


CS 10:

Problem solving via Object Oriented Programming

Graph Traversals

Agenda

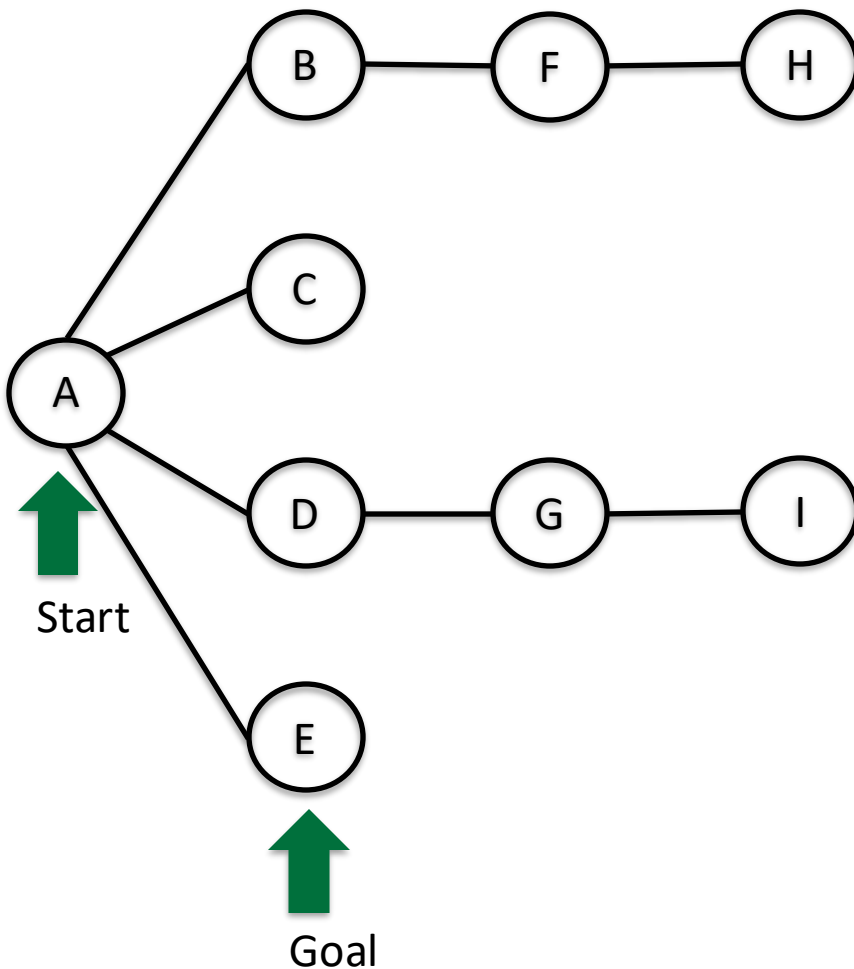
- 
1. Depth first search (DFS)
 2. Breadth first search (BFS)
 3. Examples from last class and today

Graph traversals are useful to answer questions about relationships

Some Graph traversals uses

- Uses are often around *reachability*
- Computing *path* from vertex u to vertex v
- Given start vertex s on Graph G , compute a path with the minimum number of edges between s and all other vertices (or report no such path exists)
- Testing whether G is fully connected (e.g., all vertices reachable)
- Identifying *cycles* in G (or reporting no cycle exists)
- Today's examples have ~~no~~ few cycles (cycles next class)

Depth First Search (DFS) uses a stack to explore as if in a maze



Goal: compute path from *start to goal (or to all other nodes)*

DFS basic idea

- Keep going until you can't go any further, then back track
- Relies on a **Stack** (implicit or explicit) to keep track of where you've been

Some of you did Depth First Search on Problem Set 1

RegionFinder pseudo code

```
Loop over all the pixels
  If a pixel is unvisited and of the correct color
    Start a new region
    Keep track of pixels need to be visited, initially just one
    As long as there's some pixel that needs to be visited
      Get one to visit
      Add it to the region
      Mark it as visited
      Loop over all its neighbors
        If the neighbor is of the correct color
          Add it to the list of pixels to be visited
    If the region is big enough to be worth keeping, do so
```

Some of you did Depth First Search on Problem Set 1

RegionFinder pseudo code

```
Loop over all the pixels
  If a pixel is unvisited and of the correct color
    Start a new region
    Keep track of pixels need to be visited, initially just one
    As long as there's some pixel that needs to be visited
      Get one to visit
      Add it to the region
      Mark it as visited
      Loop over all its neighbors
        If the neighbor is of the correct color
          Add it to the list of pixels to be visited
    If the region is big enough to be worth keeping, do so
```

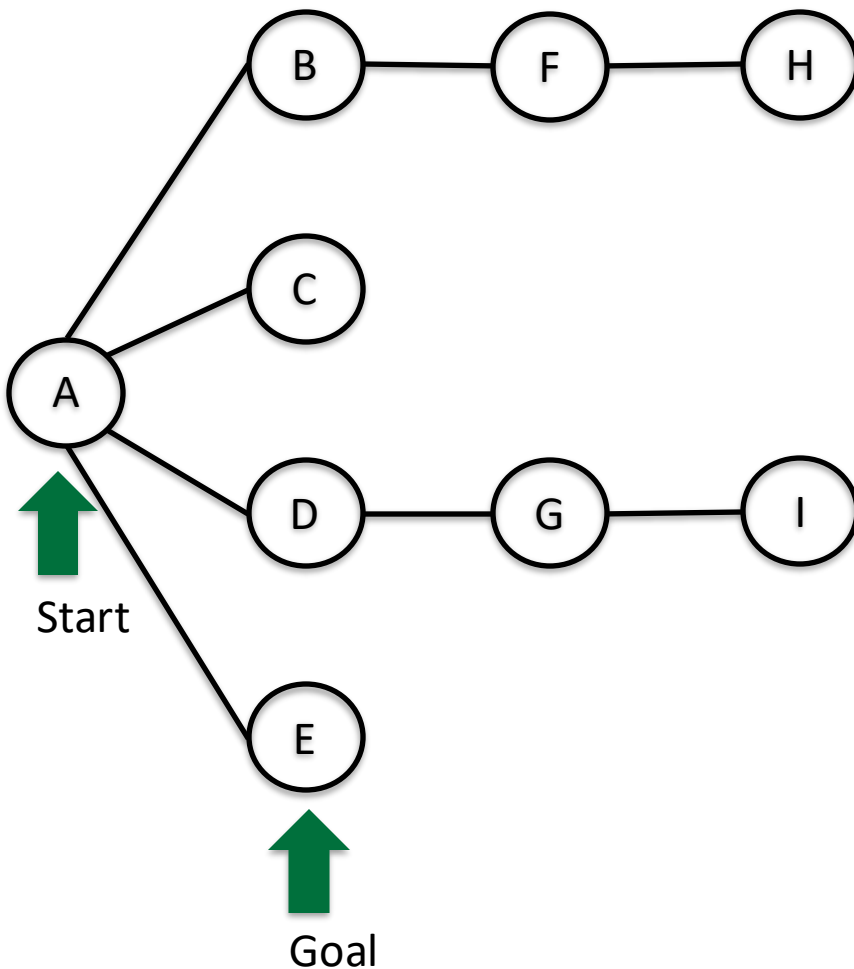
If you added to end of list...

Some of you did Depth First Search on Problem Set 1

RegionFinder pseudo code

```
Loop over all the pixels
  If a pixel is unvisited and of the correct color
    Start a new region
    Keep track of pixels need to be visited, initially just one
    As long as there's some pixel that needs to be visited
      Get one to visit ← And if you get a pixel from end
      Add it to the region      of list, you implemented a stack
      Mark it as visited
      Loop over all its neighbors
        If the neighbor is of the correct color
          Add it to the list of pixels to be visited
    If the region is big enough to be worth keeping, do so
      ↑
      If you added to end of list...
```

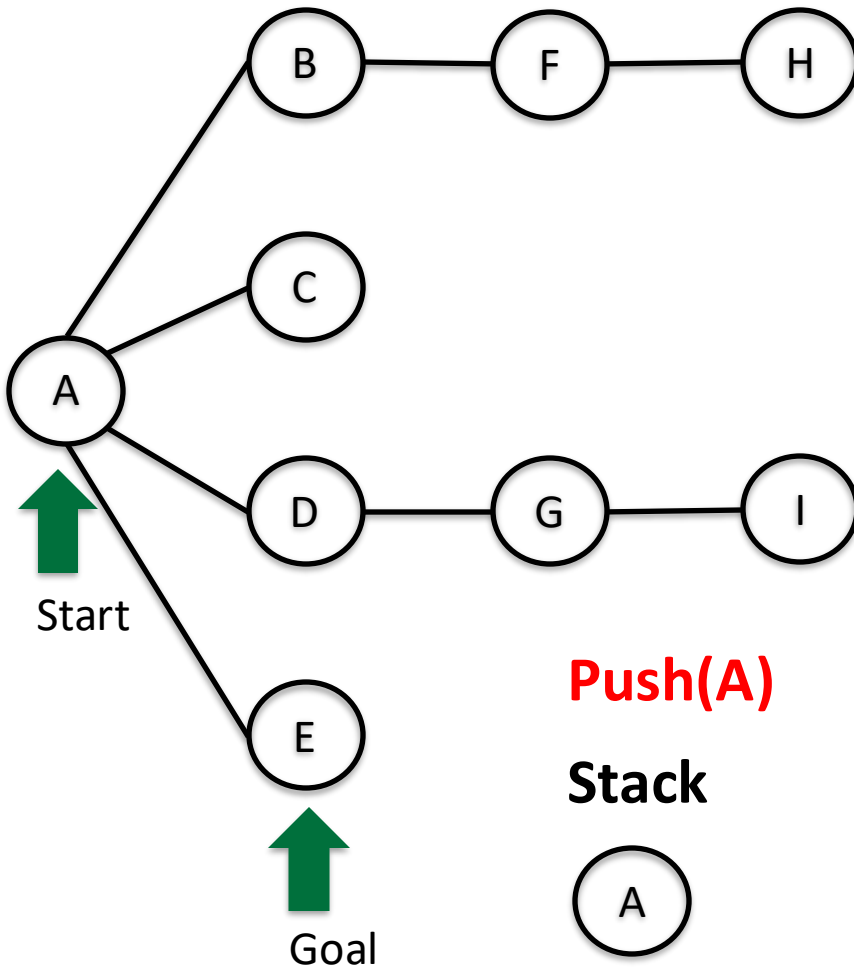
Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



DFS algorithm

```
stack.push(s) //start node
repeat until find goal vertex or
stack empty:
    u = stack.pop()
    if !u.visited
        u.visited = true
        (do something while here)
        for v ∈ u.adjacent
            if !v.visited
                stack.push(v)
```


Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



DFS algorithm

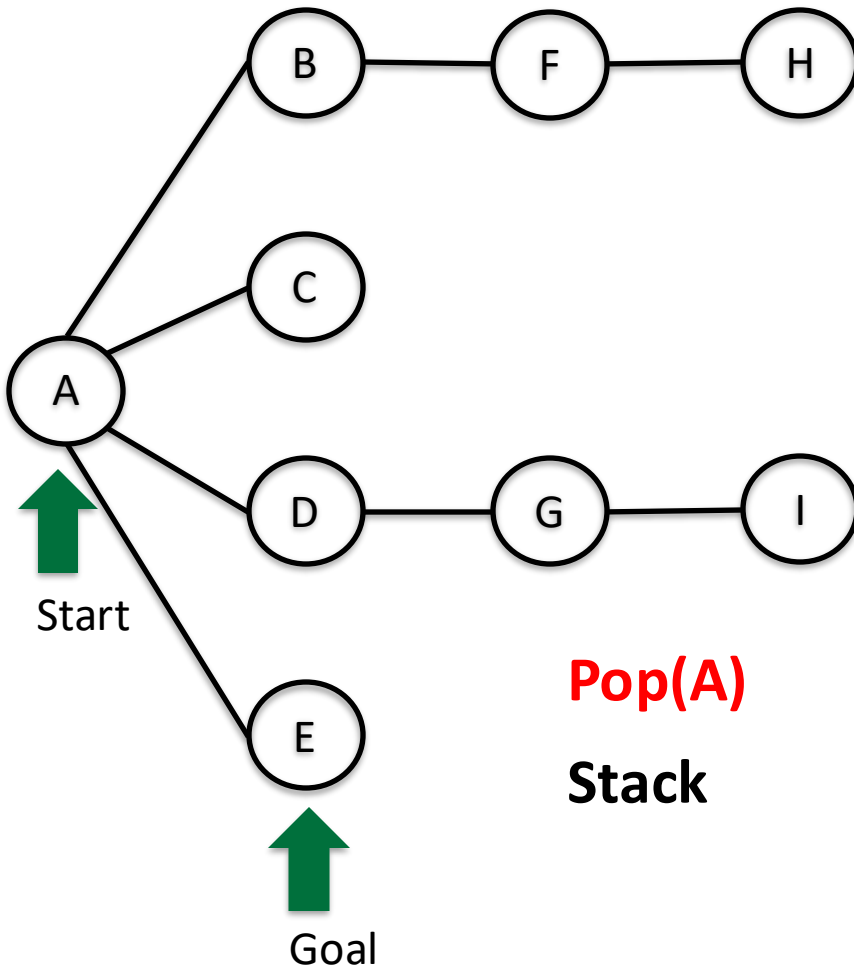
```
→ stack.push(s) //start node
repeat until find goal vertex or
stack empty:
    u = stack.pop()
    if !u.visited
        u.visited = true
        (do something while here)
        for v ∈ u.adjacent
            if !v.visited
                stack.push(v)
```

Push(A)

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)

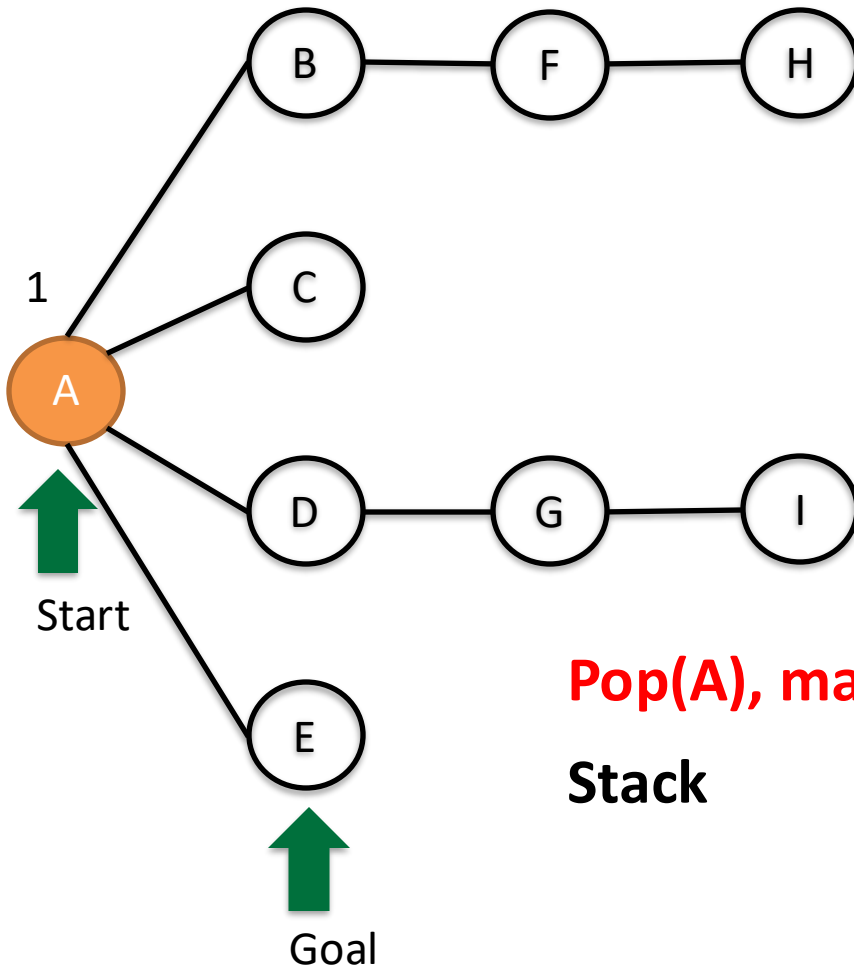


DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

```
→ u = stack.pop()  
  if !u.visited  
    u.visited = true  
    (do something while here)  
    for v ∈ u.adjacent  
      if !v.visited  
        stack.push(v)
```

Depth First Search (DFS) finds a path between *start* and other nodes (if exists)

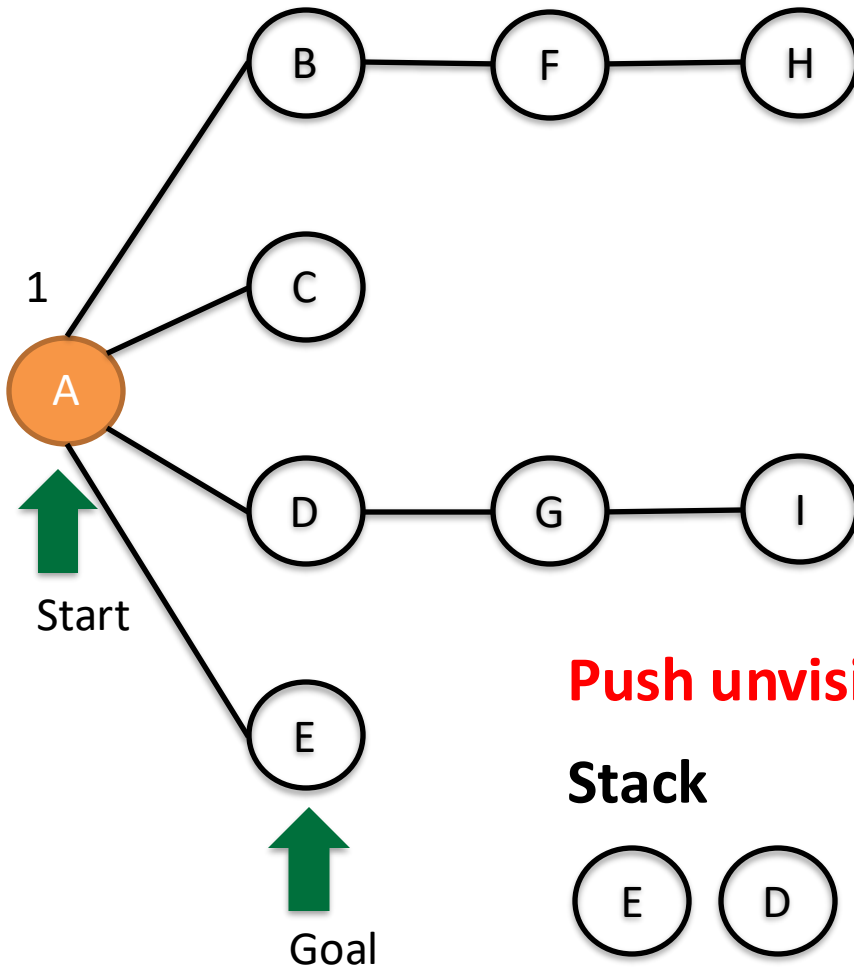


DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

```
    u = stack.pop()  
    if !u.visited  
        Visit the node  
        u.visited = true  
        (do something while here)  
        for v ∈ u.adjacent  
            if !v.visited  
                stack.push(v)
```

Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

```
    u = stack.pop()
```

```
    if !u.visited
```

```
        u.visited = true
```

```
        (do something while here)
```

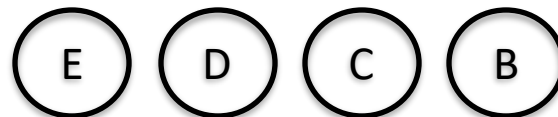
```
        for v ∈ u.adjacent
```

```
            if !v.visited
```

```
                stack.push(v)
```

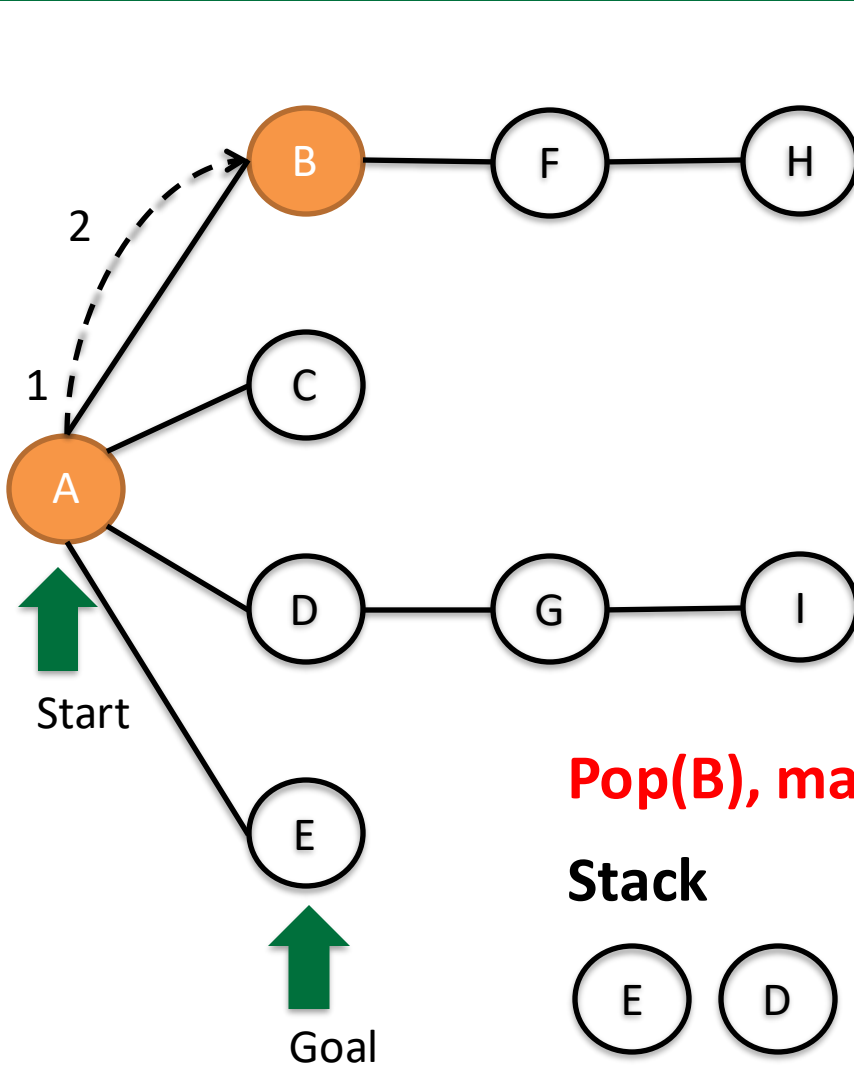
Push unvisited adjacent

Stack



- What method would we use on our `AdjacencyMapGraph`?
- `graph.outNeighbors(u)`
- Order pushed onto stack depends on order of nodes from `outNeighbors` iterator

Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



DFS algorithm

```
stack.push(s) //start node
repeat until find goal vertex or
stack empty:
```

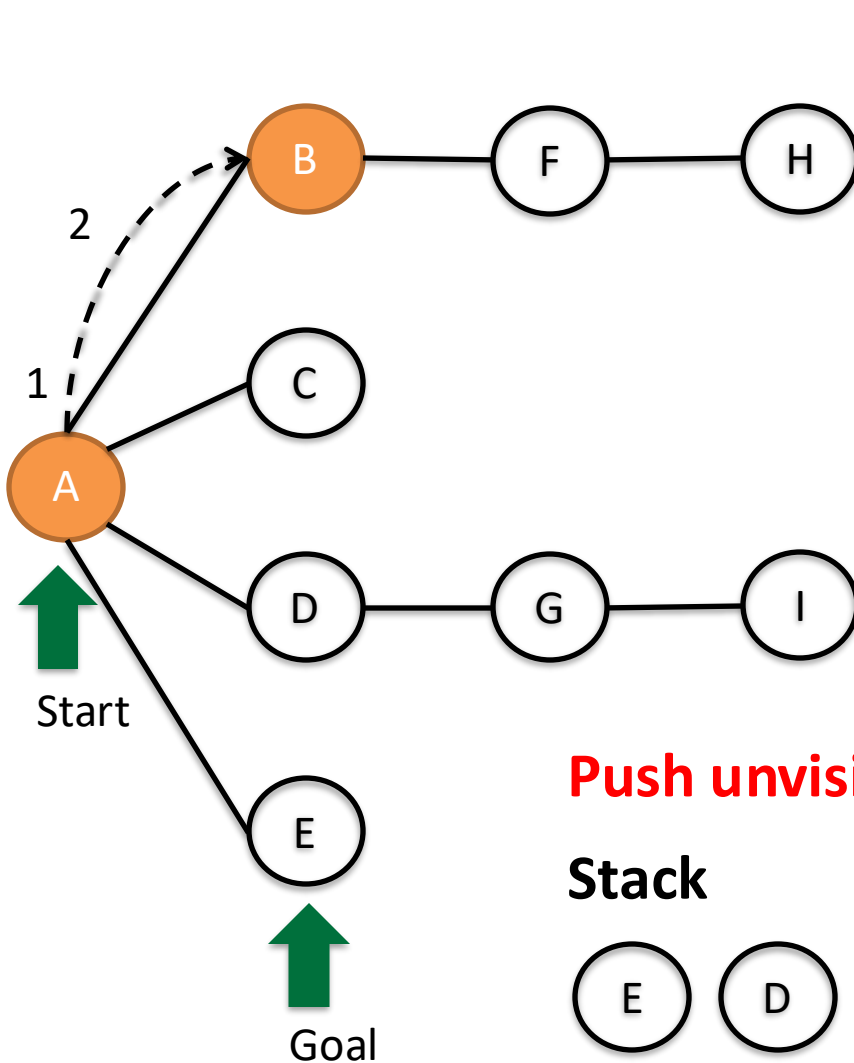
```
    → u = stack.pop()
    if !u.visited
        u.visited = true
        (do something while here)
    for v ∈ u.adjacent
        if !v.visited
            stack.push(v)
```

Pop(B), mark visited

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



--> Order nodes visited

DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

```
    u = stack.pop()
```

```
    if !u.visited
```

```
        u.visited = true
```

```
        (do something while here)
```

```
        for v ∈ u.adjacent
```

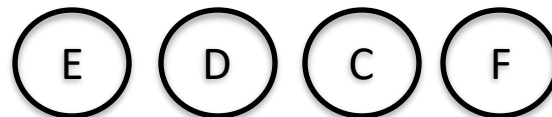
```
            if !v.visited
```

```
                stack.push(v)
```

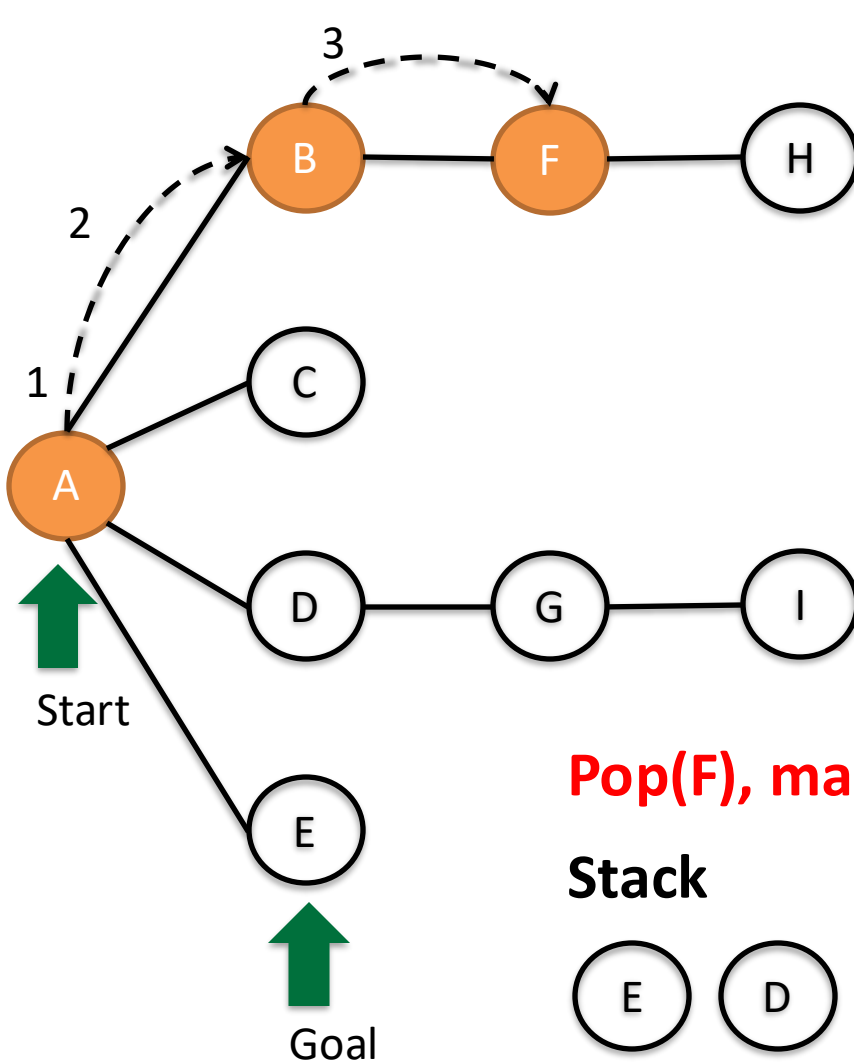


Push unvisited adjacent (F, but not A)

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



---> Order nodes visited

DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

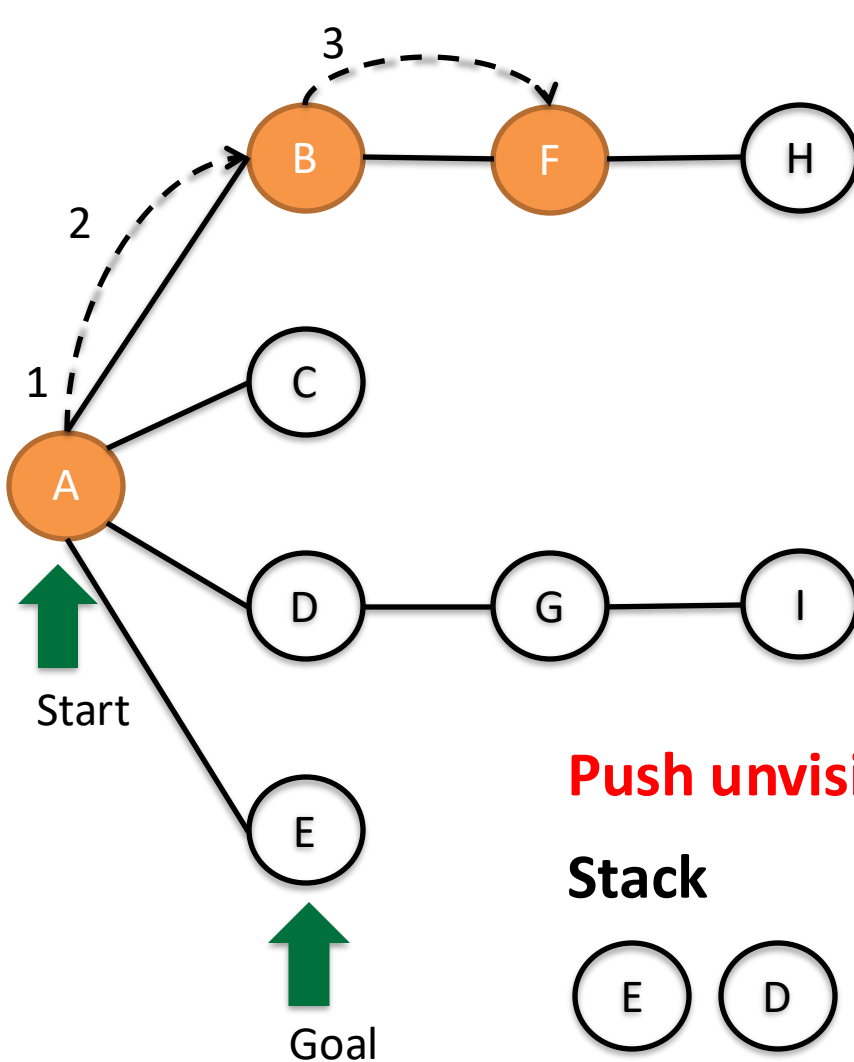
```
    ➔ u = stack.pop()  
    if !u.visited  
        u.visited = true  
        (do something while here)  
    for v ∈ u.adjacent  
        if !v.visited  
            stack.push(v)
```

Pop(F), mark visited

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

```
    u = stack.pop()
```

```
    if !u.visited
```

```
        u.visited = true
```

```
        (do something while here)
```

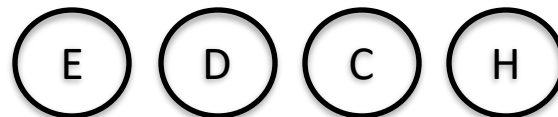
```
        for v ∈ u.adjacent
```

```
            if !v.visited
```

