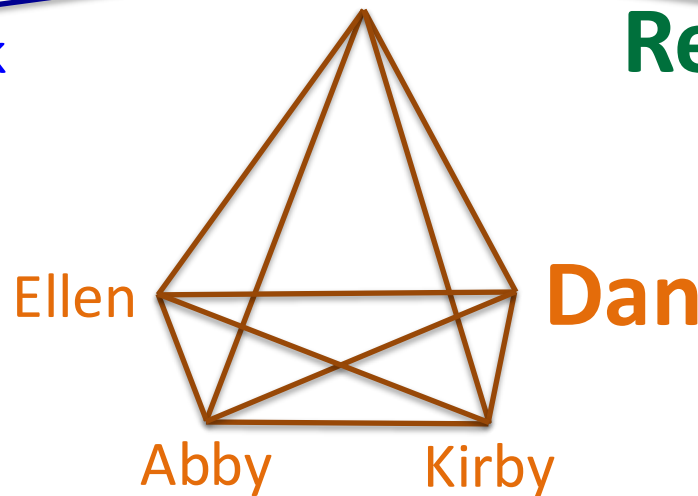
The Metropolitan  
Museum of Art



Dartmouth



- I know everyone
- Reza and Dan do not know each other directly

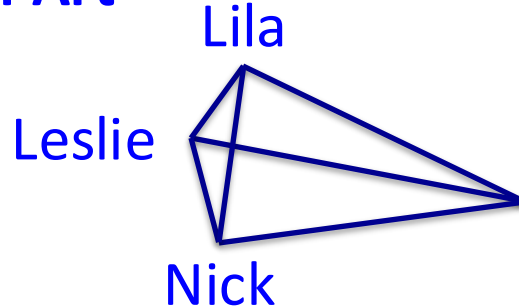


Start up

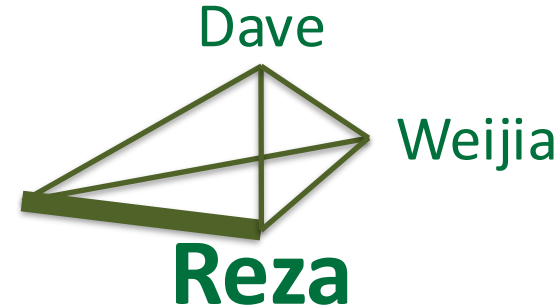
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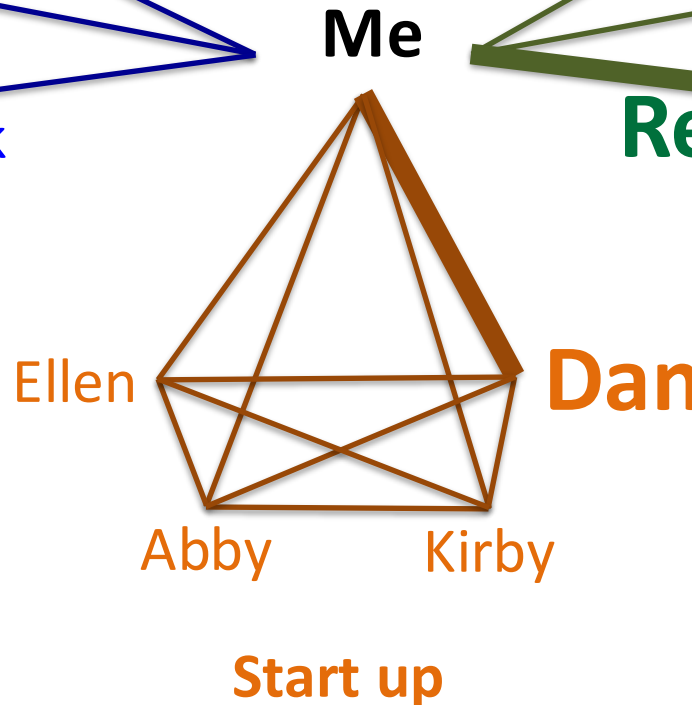
The Metropolitan  
Museum of Art



Dartmouth



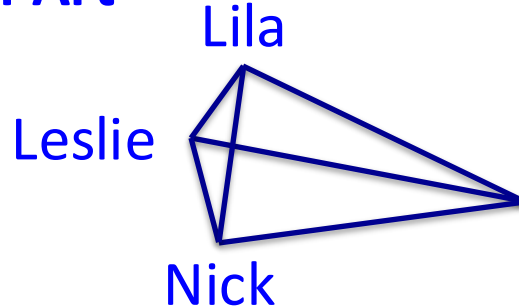
- I know everyone
- Reza and Dan do not know each other directly
- But I could introduce them (there is a **path**)



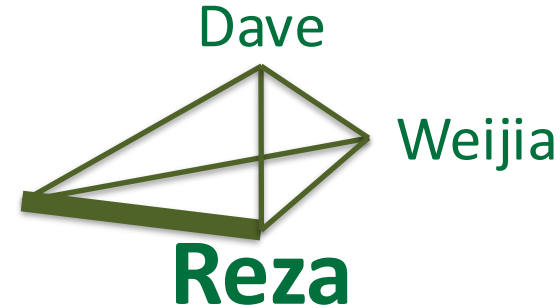
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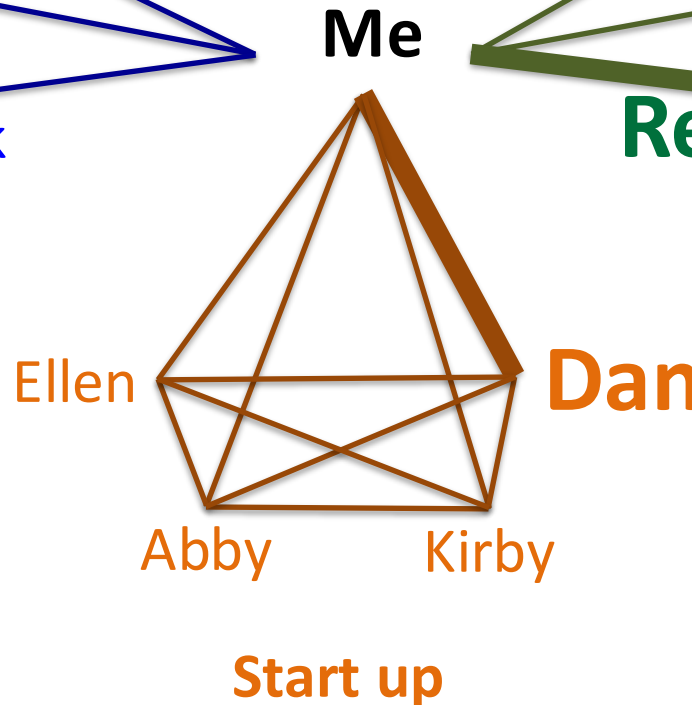
### The Metropolitan Museum of Art



### Dartmouth



- I know everyone
- Reza and Dan do not know each other directly
- But I could introduce them (there is a **path**)



- Nodes are said to be **reachable** if there is a path between them
- There may be nodes that are unreachable

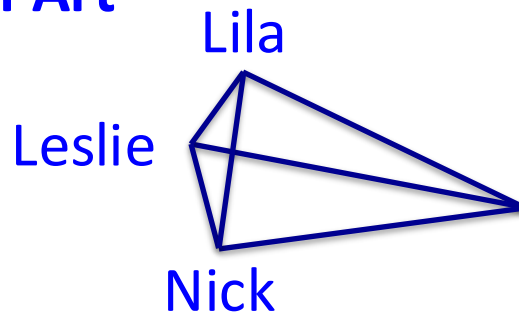
# Graphs are a useful way to represent relationships between Objects

## My coworkers

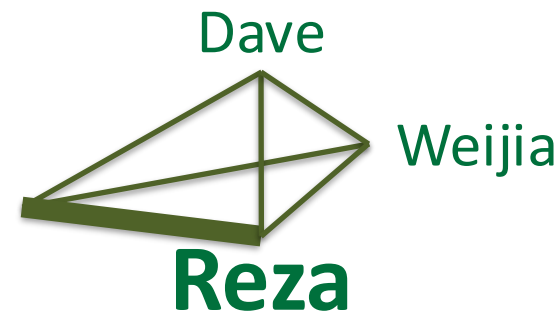
Kevin  
Bacon



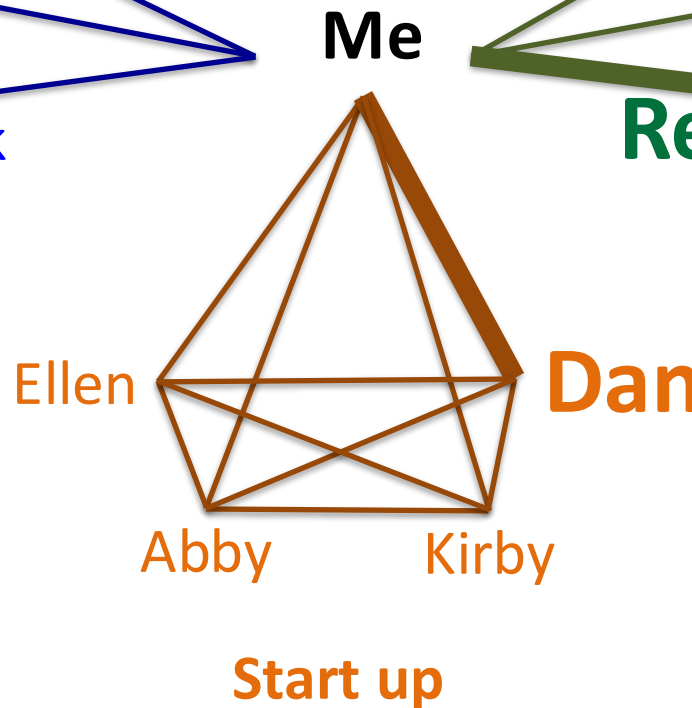
## The Metropolitan Museum of Art



## Dartmouth



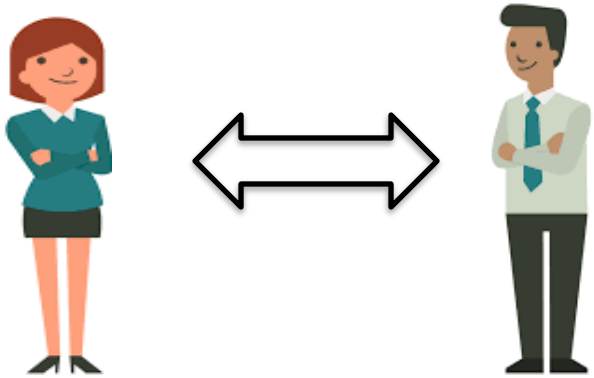
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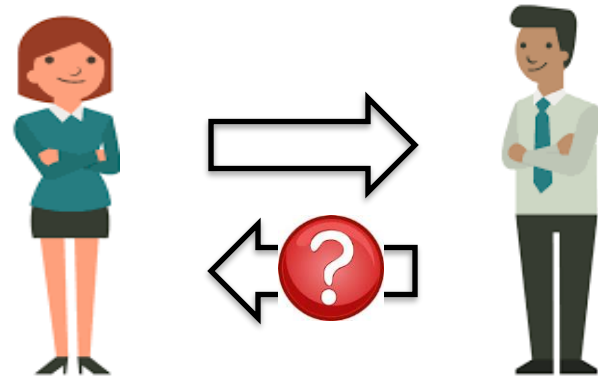
- Nodes are said to be **reachable** if there is a path between them
- There may be nodes that are unreachable