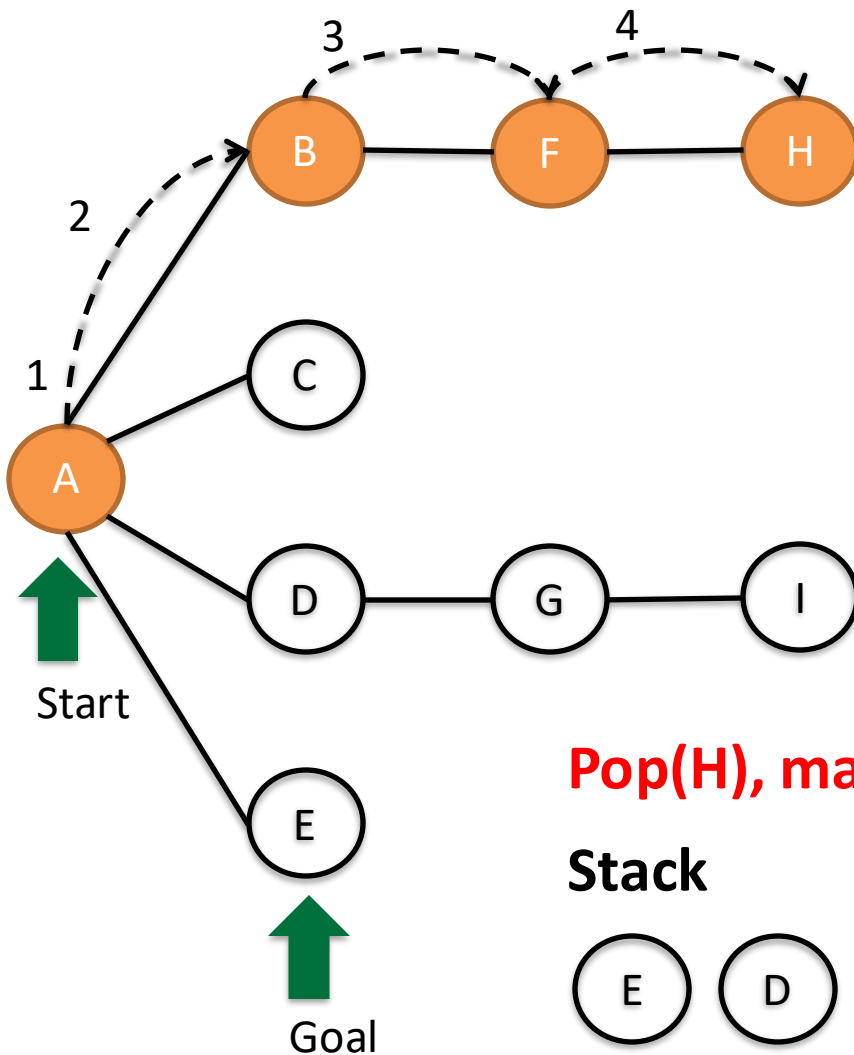
```
                stack.push(v)
```

Push unvisited adjacent (H, but not B)

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

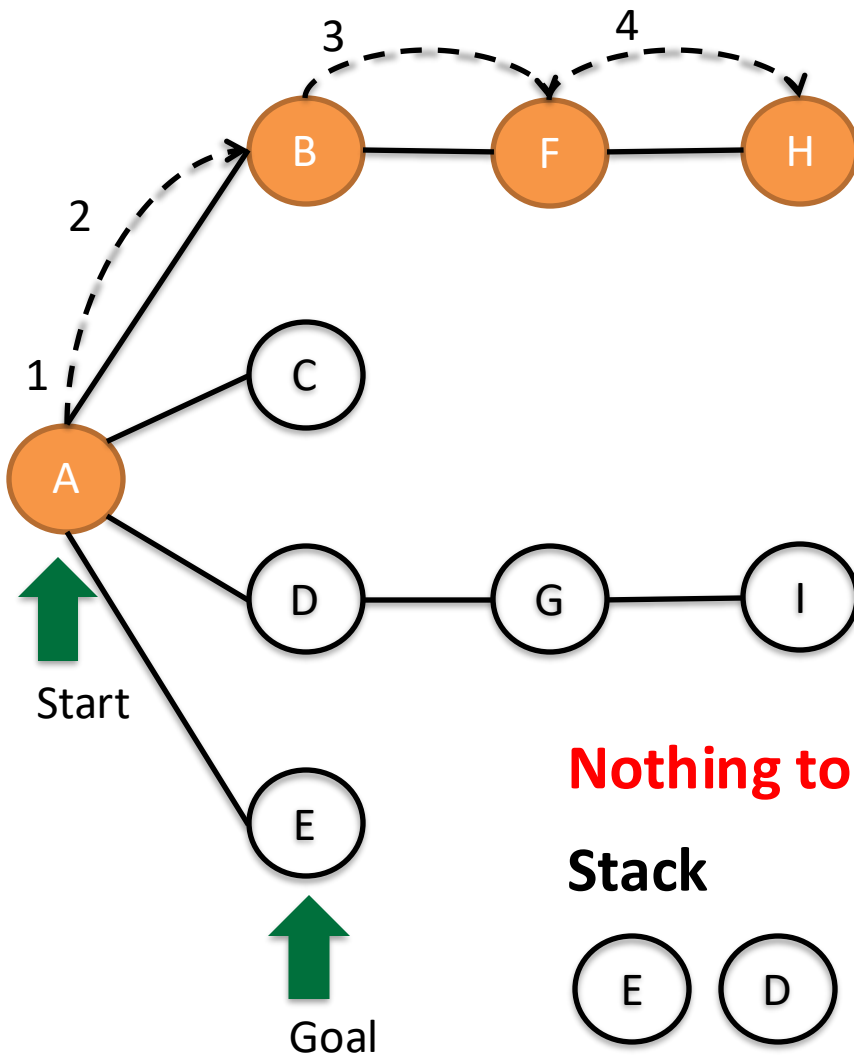
```
➔ u = stack.pop()  
  if !u.visited  
    u.visited = true  
    (do something while here)  
    for v ∈ u.adjacent  
      if !v.visited  
        stack.push(v)
```

Pop(H), mark visited

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

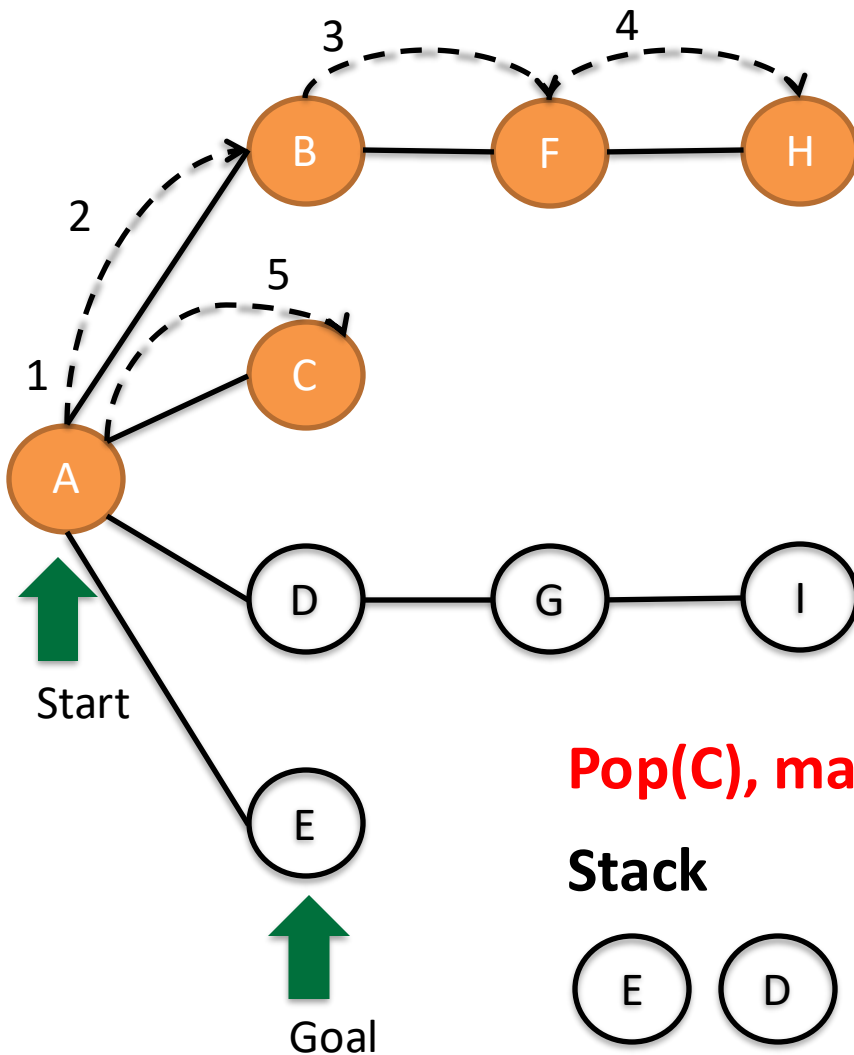
```
    → u = stack.pop()  
    if !u.visited  
        u.visited = true  
        (do something while here)  
        for v ∈ u.adjacent  
            if !v.visited  
                stack.push(v)
```

Nothing to push, back up by popping C

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



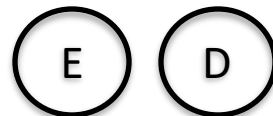
DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

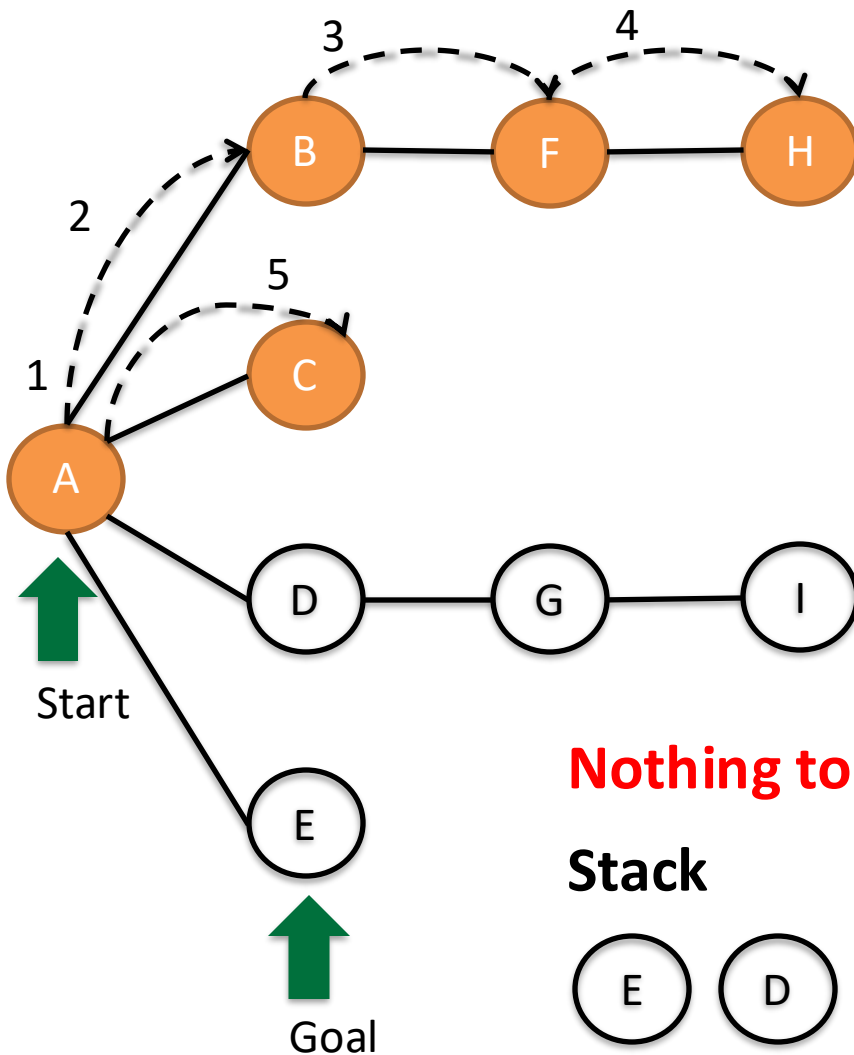
```
    → u = stack.pop()  
    if !u.visited  
        u.visited = true  
        (do something while here)  
        for v ∈ u.adjacent  
            if !v.visited  
                stack.push(v)
```

Pop(C), mark visited

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



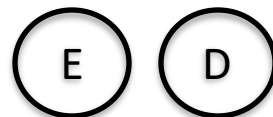
DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