# Two types of relationships: Undirected and directed



**Undirected (Symmetrical)**  
If Alice is friends with Bob,  
then Bob is friends with  
Alice



**Directed (Asymmetrical)**  
If Alice follows Bob, then  
Bob does not necessarily  
follow Alice

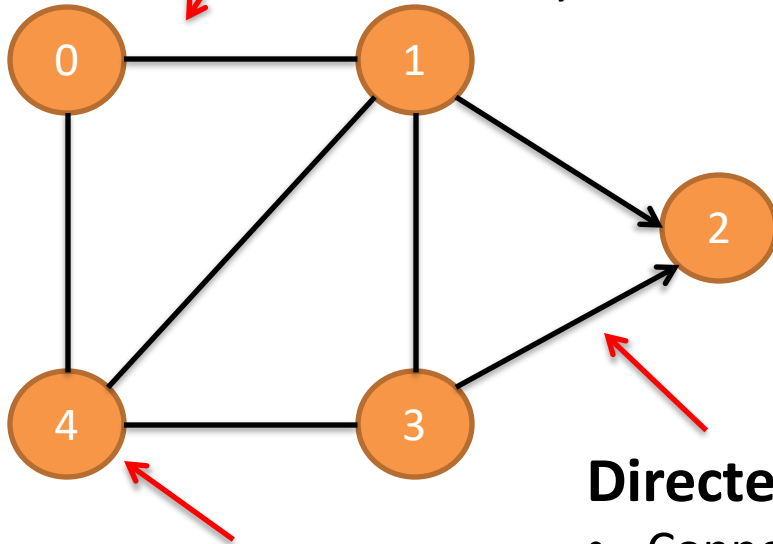
# Graphs represent directed or undirected relationships with nodes and edges

## Graphs

### Undirected edges

- Connect objects in both directions
- “Two-way street”

facebook



### Directed edges

- Connect objects in a single directions
- “One-way street”



### Nodes (vertices)

- Represent objects
- Could be a person or city or computer or intersection of roads...

### Undirected graph

Only undirected edges

### Directed graph

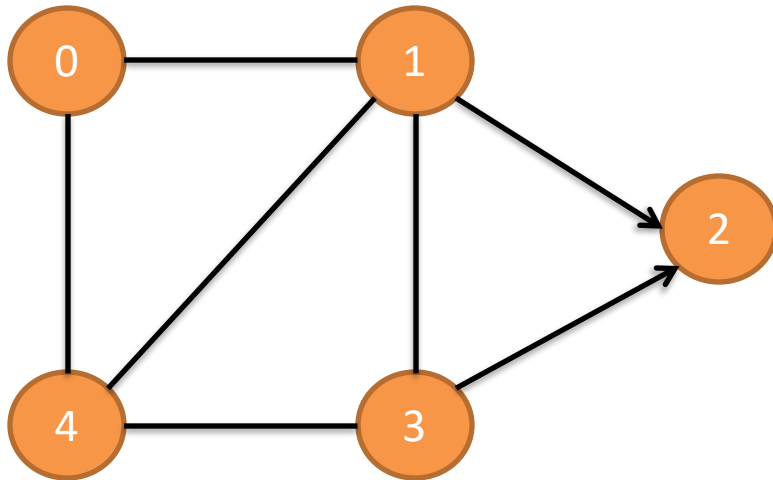
Only directed edges

### Mixed graph

Has both directed and undirected edges

# Both nodes and edges can hold information about the relationship

## Graphs



### Nodes

- Represent an Object
- Can be as simple as a String
- Could be more complex like an Object from a Person Class

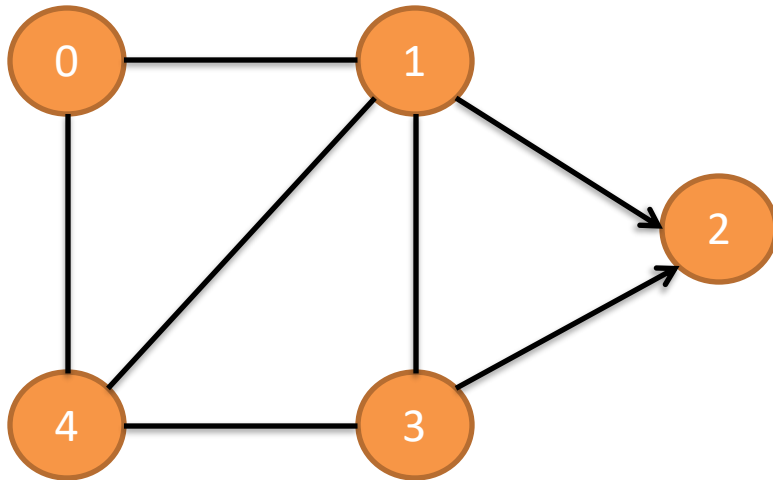
### Edges

- Can hold information about relationship
  - Distance between cities
  - Capacity of a pipe
  - Label of relationship type (“follower”, “friend”, “co-worker”)

# Graph interface defines several useful methods

## Graph.java

Interface on  
course web page



## Create/alter graph structure

`insertVertex(v)`

Add node  $v$  to graph

`insertDirected(u, v) / Undirected(u, v)`

Add edge to graph between node  $u$  and node  $v$

`removeVertex(v) / removeDirected(u, v) / removeUndirected(u, v)`

Remove node  $v$  or edge from  $u$  to  $v$

## Use graph

`outDegree(v) / inDegree(v)`

Count of edges out of or into node  $v$

`outNeighbors(v) / inNeighbors(v)`

Other nodes connected from/to node  $v$

`hasEdge(u, v)`

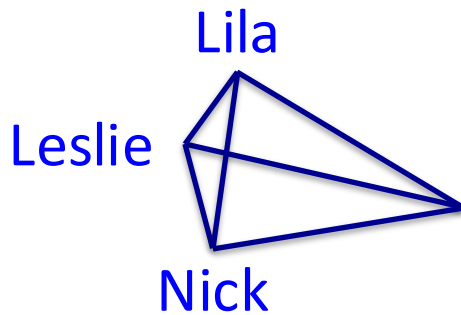
True if node  $u$  connected to node  $v$

`getLabel(u, v)`

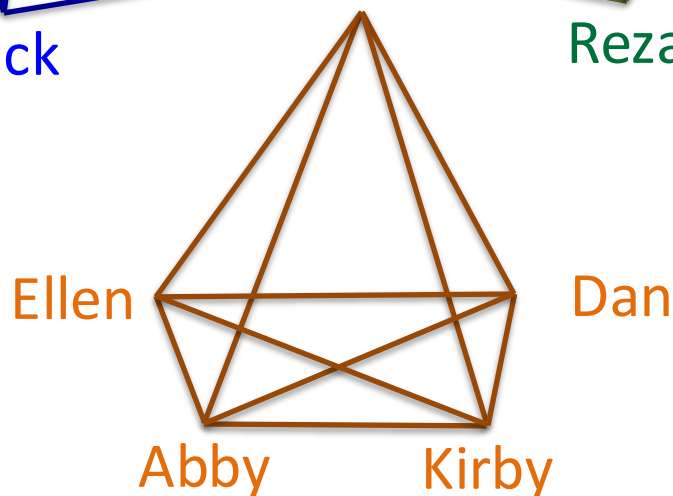
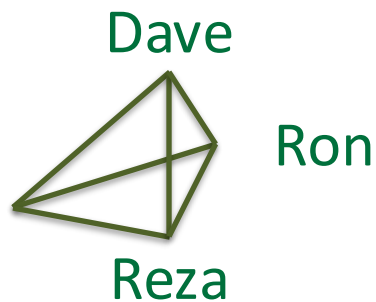
Return label on edge from node  $u$  to node  $v$

# We can use Graph ADT methods to answer interesting questions

## The Metropolitan Museum of Art



## Dartmouth



## Start up

## Questions we can answer

- Who is the most connected? (most in edges)
- Who are mutual acquaintances (“cliques” where all nodes have edges to each other)
- Who is a friend-of-a-friend but is not yet a friend? (breadth-first search, next class)

# Agenda

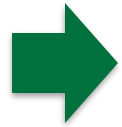
1. Graphs

 2. Four common representations

3. Implementation

# Graphs are commonly represented in one of four different ways

## Common Graph representations

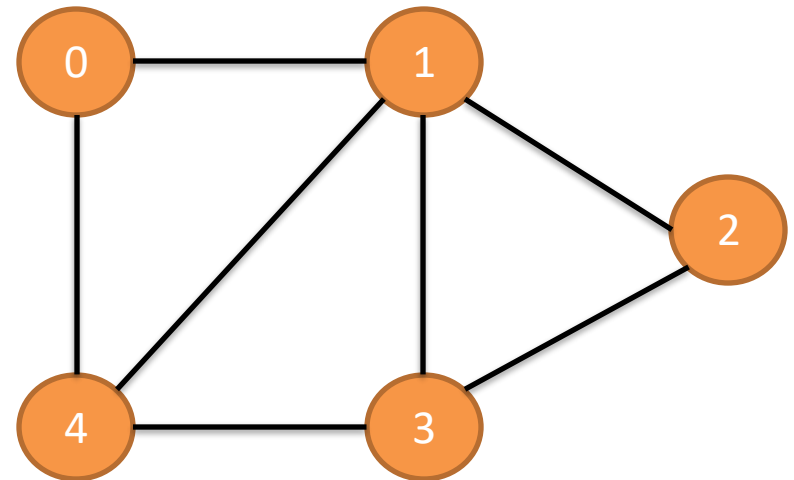


1. Edge List

2. Adjacency List

3. Adjacency Matrix

4. Adjacency Map



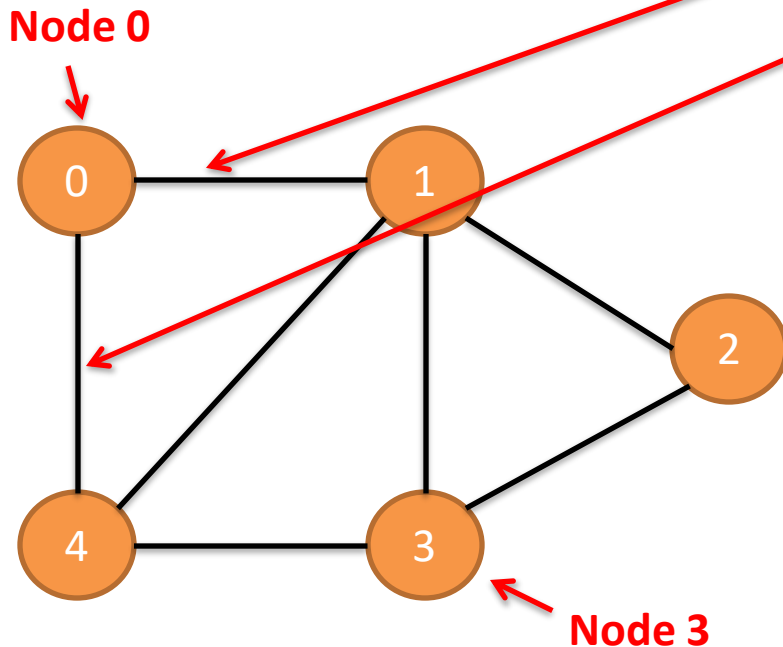
# Edge Lists create an unordered list of vertex pairs where each entry is an edge