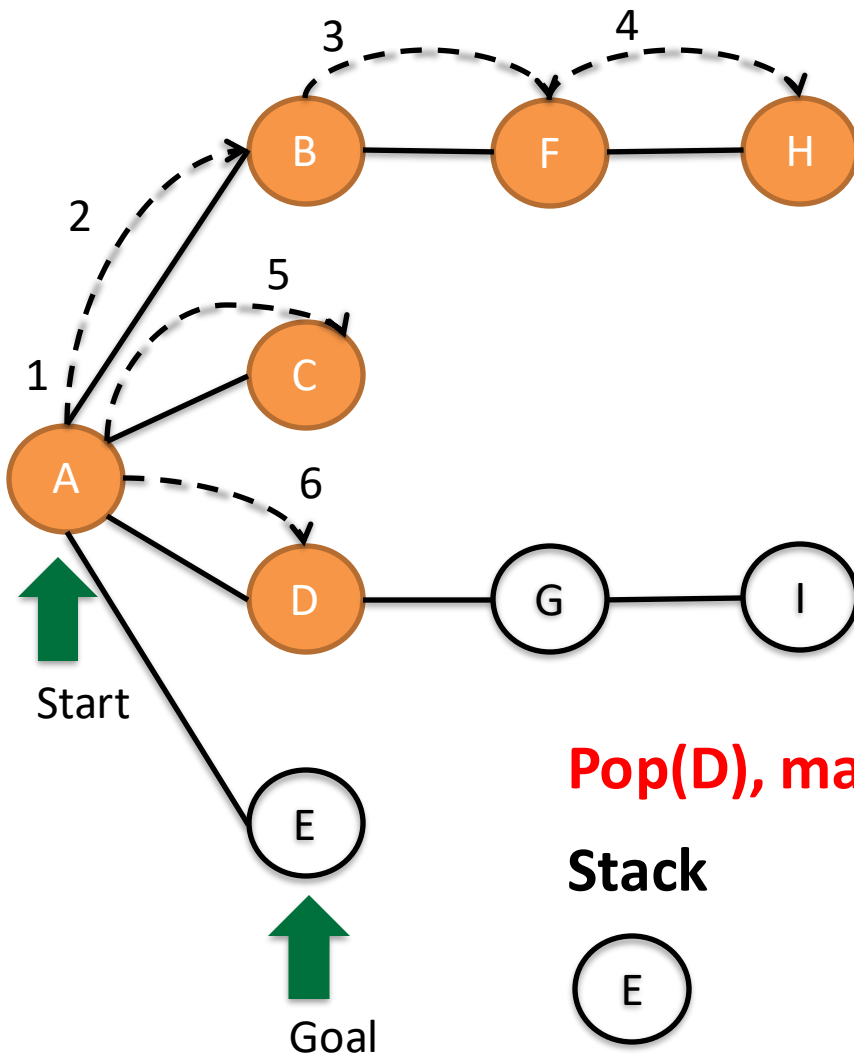
```
    → u = stack.pop()  
    if !u.visited  
        u.visited = true  
        (do something while here)  
        for v ∈ u.adjacent  
            if !v.visited  
                stack.push(v)
```

Nothing to push, back up by popping D

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



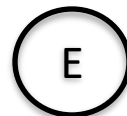
DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

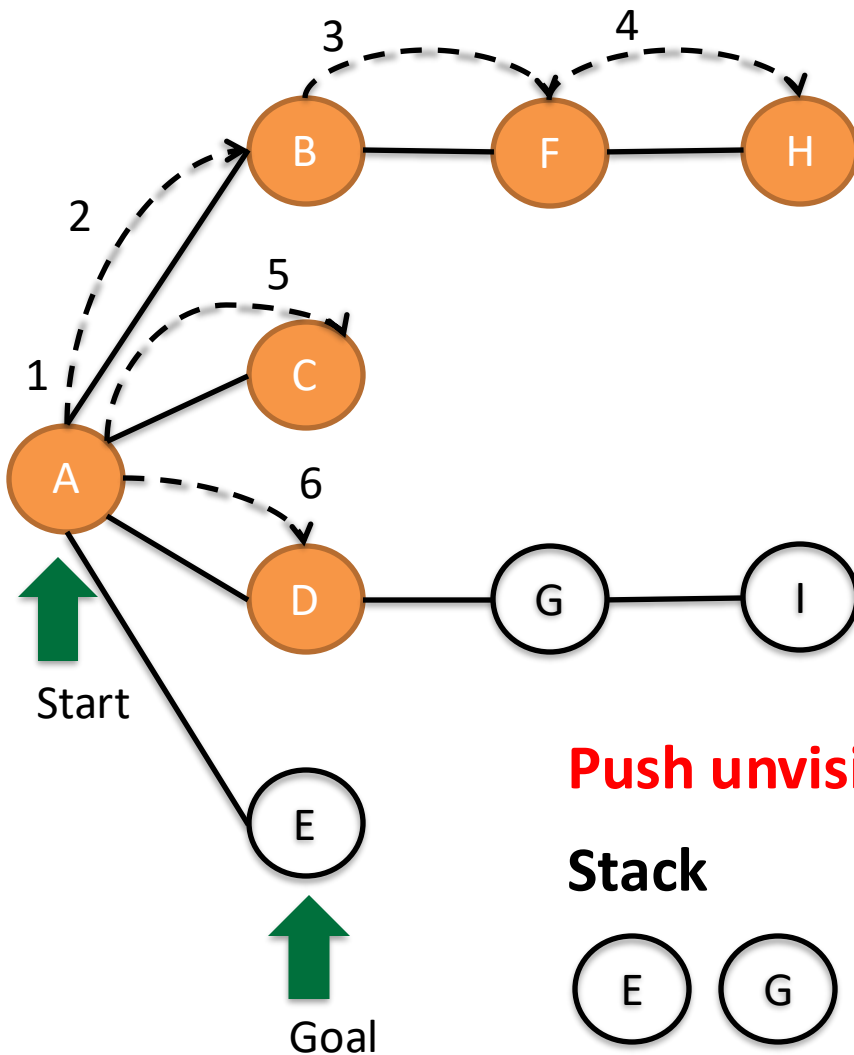
```
➔ u = stack.pop()  
  if !u.visited  
    u.visited = true  
    (do something while here)  
    for v ∈ u.adjacent  
      if !v.visited  
        stack.push(v)
```

Pop(D), mark visited

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

```
    u = stack.pop()
```

```
    if !u.visited
```

```
        u.visited = true
```

```
        (do something while here)
```

```
        for v ∈ u.adjacent
```

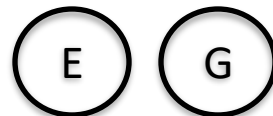
```
            if !v.visited
```

```
                stack.push(v)
```

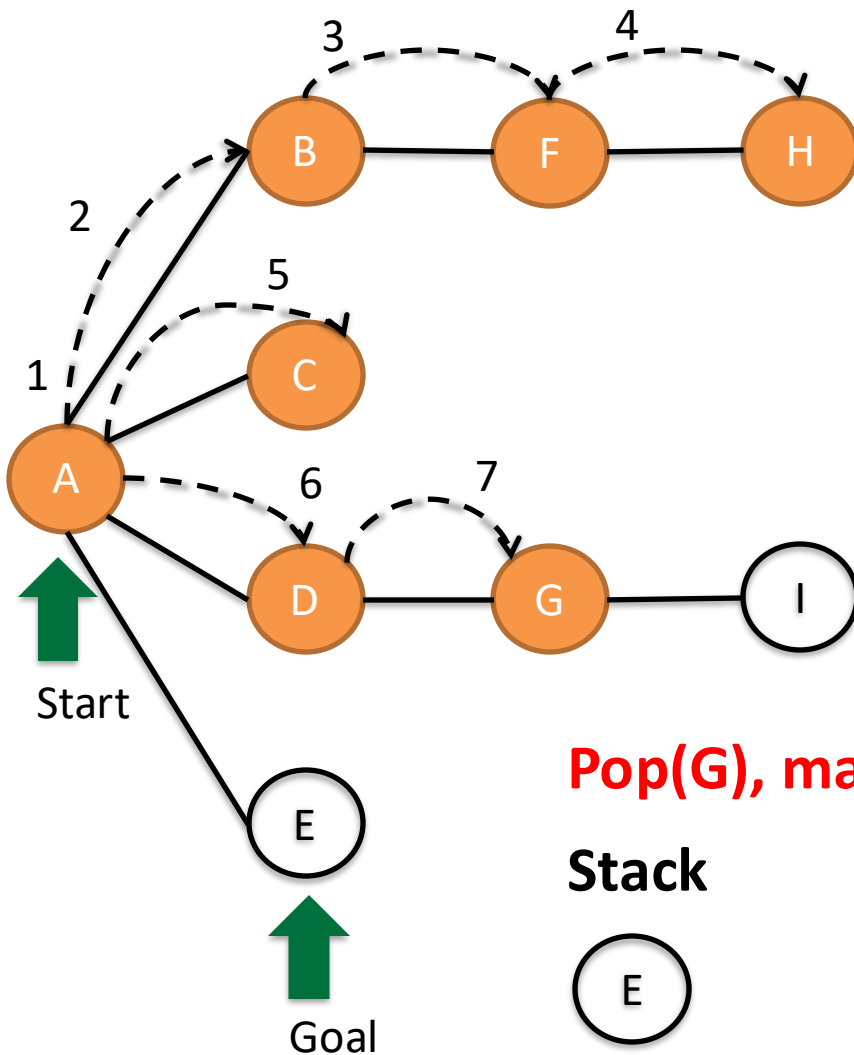


Push unvisited adjacent (G, but not A)

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



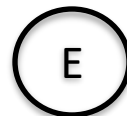
DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

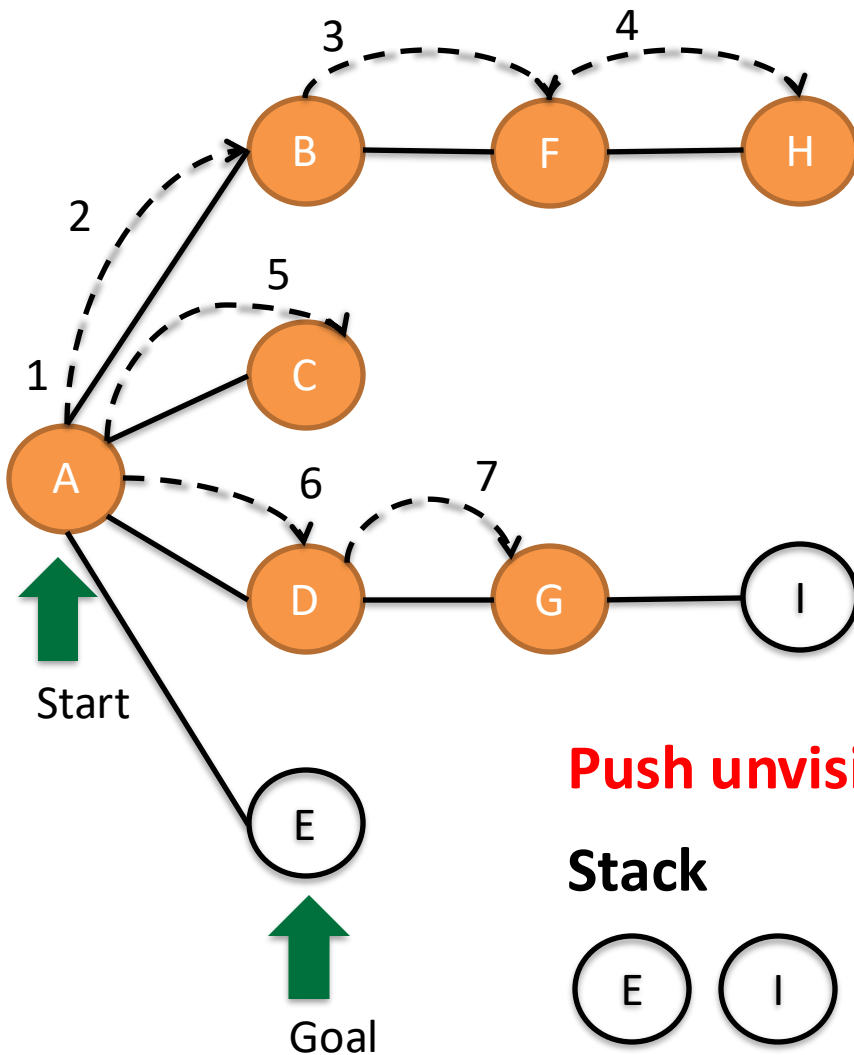
```
    → u = stack.pop()  
    if !u.visited  
        u.visited = true  
        (do something while here)  
        for v ∈ u.adjacent  
            if !v.visited  
                stack.push(v)
```

Pop(G), mark visited

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

```
    u = stack.pop()
```

```
    if !u.visited
```

```
        u.visited = true
```

```
        (do something while here)
```

```
        for v ∈ u.adjacent
```

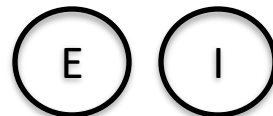
```
            if !v.visited
```

```
                stack.push(v)
```

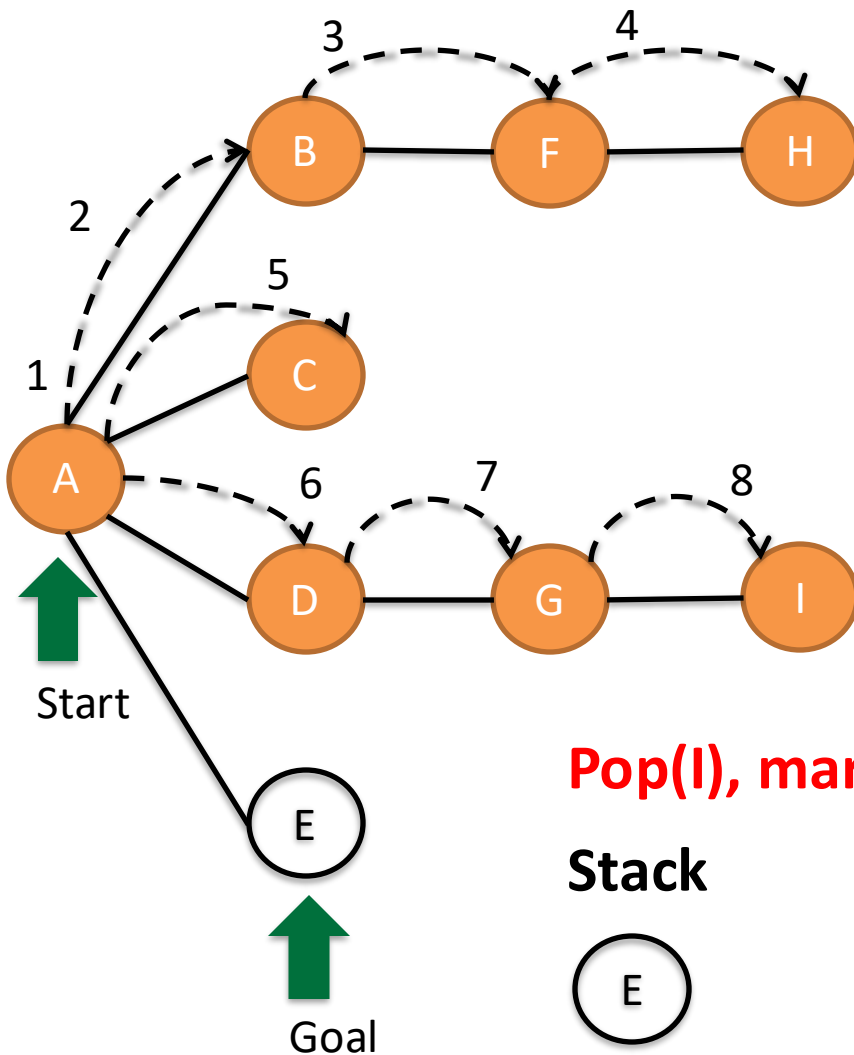


Push unvisited adjacent (I, but not D)

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



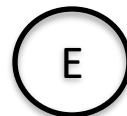
DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

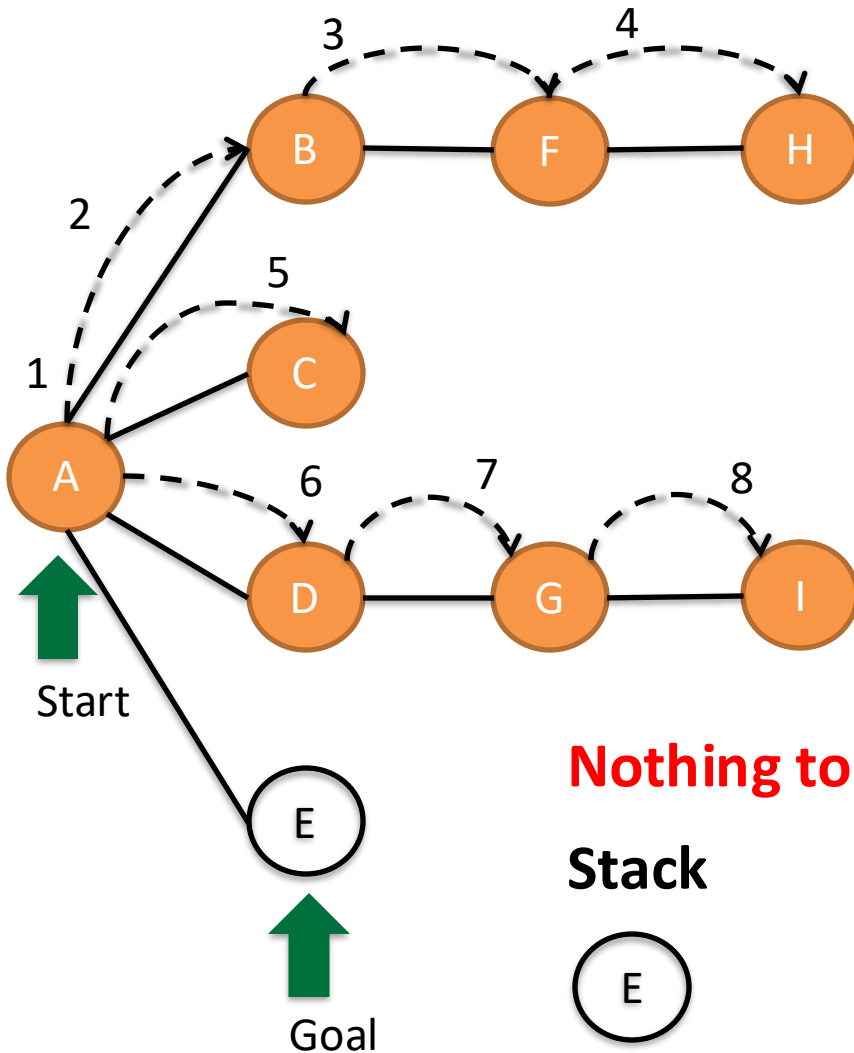
```
    → u = stack.pop()  
    if !u.visited  
        u.visited = true  
        (do something while here)  
        for v ∈ u.adjacent  
            if !v.visited  
                stack.push(v)
```

Pop(I), mark visited

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



---> Order nodes visited

DFS algorithm

```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

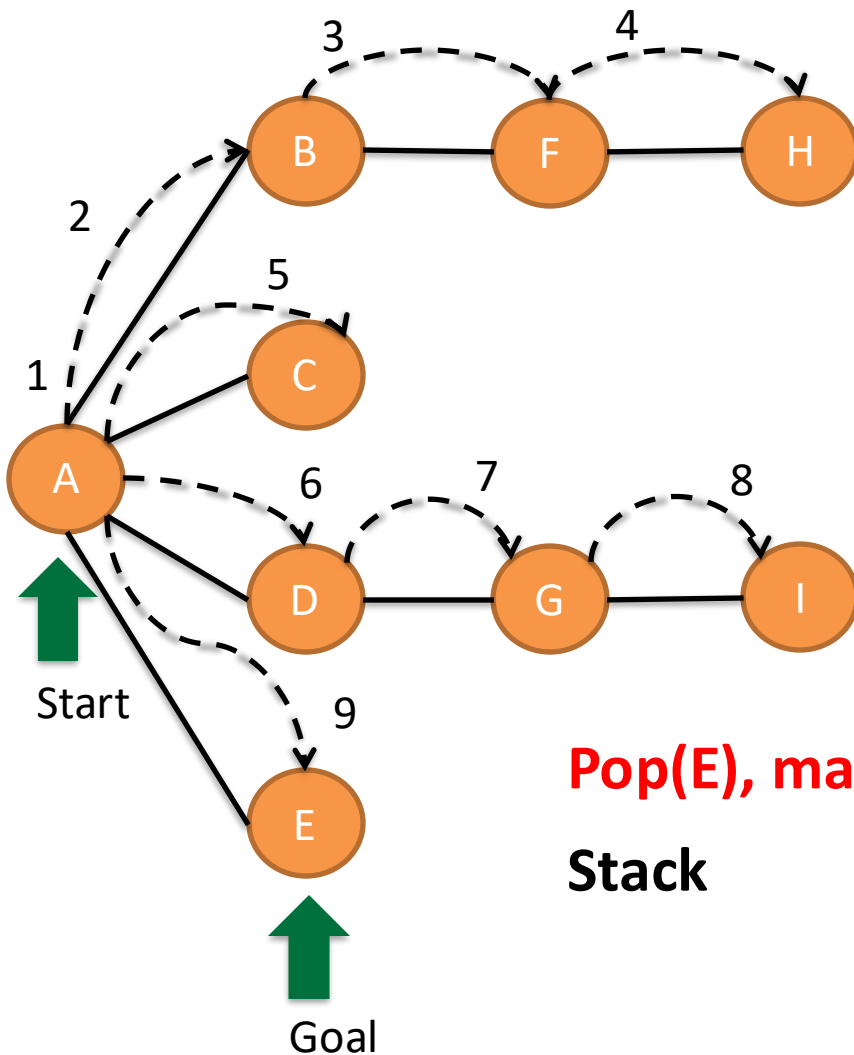
```
    → u = stack.pop()  
    if !u.visited  
        u.visited = true  
        (do something while here)  
        for v ∈ u.adjacent  
            if !v.visited  
                stack.push(v)
```

Nothing to push, back up by popping E

Stack



Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



DFS algorithm

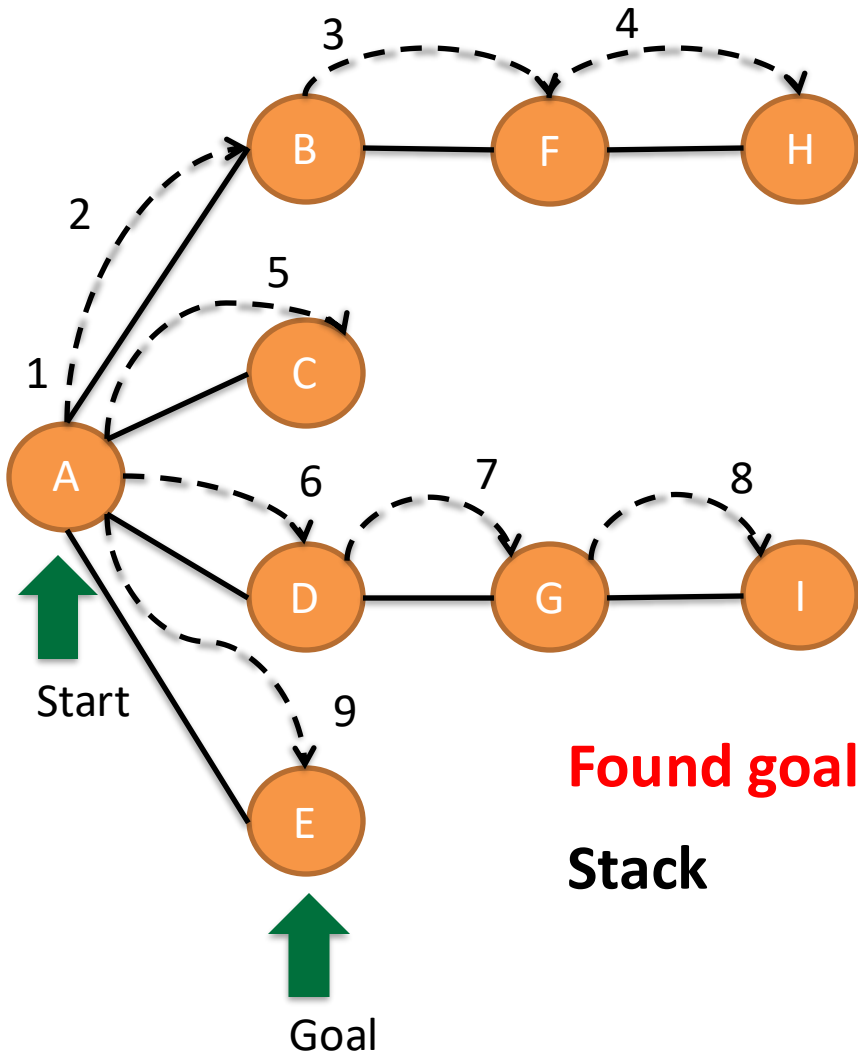
```
stack.push(s) //start node  
repeat until find goal vertex or  
stack empty:
```