## 1. Edge List List of edges

Edge list  
{node #, node #}

{ {0,1}, {0,4}, {1,2}, {1,3},  
{1,4}, {2,3}, {3,4} }

This approach is mainly used to explain concepts, not used in production code



**Assume:**

n nodes (here 5)

m edges (here 7)

### Notes:

- Number nodes 0..n-1
- Edge List stores pairs of indexes that reference nodes
- Each Edge List entry represents an edge between two nodes
- $m$  total entries in Edge List
- Can be ordered to show directed edges
- Insert edge fast, just add to list
- Everything else slow
- Example: `removeVertex` is  $\theta(m)$ , have to remove all edges to/from node, so search all edges leading to or from node



# Graphs are commonly represented in one of four different ways

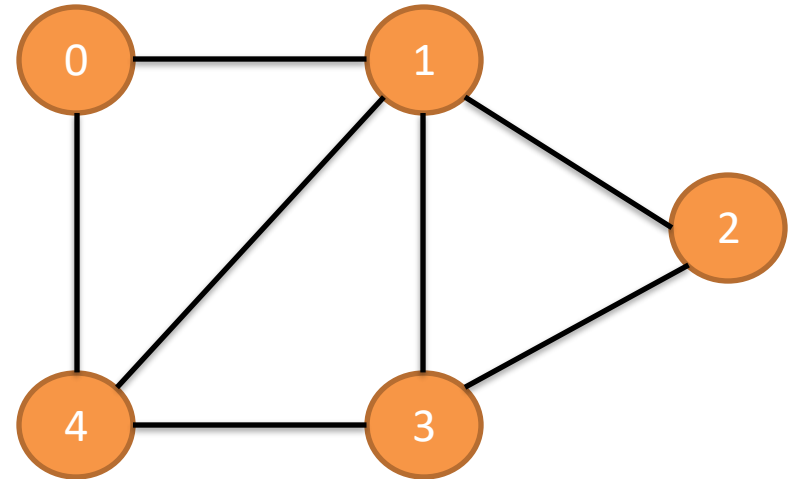
## Common Graph representations

1. Edge List

➔ 2. Adjacency List

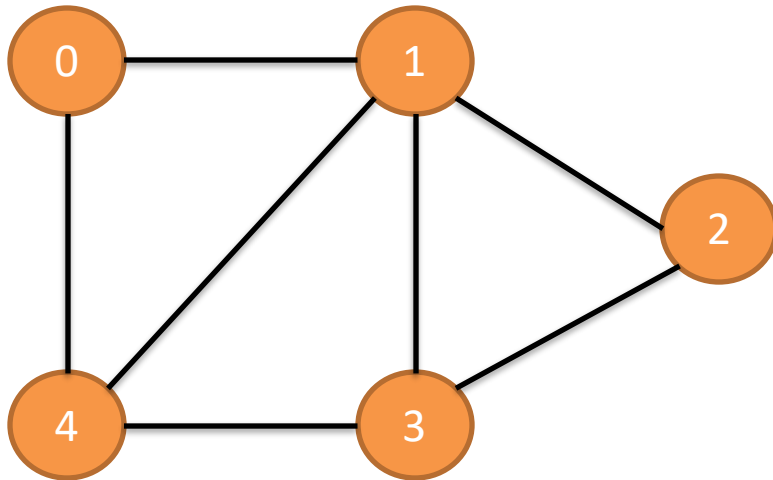
3. Adjacency Matrix

4. Adjacency Map



# Adjacency Lists store adjacent nodes in a List; gives improved performance

## 2. Adjacency List List of Lists

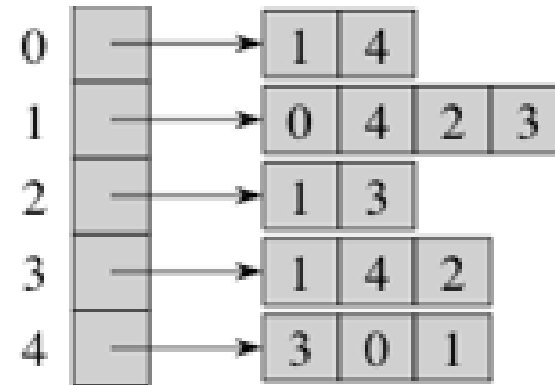


### Assume:

n nodes (here 5)

m edges (here 7)

**Trade  
memory  
for speed**



### Notes:

- Two vertices are said to be *adjacent* if there is an edge between them
- Store List of nodes in or out of each vertex (same if undirected graph)
- Might keep two lists, one for in neighbors and one for out neighbors
- Faster to get neighbors than Edge List, just iterate in  $\theta(\text{degree}(v))$  vs.  $\theta(m)$

# Graphs are commonly represented in one of four different ways

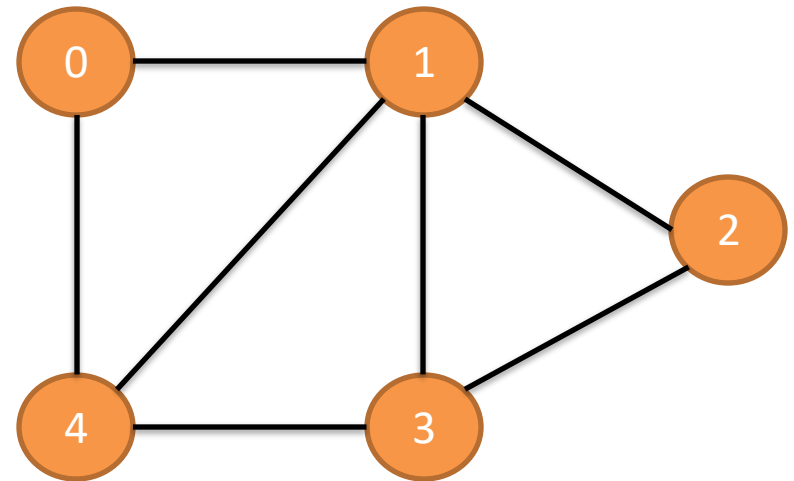
## Common Graph representations

1. Edge List

2. Adjacency List

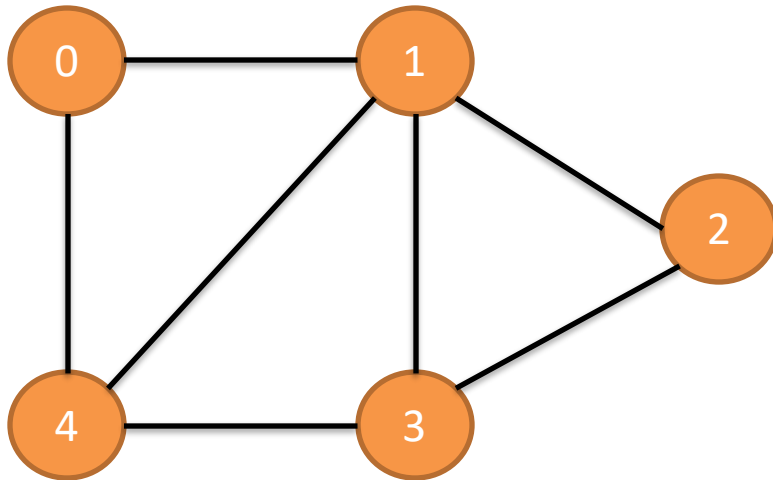
➔ 3. Adjacency Matrix

4. Adjacency Map



# Adjacency Matrices create an $n \times n$ array to indicate existence of edges

## 3. Adjacency Matrix $n \times n$ array



### Assume:

$n$  nodes (here 5)

$m$  edges (here 7)

		To				
		0	1	2	3	4
From	0	0	1	0	0	1
	1	1	0	1	1	1
	2	0	1	0	1	0
	3	0	1	1	0	1
	4	1	1	0	1	0

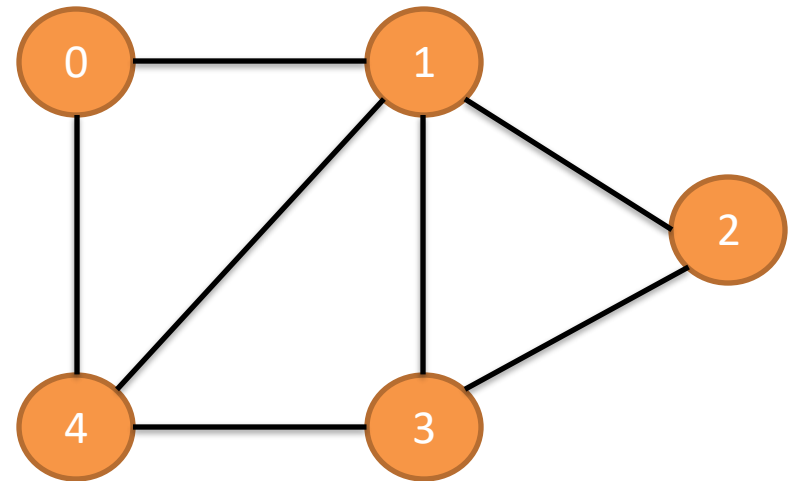
### Notes:

- Create  $n \times n$  matrix  $A$ , set  $A[i,j] = 1$  if edge from node  $i$  to node  $j$ , else 0
- Works if no parallel edges
- Undirected graph  $A[i,j] == A[j,i]$
- `hasEdge(u, v)` is now  $O(1)$ , whereas in Adjacency List it was  $\theta(\text{degree}(u))$
- Finding neighbors now  $\theta(n)$  because have to check entire row or column
- Adding/removing vertices  $\theta(n^2)$ , have to rebuild entire matrix

# Graphs are commonly represented in one of four different ways

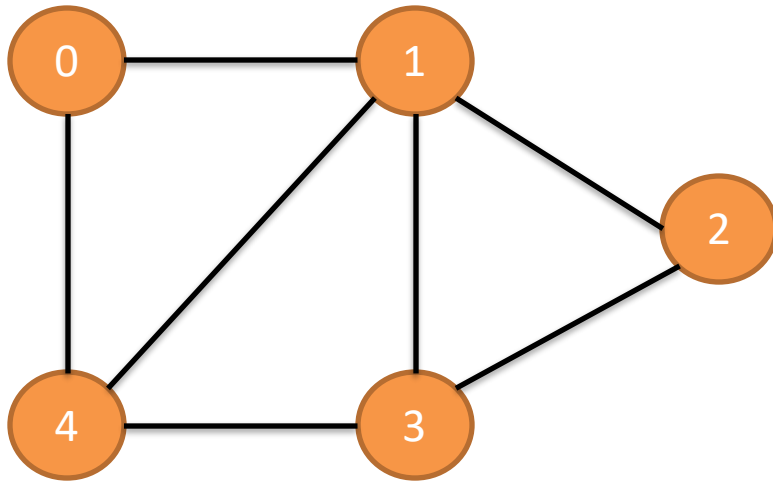
## Common Graph representations

1. Edge List
2. Adjacency List
3. Adjacency Matrix
- ➔ 4. Adjacency Map



# Adjacency Maps create a Map for each node and a second Map to adjacent nodes

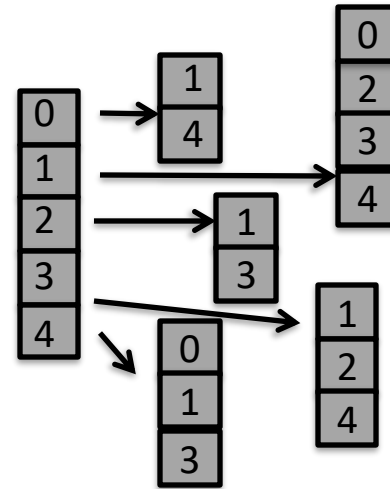
## 4. Adjacency Map Map of Maps



### Assume:

n nodes (here 5)

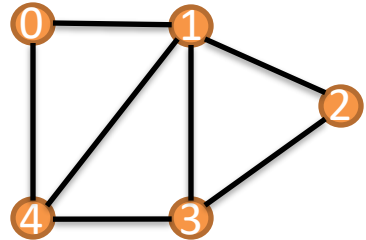
m edges (here 7)



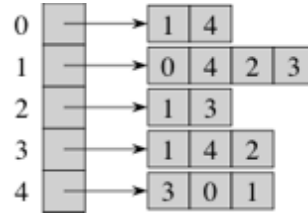
### Notes:

- Create Map with vertex names as Key
- Map Value is a second Map of adjacent vertices with vertex name as Key
- Value in second Map is edge label
- No need to number nodes in order
- `hasEdge(u, v)` now expected  $O(1)$ 
  - Look up  $u$  in Map  $O(1)$
  - Look up  $v$  in second Map  $O(1)$

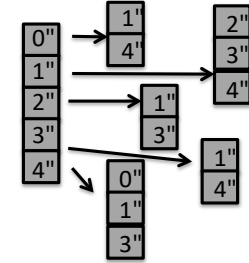
# How a Graph is implemented has a big impact on run-time performance



$\{\{0,1\},$   
 $\{0,4\}, \{1,2\},$   
 $\{1,3\}, \{1,4\},$   
 $\{2,3\}, \{3,4\}\}$



	0	1	2	3	4
0	0	1	0	0	1
1	1	1	0	1	1
2	0	1	0	1	0
3	0	1	1	0	1
4	1	1	0	1	0



Method	Edge List	Adjacency List	Adjacency Matrix	Adjacency Map
<code>in/outDegree(v)</code>	$\theta(m)$	$O(1)$	$\theta(n)$	$O(1)$
<code>in/outNeighbors(v)</code>	$\theta(m)$	$\theta(d_v)$	$\theta(n)$	$\theta(d_v)$
<code>hasEdge(u, v)</code>	$O(m)$	$O(\min(d_u, d_v))$	$O(1)$	$O(1)$
<code>insertVertex(v)</code>	$O(1)$	$O(1)$	$\theta(n^2)$	$O(1)$
<code>removeVertex(v)</code>	$\theta(m)$	$O(d_v)$	$\theta(n^2)$	$\theta(d_v)$
<code>insertEdge(u, v, e)</code>	$O(1)$	$O(1)$	$O(1)$	$O(1)$
<code>removeEdge(u, v)</code>	$\theta(m)$	$O(1)$	$O(1)$	$O(1)$

Best performance is shown in red

$n$  = number of nodes (5),  $m$  = number of edges (7),  $d_v$  = degree of node  $v$

# Agenda

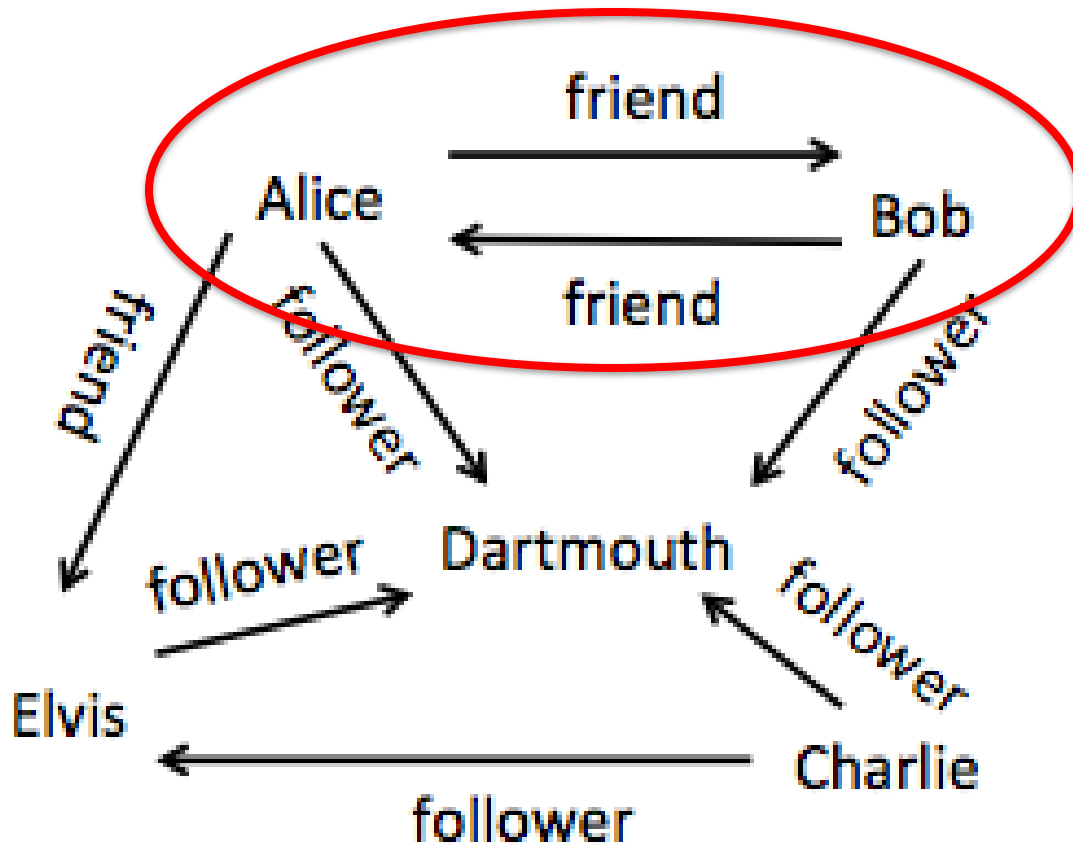
1. Graphs

2. Four common representations

 3. Implementation



# Our implementation will allow a mixed graph (directed and undirected edges)



Undirected edges are two directed edges, one in each direction

# AdjacencyMapGraph.java tracks *in* and *out* edges in two different Maps

## AdjacencyMapGraph.java

```
12 public class AdjacencyMapGraph<V,E> implements Graph<V,E> {
13     protected Map<V, Map<V, E>> out;    // from v1 to v2: { v1 -> { v2 -> edge } }
14     protected Map<V, Map<V, E>> in;    // to v1 from v2: { v1 -> { v2 -> edge } }
15
16     /**
17      * Default constructor, creating an empty graph
18      */
19     public AdjacencyMapGraph() {
20         in = new HashMap<V, Map<V, E>>();
21         out = new HashMap<V, Map<V, E>>();
22     }
23 }
```

**Will normally declare something like:**

```
Graph<String, String> relationships = new AdjacencyMapGraph<String, String>();
```

**Vertices V will be Strings (e.g., someone's name)**

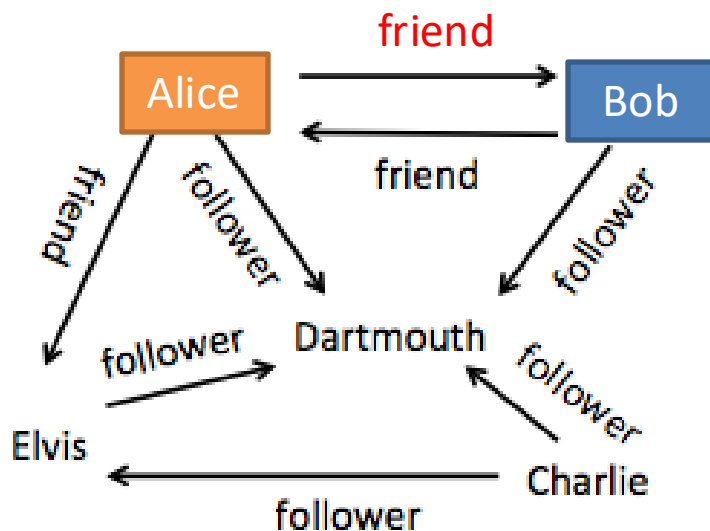
**Edges E will be Strings (e.g., "follows" or "friend")**