```
➔ u = stack.pop()  
  if !u.visited  
    u.visited = true  
    (do something while here)  
    for v ∈ u.adjacent  
      if !v.visited  
        stack.push(v)
```

Pop(E), mark visited

Stack

Depth First Search (DFS) finds a path between *start* and other nodes (if exists)



DFS algorithm

```
stack.push(s) //start node
repeat until find goal vertex or
stack empty:
    u = stack.pop()
    if !u.visited
        u.visited = true
        (do something while here)
        for v ∈ u.adjacent
            if !v.visited
                stack.push(v)
```

After DFS, we can find a path from the *start* node to all other nodes in the Graph

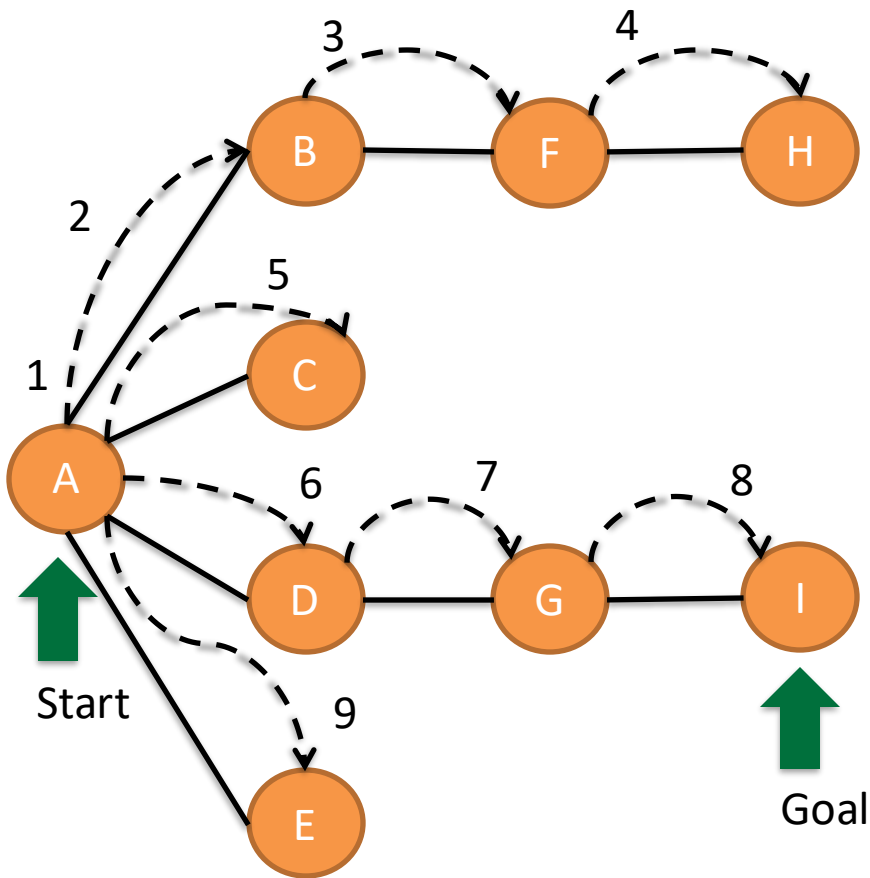
Discovery edges

- Edges that lead to unvisited nodes called *discovery edges*
- Discovery edges form a tree on the graph (root, no cycles)
- Can traverse from *start* to *goal* on tree (if *goal* reachable)
- Can tell us which nodes are not reachable from *start* (not on path formed by discovery edges)
- **With DFS, path not guaranteed to be shortest path!**

Back, cross, and forward edges

- Edges that lead to previously discovered nodes
- Back edges lead to ancestor nodes, forward edges to descendants, cross edges to non-ancestor or descendant
- Back edges indicate presence of a cycle in the Graph
- Today's focus on graphs without cycles

To find path from *start* to *goal*, keep track of previous node as nodes are “discovered”



---> Order nodes visited

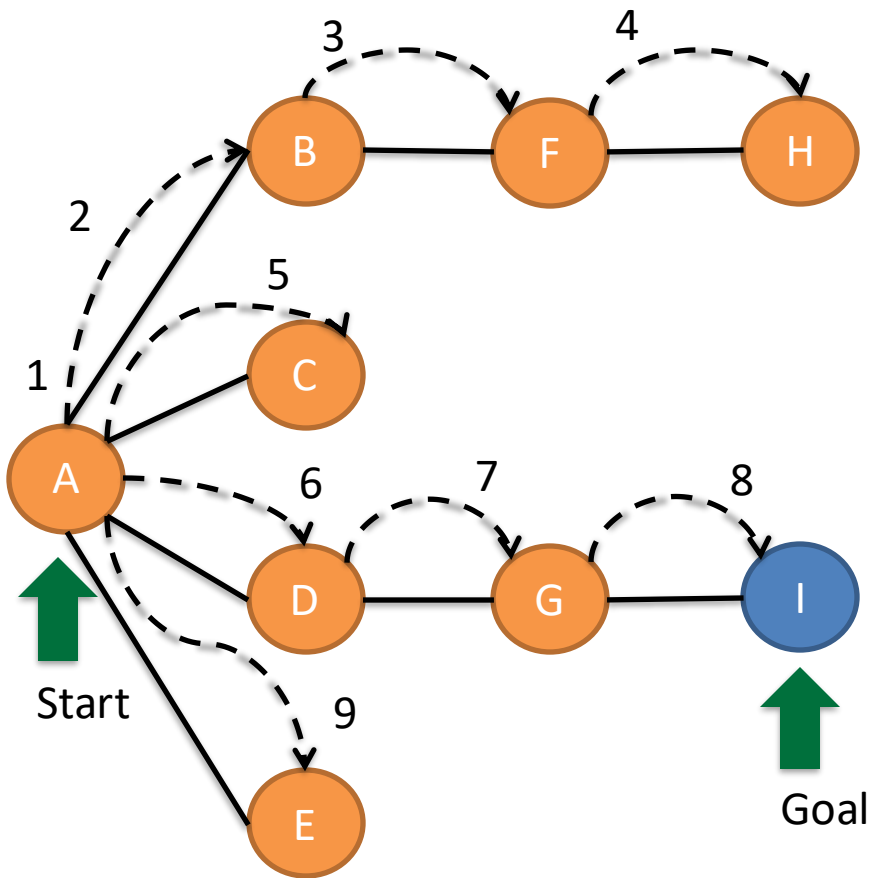
Path from *start* to *goal*

1. Do DFS from *start*
 - When node *discovered*, record previous node
 - Could keep Map with node as Key and previous as Value
2. After DFS complete, find path using Map
 - Begin at *goal* node
 - Track backward on Map until find *start* node
 - Will find a path if it exists, but not necessarily the shortest path (wait for BFS)

Path A to I

Key	Value
A	Null
B	A
C	A
D	A
E	A
F	B
G	D
H	F
I	G

To find path from *start* to *goal*, keep track of previous node as nodes are “discovered”



Path from *start* to *goal*

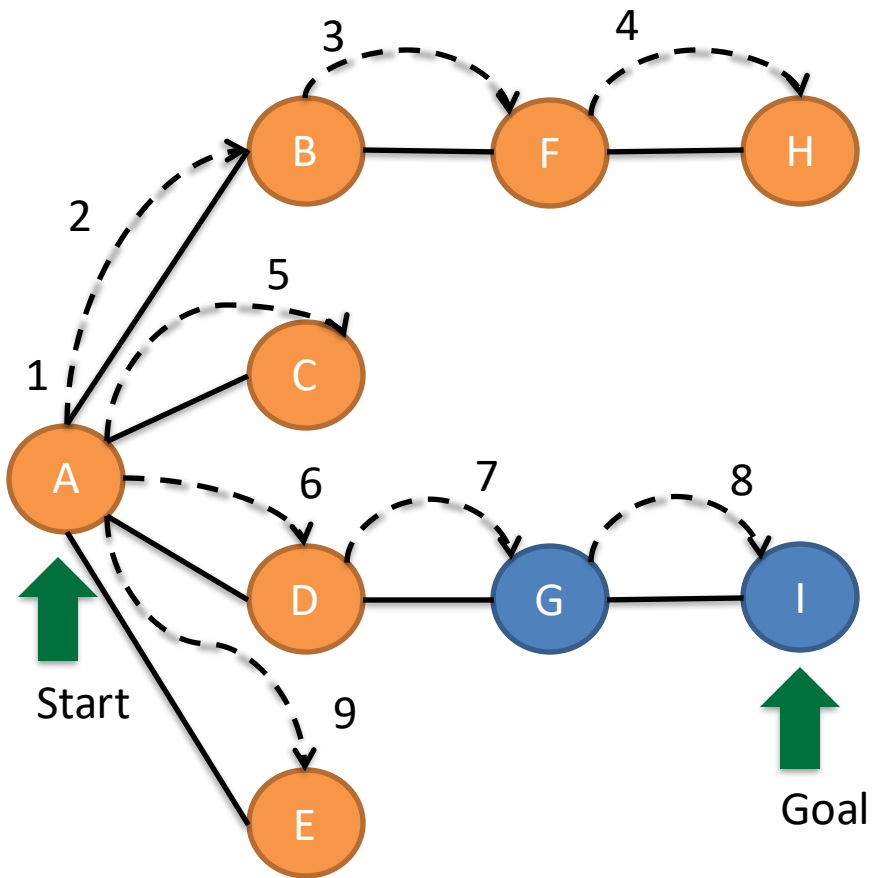
1. Do DFS from *start*
 - When node *discovered*, record previous node
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2. After DFS complete, find path using Map
 - Begin at *goal* node
 - Track backward on Map until find *start* node
 - Will find a path if it exists, but not necessarily the shortest path (wait for BFS)

Path A to I

Key	Value
A	Null
B	A
C	A
D	A
E	A
F	B
G	D
H	F
I	G

Path G,I

To find path from *start* to *goal*, keep track of previous node as nodes are “discovered”



Path from *start* to *goal*

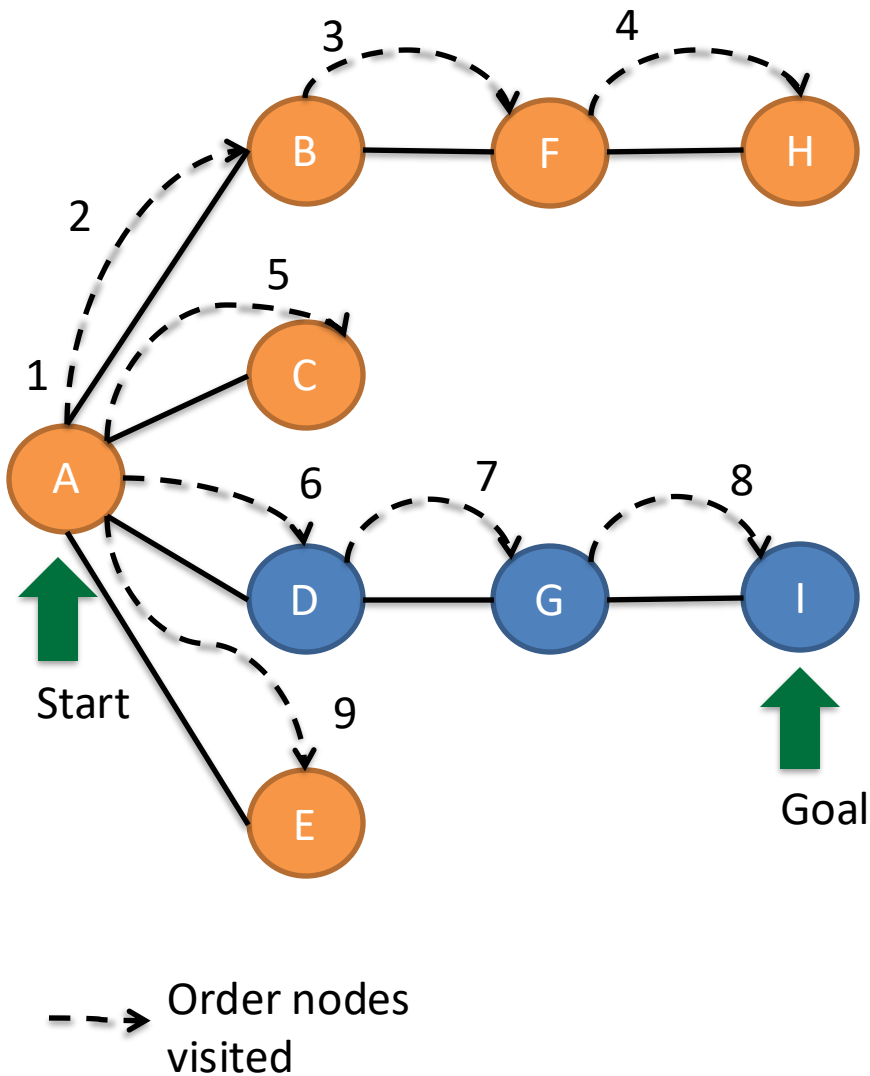
1. Do DFS from *start*
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2. After DFS complete, find path using Map
 - Begin at *goal* node
 - Track backward on Map until find *start* node
 - Will find a path if it exists, but not necessarily the shortest path (wait for BFS)

Path A to I

Key	Value
A	Null
B	A
C	A
D	A
E	A
F	B
G	D
H	F
I	G

Path D,G,I

To find path from *start* to *goal*, keep track of previous node as nodes are “discovered”



Path from *start* to *goal*

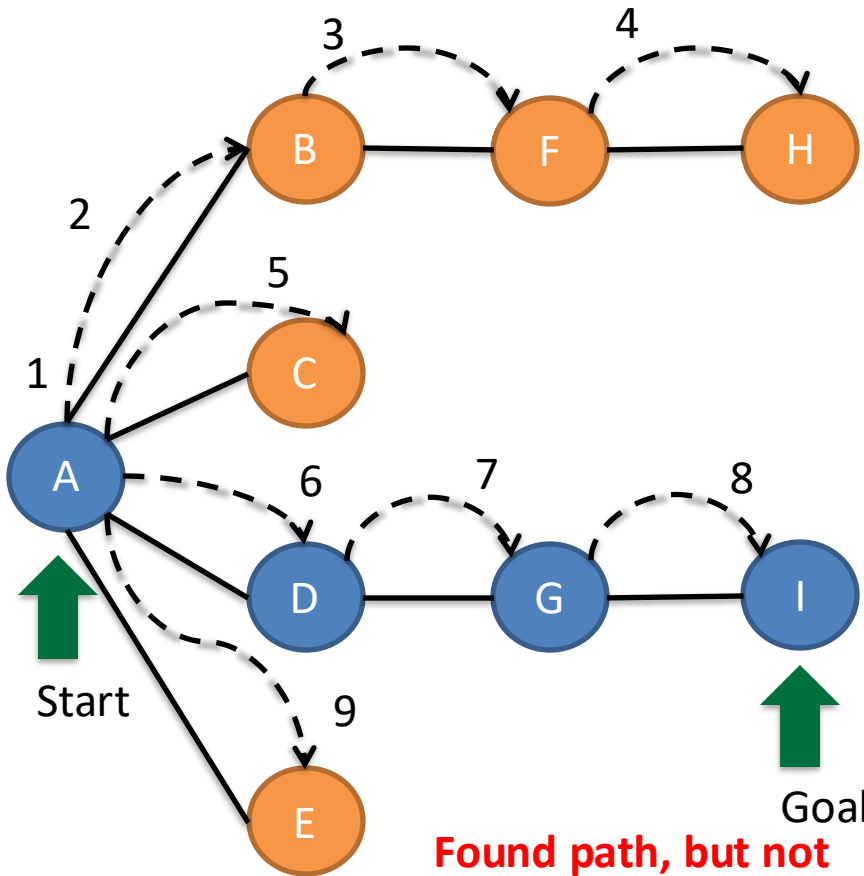
1. Do DFS from *start*
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2. After DFS complete, find path using Map
 - Begin at *goal* node
 - Track backward on Map until find *start* node
 - Will find a path if it exists, but not necessarily the shortest path (wait for BFS)

Path A to I

Key	Value
A	Null
B	A
C	A
D	A
E	A
F	B
G	D
H	F
I	G

Path A,D,G,I

To find path from *start* to *goal*, keep track of previous node as nodes are “discovered”



Found path, but not necessarily shortest path

After DFS from *start* can find a path from *start* to any other reachable node

Path from *start* to *goal*

1. Do DFS from *start*
 - When node *discovered*, record previous node
 - Could keep Map with node as Key and previous as Value
2. After DFS complete, find path using Map
 - Begin at *goal* node
 - Track backward on Map until find *start* node
 - Will find a path if it exists, but not necessarily the shortest path (wait for BFS)

Path A to I

Key	Value
A	Null
B	A
C	A
D	A
E	A
F	B
G	D
H	F
I	G

Path A,D,G,I

Could we start from node other than A? No!

GraphTraversal.java: DFS code