# out tracks edges leaving a vertex

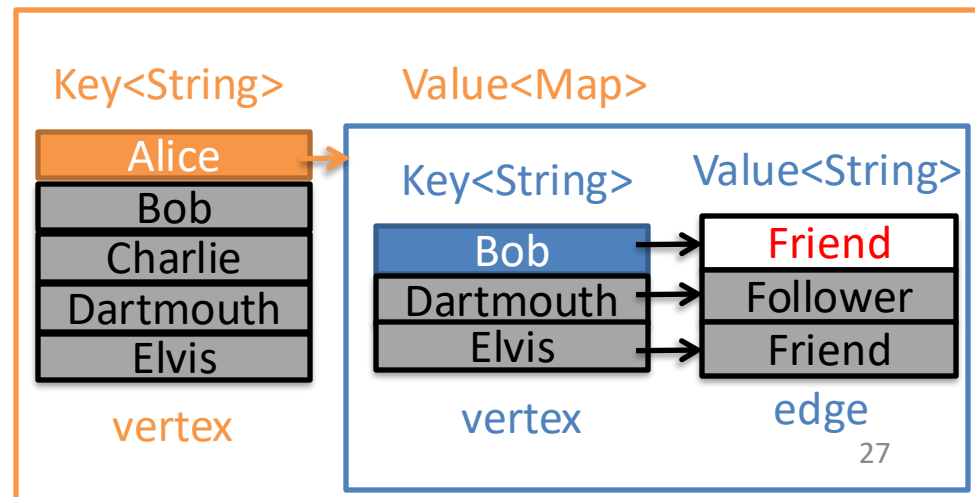
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22     }
23 }
```

- **out tracks edges leaving a vertex**
- **out is a Map with start vertex Key, Map Value**
- **Value Map has end vertex as Key, Edge as Value**



## out

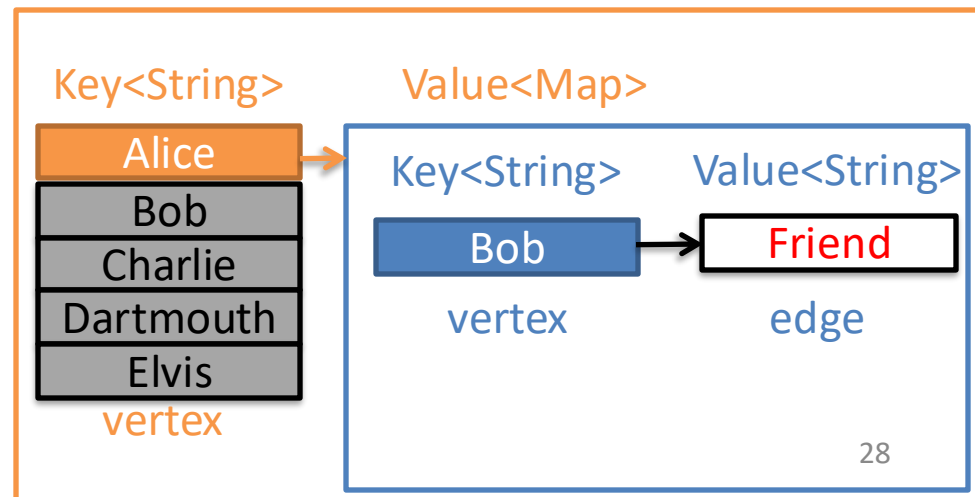
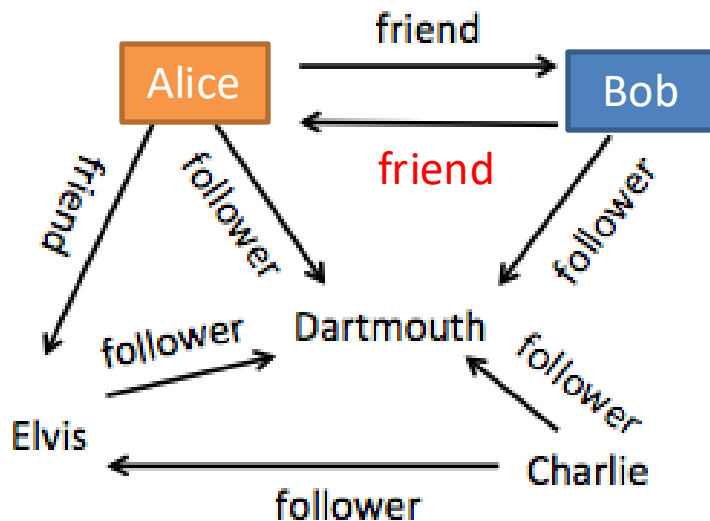


# *in* tracks edges entering a vertex

## AdjacencyMapGraph.java

```
12 public class AdjacencyMapGraph<V,E> implements Graph<V,E> {
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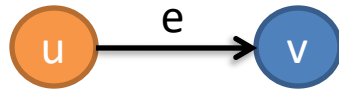
- *in* tracks edges entering a vertex
- *in* is a Map with end vertex Key, Map as Value
- Value Map has start vertex as Key, Edge as Value



# Inserting vertices and edges requires updating both *in* and *out*

## AdjacencyMapGraph.java

```
66
67 public void insertVertex(V v) {
68     if (!out.keySet().contains(v)) {
69         out.put(v, new HashMap<V, E>()); // edges from v
70         in.put(v, new HashMap<V, E>()); // edges to
71     }
72 }
73
74 public void insertDirected(V u, V v, E e) {
75     out.get(u).put(v, e); //out from u to v
76     in.get(v).put(u, e); //reversed for in, from v to u
77 }
78
79 public void insertUndirected(V u, V v, E e) {
80     // insert in both directions
81     insertDirected(u, v, e);
82     insertDirected(v, u, e);
83 }
84
```



- Adding new vertex adds Key to both *in* and *out*
- Value in both cases is set to empty Map (e.g., new vertex has no in or out edges)

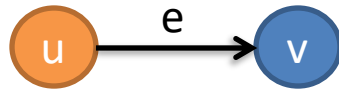
Add directed edge from vertex *u* to vertex *v* with edge label *e*

- Get *out* Value Map using vertex *u* as Key

# Inserting vertices and edges requires updating both *in* and *out*

## AdjacencyMapGraph.java

```
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67 public void insertVertex(V v) {
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```
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```
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- Adding new vertex adds Key to both *in* and *out*
- Value in both cases is set to empty Map (e.g., new vertex has no in or out edges)

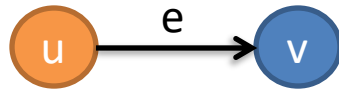
Add directed edge from vertex *u* to vertex *v* with edge label *e*

- Get *out* Value Map using vertex *u* as Key
- Put new entry into Value Map with destination vertex *v* and edge *e*

# Inserting vertices and edges requires updating both *in* and *out*

## AdjacencyMapGraph.java

```
66
67 public void insertVertex(V v) {
68     if (!out.keySet().contains(v)) {
69         out.put(v, new HashMap<V, E>()); // edges from v
70         in.put(v, new HashMap<V, E>()); // edges to
71     }
72 }
```



```
74 public void insertDirected(V u, V v, E e) {
75     out.get(u).put(v, e); //out from u to v
76     in.get(v).put(u, e); //reversed for in, from v to u
77 }
```

```
79 public void insertUndirected(V u, V v, E e) {
80     // insert in both directions
81     insertDirected(u, v, e);
82     insertDirected(v, u, e);
83 }
```

- Adding new vertex adds Key to both *in* and *out*
- Value in both cases is set to empty Map (e.g., new vertex has no in or out edges)

Add directed edge from vertex *u* to vertex *v* with edge label *e*

- Get *out* Value Map using vertex *u* as Key

- Put new entry into Value Map with destination vertex *v* and edge *e*

- Repeat process, updating *in* for incoming edge *e* into *v* from *u*

# We model undirected edges as directed edges going in both directions

## AdjacencyMapGraph.java

```
66
67 public void insertVertex(V v) {
68     if (!out.keySet().contains(v)) {
69         out.put(v, new HashMap<V, E>()); // edges from v
70         in.put(v, new HashMap<V, E>()); // edges to
71     }
72 }
73
74 public void insertDirected(V u, V v, E e) {
75     out.get(u).put(v, e); //out from u to v
76     in.get(v).put(u, e); //reversed for in, from v to u
77 }
78
79 public void insertUndirected(V u, V v, E e) {
80     // insert in both directions
81     insertDirected(u, v, e);
82     insertDirected(v, u, e);
83 }
84
```

**Adding undirected edge creates two directed edges**

- One edge from u to v
- One edge from v to u



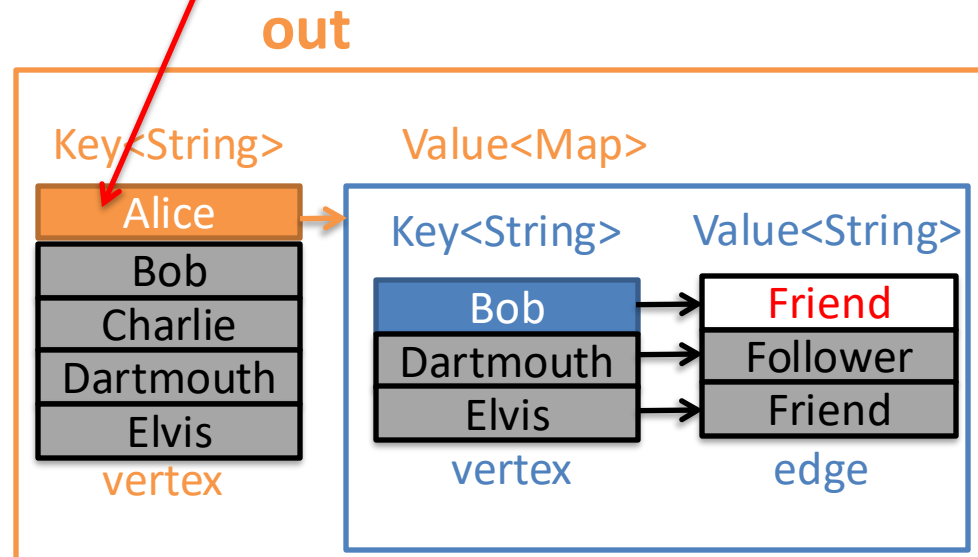
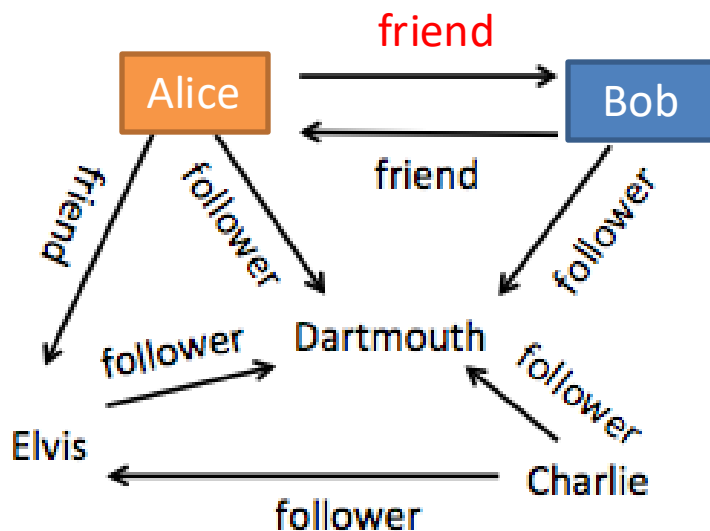


# `getLabel(u,v)` returns the label on the edge between $u$ and $v$

AdjacencyMapGraph.java

```
62  
63 public E getLabel(V u, V v) {  
64     return out.get(u).get(v);  
65 }  
66
```

- `getLabel(u,v)` returns label on edge from  $u$  to  $v$
- `getLabel("Alice", "Bob")` returns "Friend"
- First get Value Map for Key "Alice" from `out`

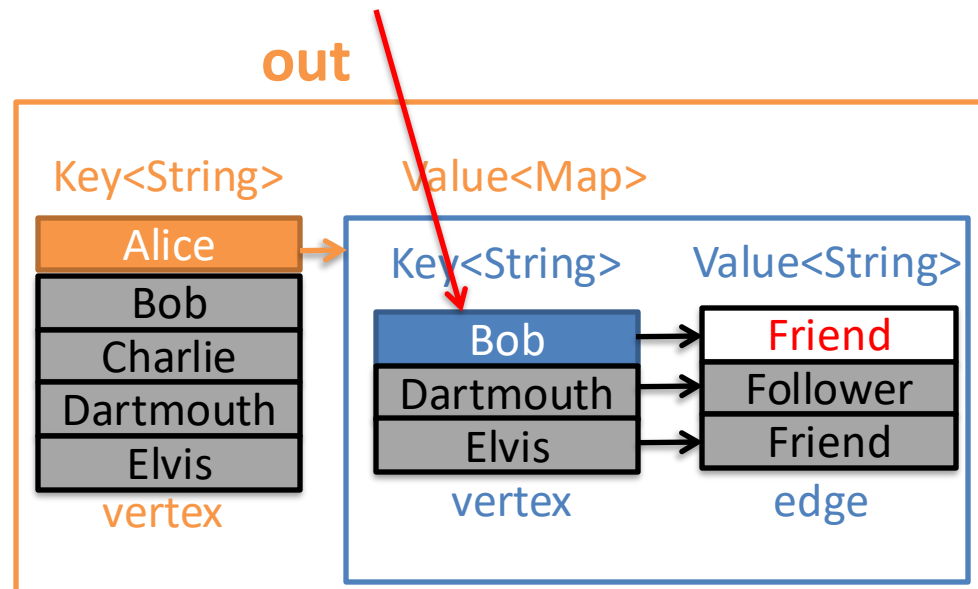
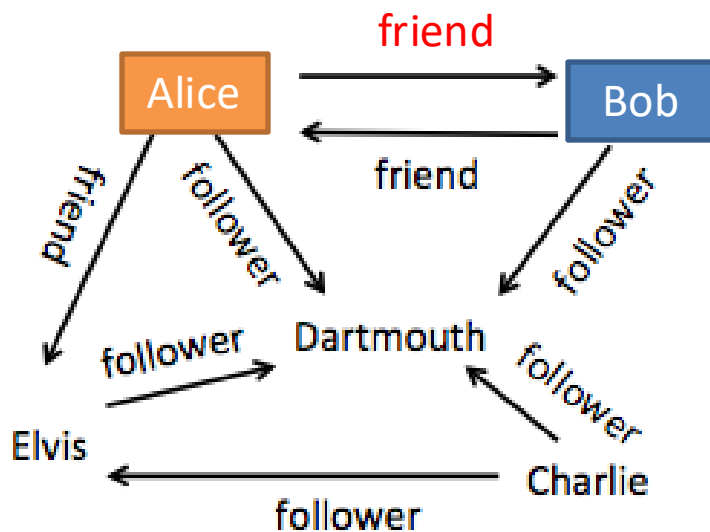


# *getLabel(u,v)* returns the label on the edge between *u* and *v*

## AdjacencyMapGraph.java

```
62  
63 public E getLabel(V u, V v) {  
64     return out.get(u).get(v);  
65 }  
66
```

- *getLabel(u,v)* returns label on edge from *u* to *v*
- *getLabel("Alice","Bob")* returns "Friend"
- First get Value Map for Key "Alice" from *out*
- Next get use Key "Bob" to get Value String

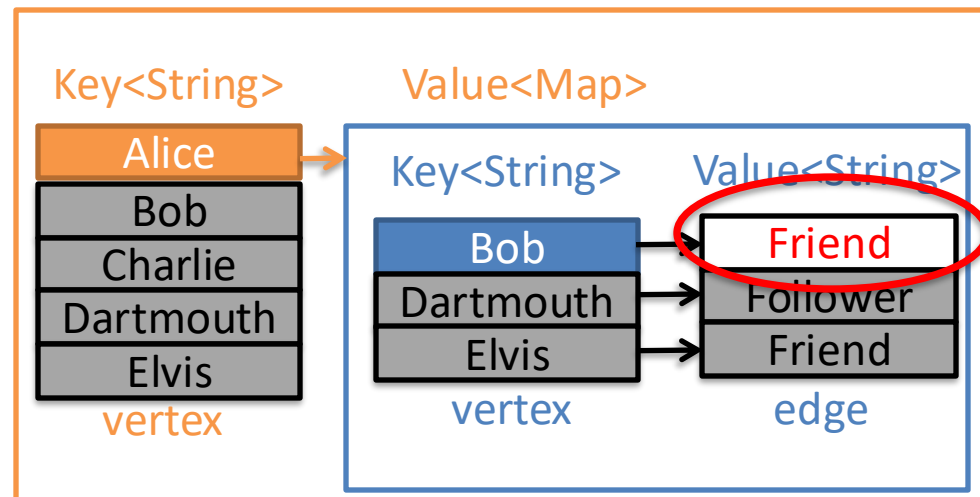
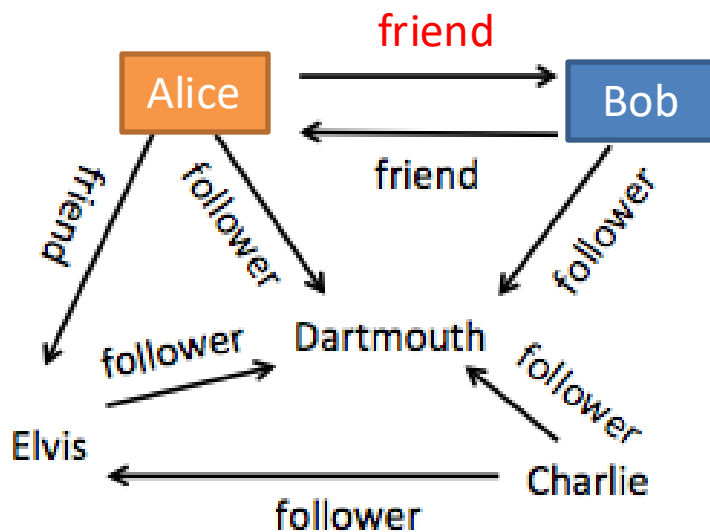


# *getLabel(u,v)* returns the label on the edge between *u* and *v*

## AdjacencyMapGraph.java

```
62  
63 public E getLabel(V u, V v) {  
64     return out.get(u).get(v);  
65 }  
66
```

- *getLabel(u,v)* returns label on edge from *u* to *v*
- *getLabel("Alice","Bob")* returns "Friend"
- First get Value Map for Key "Alice" from *out*
- Next get use Key "Bob" to get Value String
- Return "Friend"



# When removing edges and vertices, must remove from both *in* and *out* Maps

## AdjacencyMapGraph.java

```
0+
△ 85 public void removeVertex(V v) {
86     if (!out.keySet().contains(v)) return;
87     //remove all edges to and from v
88     // remove all in edges to v
89     for (V u : inNeighbors(v)) { // u has an out edge to v
90         out.get(u).remove(v);
91     }
92     //remove all out edges from v
93     for (V w : outNeighbors(v)) { // w has an in edge to v
94         in.get(w).remove(v);
95     }
96     //remove node from outer map
97     in.remove(v);
98     out.remove(v);
99 }
100
△101 public void removeDirected(V u, V v) {
102     //remove edge from u to v in both in and out maps
103     in.get(v).remove(u); //remove from in to v
104     out.get(u).remove(v); //remove from out of u
105 }
106
△107 public void removeUndirected(V u, V v) {
108     // remove in both directions
109     removeDirected(u, v);
110     removeDirected(v, u);
111 }
112
```

### Removing vertex *v*

- Remove all *in* edges (out from neighbor)
- Remove all *out* edges (in from neighbor)
- Then remove *v* from *in* and *out* Maps

```
public Iterable<V> outNeighbors(V v) {
    return out.get(v).keySet();
}

public Iterable<V> inNeighbors(V v) {
    return in.get(v).keySet();
}
```

*Iterable* must have an *iterator* method

- Removing directed edge from *u* to *v*
- Remove from both *in* and *out* Maps
- Removing undirected, call *removeDirected()* twice

# RelationshipTest.java: create graph with both directed and non-directed edges

## RelationshipTest.java

```
4 public class RelationshipsTest {
5     public static void main(String [] args) {
6         Graph<String, String> relationships = new AdjacencyMapGraph
7
8         relationships.insertVertex("Alice");
9         relationships.insertVertex("Bob");
10        relationships.insertVertex("Charlie");
11        relationships.insertVertex("Dartmouth");
12        relationships.insertVertex("Elvis");
13        relationships.insertDirected("Alice", "Dartmouth", "follow
14        relationships.insertDirected("Bob", "Dartmouth", "follower
15        relationships.insertDirected("Charlie", "Dartmouth", "foll
16        relationships.insertDirected("Elvis", "Dartmouth", "follower");
17        relationships.insertUndirected("Alice", "Bob", "friend"); // symmetric, undirected edge
18        relationships.insertDirected("Alice", "Elvis", "friend"); // not symmetric, directed e
19        relationships.insertDirected("Charlie", "Elvis", "follower");
20
21        System.out.println("The graph:");
22        System.out.println(relationships);
23    }
```

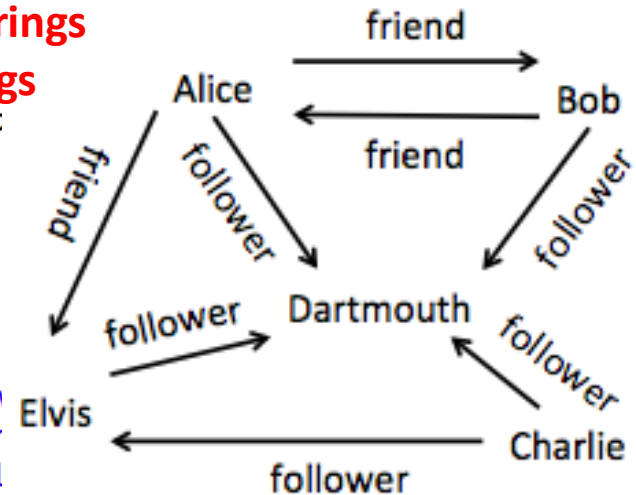
Declare graph:

Vertices V are Strings

Edges E are Strings

Add nodes

Add edges



**Output (from implicit toString() call):**

The graph:

Vertices: [Bob, Dartmouth, Alice, Elvis, Charlie]

Out edges: {Bob={Dartmouth=follower, Alice=friend}, Dartmouth={},

Alice={Dartmouth=follower, Bob=friend, Elvis=friend}, Elvis={Dartmouth=follower},

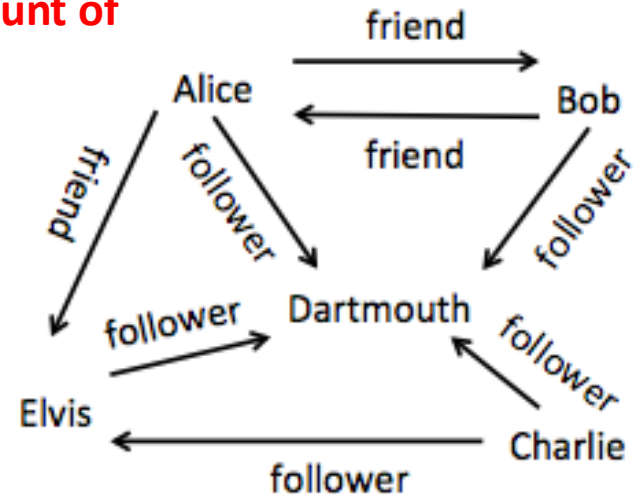
Charlie={Dartmouth=follower, Elvis=follower}}

# RelationshipTest.java: create graph with both directed and non-directed edges

## RelationshipTest.java

```
21 System.out.println("The graph:");
22 System.out.println(relationships);
23
24 System.out.println("\nLinks to Dartmouth = " + relationships.inDegree("Dartmouth"));
25
26 System.out.println("\nLinks from Alice:");
27 for (String to : relationships.outNeighbors("Alice"))
28     System.out.println(to + " (" + relationships.getLabel("Alice", to) + ")");
29
30 System.out.println("\nLinks to Dartmouth:");
31 for (String from : relationships.inNeighbors("Dartmouth"))
32     System.out.println(from + " (" + relationships.getLabel(from, "Dartmouth") + ")");
33
34 System.out.println("\nElvis has left the building");
35 relationships.removeVertex("Elvis");
36 System.out.println("\nLinks from Alice:");
37 for (String to : relationships.outNeighbors("Alice"))
38     System.out.println(to + " (" + relationships.getLabel("Alice", to) + ")");
39
40 System.out.println("\nAlice & Charlie work together");
41 relationships.insertUndirected("Alice", "Charlie", "co-worker");
42 System.out.println("\nLinks from Alice:");
43 for (String to : relationships.outNeighbors("Alice"))
44     System.out.println(to + " (" + relationships.getLabel("Alice", to) + ")");
45 System.out.println("\nLinks from Charlie:");
46 for (String to : relationships.outNeighbors("Charlie"))
47     System.out.println(to + " (" + relationships.getLabel("Charlie", to) + ")");
48
49 System.out.println("\nAlice unfriended Bob");
50 relationships.removeDirected("Alice", "Bob");
51 System.out.println("and Charlie gets fired");
52 relationships.removeUndirected("Alice", "Charlie");
53 System.out.println("\nLinks from Alice:");
54 for (String to : relationships.outNeighbors("Alice"))
55     System.out.println(to + " (" + relationships.getLabel("Alice", to) + ")");
56
57 System.out.println("\nThe final graph:");
58 System.out.println(relationships);
```

- ***inDegree(u)* gives count of edges coming into u**



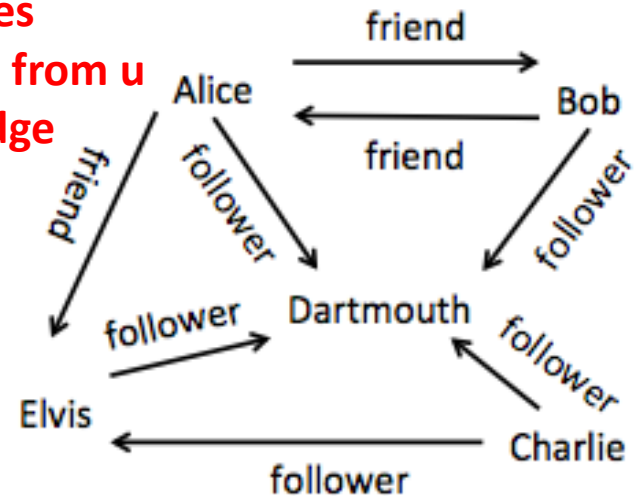
**Output:**  
Links to Dartmouth = 4

# RelationshipTest.java: create graph with both directed and non-directed edges

## RelationshipTest.java

```
21 System.out.println("The graph:");
22 System.out.println(relationships);
23
24 System.out.println("\nLinks to Dartmouth = " + relationships.inDegree("Dartmouth"));
25
26 System.out.println("\nLinks from Alice:");
27 for (String to : relationships.outNeighbors("Alice"))
28     System.out.println(to + " (" + relationships.getLabel("Alice", to) + ")");
29
30 System.out.println("\nLinks to Dartmouth:");
31 for (String from : relationships.inNeighbors("Dartmouth"))
32     System.out.println(from + " (" + relationships.getLabel(from, "Dartmouth") + ")");
33
34 System.out.println("\nElvis has left the building");
35 relationships.removeVertex("Elvis");
36 System.out.println("\nLinks from Alice:");
37 for (String to : relationships.outNeighbors("Alice"))
38     System.out.println(to + " (" + relationships.getLabel("Alice", to) + ")");
39
40 System.out.println("\nAlice & Charlie work together");
41 relationships.insertUndirected("Alice", "Charlie", "co-worker");
42 System.out.println("\nLinks from Alice:");
43 for (String to : relationships.outNeighbors("Alice"))
44     System.out.println(to + " (" + relationships.getLabel("Alice", to) + ")");
45 System.out.println("\nLinks from Charlie:");
46 for (String to : relationships.outNeighbors("Charlie"))
47     System.out.println(to + " (" + relationships.getLabel("Charlie", to) + ")");
48
49 System.out.println("\nAlice unfriended Bob");
50 relationships.removeDirected("Alice", "Bob");
51 System.out.println("and Charlie gets fired");
52 relationships.removeUndirected("Alice", "Charlie");
53 System.out.println("\nLinks from Alice:");
54 for (String to : relationships.outNeighbors("Alice"))
55     System.out.println(to + " (" + relationships.getLabel("Alice", to) + ")");
56
57 System.out.println("\nThe final graph:");
58 System.out.println(relationships);
```

- **outNeighbors(u)** gives neighboring vertices from u
- **getLabel(u,v)** gets edge label from u to v



## Output:

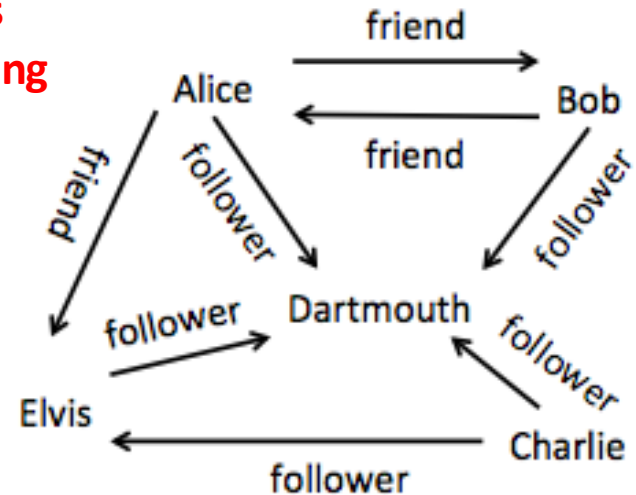
Links from Alice:  
Dartmouth (follower)  
Bob (friend)  
Elvis (friend)

# RelationshipTest.java: create graph with both directed and non-directed edges

## RelationshipTest.java

```
21 System.out.println("The graph:");
22 System.out.println(relationships);
23
24 System.out.println("\nLinks to Dartmouth = " + relationships.inDegree("Dartmouth"));
25
26 System.out.println("\nLinks from Alice:");
27 for (String to : relationships.outNeighbors("Alice"))
28     System.out.println(to + " (" + relationships.getLabel("Alice", to) + ")");
29
30 System.out.println("\nLinks to Dartmouth:");
31 for (String from : relationships.inNeighbors("Dartmouth"))
32     System.out.println(from + " (" + relationships.getLabel(from, "Dartmouth") + ")");
33
34 System.out.println("\nElvis has left the building");
35 relationships.removeVertex("Elvis");
36 System.out.println("\nLinks from Alice:");
37 for (String to : relationships.outNeighbors("Alice"))
38     System.out.println(to + " (" + relationships.getLabel("Alice", to) + ")");
39
40 System.out.println("\nAlice & Charlie work together");
41 relationships.insertUndirected("Alice", "Charlie", "co-worker");
42 System.out.println("\nLinks from Alice:");
43 for (String to : relationships.outNeighbors("Alice"))
44     System.out.println(to + " (" + relationships.getLabel("Alice", to) + ")");
45 System.out.println("\nLinks from Charlie:");
46 for (String to : relationships.outNeighbors("Charlie"))
47     System.out.println(to + " (" + relationships.getLabel("Charlie", to) + ")");
48
49 System.out.println("\nAlice unfriended Bob");
50 relationships.removeDirected("Alice", "Bob");
51 System.out.println("and Charlie gets fired");
52 relationships.removeUndirected("Alice", "Charlie");
53 System.out.println("\nLinks from Alice:");
54 for (String to : relationships.outNeighbors("Alice"))
55     System.out.println(to + " (" + relationships.getLabel("Alice", to) + ")");
56
57 System.out.println("\nThe final graph:");
58 System.out.println(relationships);
```

- ***inNeighbors(u)* gives neighbors on incoming edges**



### Output:

Links to Dartmouth:

Bob (follower)

Alice (follower)

Elvis (follower)

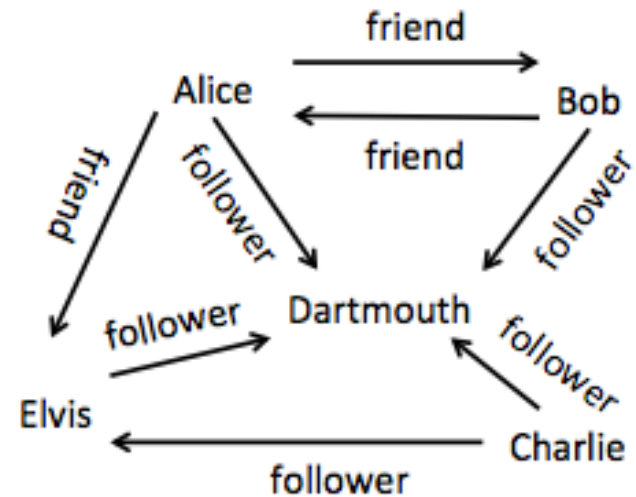
Charlie (follower)



# RelationshipTest.java: create graph with both directed and non-directed edges

## RelationshipTest.java

```
21 System.out.println("The graph:");
22 System.out.println(relationships);
23
24 System.out.println("\nLinks to Dartmouth = " + relationships.inDegree("Dartmouth"));
25
26 System.out.println("\nLinks from Alice:");
27 for (String to : relationships.outNeighbors("Alice"))
28     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
29
30 System.out.println("\nLinks to Dartmouth:");
31 for (String from : relationships.inNeighbors("Dartmouth"))
32     System.out.println(from + " (" +relationships.getLabel(from, "Dartmouth")+")");
33
34 System.out.println("\nElvis has left the building"); Removing node Elvis
35 relationships.removeVertex("Elvis"); also removes link from
36 System.out.println("\nLinks from Alice:"); Alice and others
37 for (String to : relationships.outNeighbors("Alice"))
38     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
39
40 System.out.println("\nAlice & Charlie work together");
41 relationships.insertUndirected("Alice", "Charlie", "co-worker");
42 System.out.println("\nLinks from Alice:");
43 for (String to : relationships.outNeighbors("Alice"))
44     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
45 System.out.println("\nLinks from Charlie:");
46 for (String to : relationships.outNeighbors("Charlie"))
47     System.out.println(to + " (" +relationships.getLabel("Charlie", to)+")");
48
49 System.out.println("\nAlice unfriended Bob");
50 relationships.removeDirected("Alice", "Bob");
51 System.out.println("and Charlie gets fired");
52 relationships.removeUndirected("Alice", "Charlie");
53 System.out.println("\nLinks from Alice:");
54 for (String to : relationships.outNeighbors("Alice"))
55     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
56
57 System.out.println("\nThe final graph:");
58 System.out.println(relationships);
```

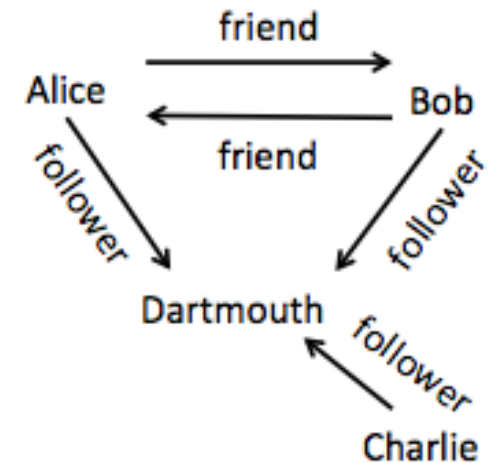


# RelationshipTest.java: create graph with both directed and non-directed edges

## RelationshipTest.java

```
21 System.out.println("The graph:");
22 System.out.println(relationships);
23
24 System.out.println("\nLinks to Dartmouth = " + relationships.inDegree("Dartmouth"));
25
26 System.out.println("\nLinks from Alice:");
27 for (String to : relationships.outNeighbors("Alice"))
28     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
29
30 System.out.println("\nLinks to Dartmouth:");
31 for (String from : relationships.inNeighbors("Dartmouth"))
32     System.out.println(from + " (" +relationships.getLabel(from, "Dartmouth")+")");
33
34 System.out.println("\nElvis has left the building");
35 relationships.removeVertex("Elvis");
36 System.out.println("\nLinks from Alice:");
37 for (String to : relationships.outNeighbors("Alice"))
38     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
39
40 System.out.println("\nAlice & Charlie work together");
41 relationships.insertUndirected("Alice", "Charlie", "co-worker");
42 System.out.println("\nLinks from Alice:");
43 for (String to : relationships.outNeighbors("Alice"))
44     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
45 System.out.println("\nLinks from Charlie:");
46 for (String to : relationships.outNeighbors("Charlie"))
47     System.out.println(to + " (" +relationships.getLabel("Charlie", to)+")");
48
49 System.out.println("\nAlice unfriended Bob");
50 relationships.removeDirected("Alice", "Bob");
51 System.out.println("and Charlie gets fired");
52 relationships.removeUndirected("Alice", "Charlie");
53 System.out.println("\nLinks from Alice:");
54 for (String to : relationships.outNeighbors("Alice"))
55     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
56
57 System.out.println("\nThe final graph:");
58 System.out.println(relationships);
```

**Removing node Elvis  
also removes link from  
Alice and others**



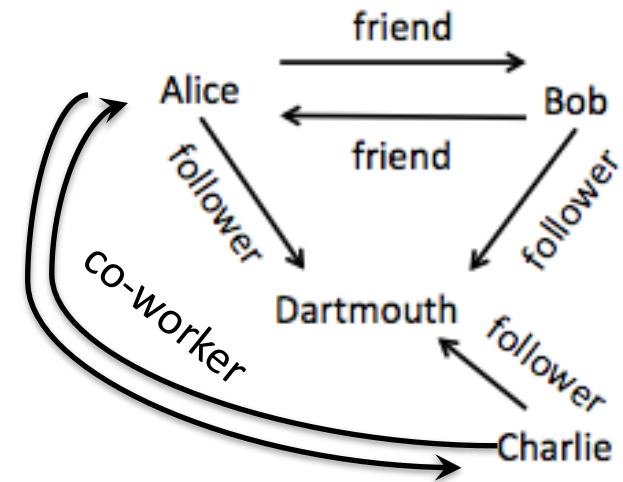
**Output:**  
Links from Alice:  
Dartmouth (follower)  
Bob (friend)

# RelationshipTest.java: create graph with both directed and non-directed edges

## RelationshipTest.java

```
21 System.out.println("The graph:");
22 System.out.println(relationships);
23
24 System.out.println("\nLinks to Dartmouth = " + relationships.inDegree("Dartmouth"));
25
26 System.out.println("\nLinks from Alice:");
27 for (String to : relationships.outNeighbors("Alice"))
28     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
29
30 System.out.println("\nLinks to Dartmouth:");
31 for (String from : relationships.inNeighbors("Dartmouth"))
32     System.out.println(from + " (" +relationships.getLabel(from, "Dartmouth")+")");
33
34 System.out.println("\nElvis has left the building");
35 relationships.removeVertex("Elvis");
36 System.out.println("\nLinks from Alice:");
37 for (String to : relationships.outNeighbors("Alice"))
38     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
39
40 System.out.println("\nAlice & Charlie work together");
41 relationships.insertUndirected("Alice", "Charlie", "co-worker");
42 System.out.println("\nLinks from Alice:");
43 for (String to : relationships.outNeighbors("Alice"))
44     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
45 System.out.println("\nLinks from Charlie:");
46 for (String to : relationships.outNeighbors("Charlie"))
47     System.out.println(to + " (" +relationships.getLabel("Charlie", to)+")");
48
49 System.out.println("\nAlice unfriended Bob");
50 relationships.removeDirected("Alice", "Bob");
51 System.out.println("and Charlie gets fired");
52 relationships.removeUndirected("Alice", "Charlie");
53 System.out.println("\nLinks from Alice:");
54 for (String to : relationships.outNeighbors("Alice"))
55     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
56
57 System.out.println("\nThe final graph:");
58 System.out.println(relationships);
```

**Adding link between Charlie and Alice**



**Output:**  
Alice & Charlie work together

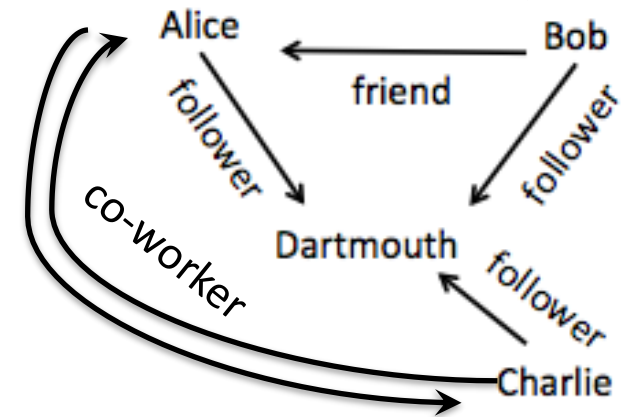
Links from Alice:  
Dartmouth (follower)  
Bob (friend)  
Charlie (co-worker)

Links from Charlie:  
Dartmouth (follower)  
Alice (co-worker)

# RelationshipTest.java: create graph with both directed and non-directed edges

## RelationshipTest.java

```
21 System.out.println("The graph:");
22 System.out.println(relationships);
23
24 System.out.println("\nLinks to Dartmouth = " + relationships.inDegree("Dartmouth"));
25
26 System.out.println("\nLinks from Alice:");
27 for (String to : relationships.outNeighbors("Alice"))
28     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
29
30 System.out.println("\nLinks to Dartmouth:");
31 for (String from : relationships.inNeighbors("Dartmouth"))
32     System.out.println(from + " (" +relationships.getLabel(from, "Dartmouth")+")");
33
34 System.out.println("\nElvis has left the building"); Alice removes edge to
35 relationships.removeVertex("Elvis"); Bob
36 System.out.println("\nLinks from Alice:");
37 for (String to : relationships.outNeighbors("Alice"))
38     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
39
40 System.out.println("\nAlice & Charlie work together");
41 relationships.insertUndirected("Alice", "Charlie", "co-worker");
42 System.out.println("\nLinks from Alice:");
43 for (String to : relationships.outNeighbors("Alice"))
44     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
45 System.out.println("\nLinks from Charlie:");
46 for (String to : relationships.outNeighbors("Charlie"))
47     System.out.println(to + " (" +relationships.getLabel("Charlie", to)+")");
48
49 System.out.println("\nAlice unfriends Bob"); And Charlie no
50 relationships.removeDirected("Alice", "Bob"); longer co-
51 System.out.println("\nand Charlie gets fired"); worker
52 relationships.removeUndirected("Alice", "Charlie");
53 System.out.println("\nLinks from Alice:");
54 for (String to : relationships.outNeighbors("Alice"))
55     System.out.println(to + " (" +relationships.getLabel("Alice", to)+")");
56
57 System.out.println("\nBlue final graph:");
58 System.out.println(relationships);
```



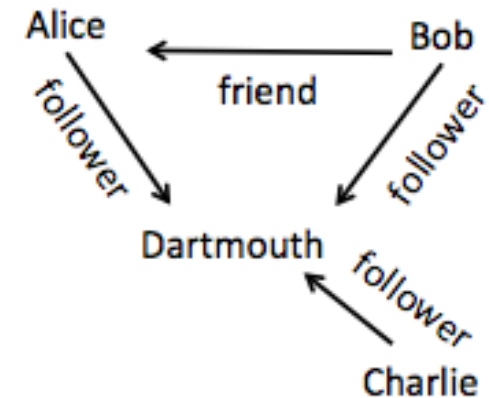
**Output:**  
Alice unfriends Bob  
and Charlie gets fired

Links from Alice:  
Dartmouth (follower)

# RelationshipTest.java: create graph with both directed and non-directed edges

## RelationshipTest.java

```
21 System.out.println("The graph:");
22 System.out.println(relationships);
23
24 System.out.println("\nLinks to Dartmouth = " + relationships.inDegree("Dartmouth"));
25
26 System.out.println("\nLinks from Alice:");
27 for (String to : relationships.outNeighbors("Alice"))
28     System.out.println(to + " (" +relationships.getLabel("Alice", to)+)");
29
30 System.out.println("\nLinks to Dartmouth:");
31 for (String from : relationships.inNeighbors("Dartmouth"))
32     System.out.println(from + " (" +relationships.getLabel(from, "Dartmouth")+)");
33
34 System.out.println("\nElvis has left the building");
35 relationships.removeVertex("Elvis");
36 System.out.println("\nLinks from Alice:");
37 for (String to : relationships.outNeighbors("Alice"))
38     System.out.println(to + " (" +relationships.getLabel("Alice", to)+)");
39
40 System.out.println("\nAlice & Charlie work together");
41 relationships.insertUndirected("Alice", "Charlie", "co-worker");
42 System.out.println("\nLinks from Alice:");
43 for (String to : relationships.outNeighbors("Alice"))
44     System.out.println(to + " (" +relationships.getLabel("Alice", to)+)");
45 System.out.println("\nLinks from Charlie:");
46 for (String to : relationships.outNeighbors("Charlie"))
47     System.out.println(to + " (" +relationships.getLabel("Charlie", to)+)");
48
49 System.out.println("\nAlice unfriended Bob");
50 relationships.removeDirected("Alice", "Bob");
51 System.out.println("and Charlie gets fired");
52 relationships.removeUndirected("Alice", "Charlie");
53 System.out.println("\nLinks from Alice:");
54 for (String to : relationships.outNeighbors("Alice"))
55     System.out.println(to + " (" +relationships.getLabel("Alice", to)+)");
56
57 System.out.println("\nThe final graph:");
58 System.out.println(relationships);
```



### Output:

The final graph:

Vertices: [Bob, Dartmouth, Alice, Charlie]

Out edges: {Bob={Dartmouth=follower, Alice=friend}, Dartmouth={}

Alice={Dartmouth=follower},Charlie={Dartmouth=follower}}