```
17 public class GraphTraversal<V,E> {
18
19     public Map<V,V> backTrack; //keep track of prior vertex when v
20
21     /**
22      * Constructor. Initialize backTrack to new HashMap.
23      */
24     public GraphTraversal() {
25         backTrack = new HashMap<V,V>();
26     }
27
28     /**
29      * Depth First Search
30      * @param G -- graph to search
31      * @param start -- starting vertex
32      */
33     public void DFS(AdjacencyMapGraph<V,E> G, V start) {
34         System.out.println("\nDepth First Search from " + start);
35         backTrack = new HashMap<V,V>(); //initialize backTrack
36         backTrack.put(start, null); //load start node with null pa
37         Set<V> visited = new HashSet<V>(); //Set to track which ve
38         Stack<V> stack = new Stack<V>(); //stack to implement DFS
39
40         stack.push(start); //push start vertex
41         while (!stack.isEmpty()) { //loop until no more vertices
42             V u = stack.pop(); //get most recent vertex
43             if (!visited.contains(u)) { //if not already visited
44                 visited.add(u); //add to visited Set
45                 for (V v : G.outNeighbors(u)) { //loop over out ne
46                     if (!visited.contains(v)) { //if neighbor not
47                         stack.push(v); //push non-visited neighbor
48                         backTrack.put(v, u); //save that this vert
49                     }
50                 }
51             }
52         }
53     }
54 }
```

- When running DFS (or BFS), keep track of prior vertex when a vertex is discovered
- Map Key is current vertex, Value is prior vertex

DFS – given Graph *G* and *start* vertex

- Use *Set* to track visited vertices
- Use *Stack* to track vertices to visit
- Follow pseudo code from previous slides
- Add vertex to *backTrack* when discovered
- Only discovered vertices are added, non-reachable vertices not added to *backTrack*

After DFS can get from *start* to any reachable node in Graph using *backTrack*

DFS run time is $O(n+m)$

Run time

- Assume graph with n nodes and m edges
- Visit each node at most one time due to visited indicator
- Examine each edge at most one time
- Run-time complexity is $O(n+m)$

After DFS (or BFS) *findPath()* finds a path from start to end if it exists

GraphTraversal.java

```
public List<V> findPath(V start, V end) {  
    //check that DFS or BFS have already been run from start  
    if (backTrack.isEmpty() || !backTrack.containsKey(start) ||  
        (backTrack.containsKey(start) && backTrack.get(start) != null)) {  
        System.out.println("Run DFS or BFS on " + start + " before trying to find a path");  
        return new ArrayList<V>();  
    }  
    System.out.println("Path from " + start + " to " + end);  
    //make sure end vertex in backTrack  
    if (!backTrack.containsKey(end)) {  
        System.out.println("\tNo path found");  
        return new ArrayList<V>();  
    }  
    //start from end vertex and work backward to start vertex  
    List<V> path = new LinkedList<V>(); //this will hold the path from start to end vertex  
    V current = end; //start at end vertex  
    //loop from end vertex back to start vertex  
    while (current != null) {  
        path.add(index: 0, current); //add this vertex to front of arraylist path  
        current = backTrack.get(current); //get vertex that discovered this vertex  
    }  
    System.out.println(path);  
    return path;  
}
```

Make sure DFS or BFS has been previously run from *start* vertex

Make sure *end* vertex reachable

- Run time performance?
- Dependent on length of path from *start* to *end*

- Loop backward from *end* to *start* (parent null)
- Add new vertices to front of *path*
- Return *path* when done

Agenda

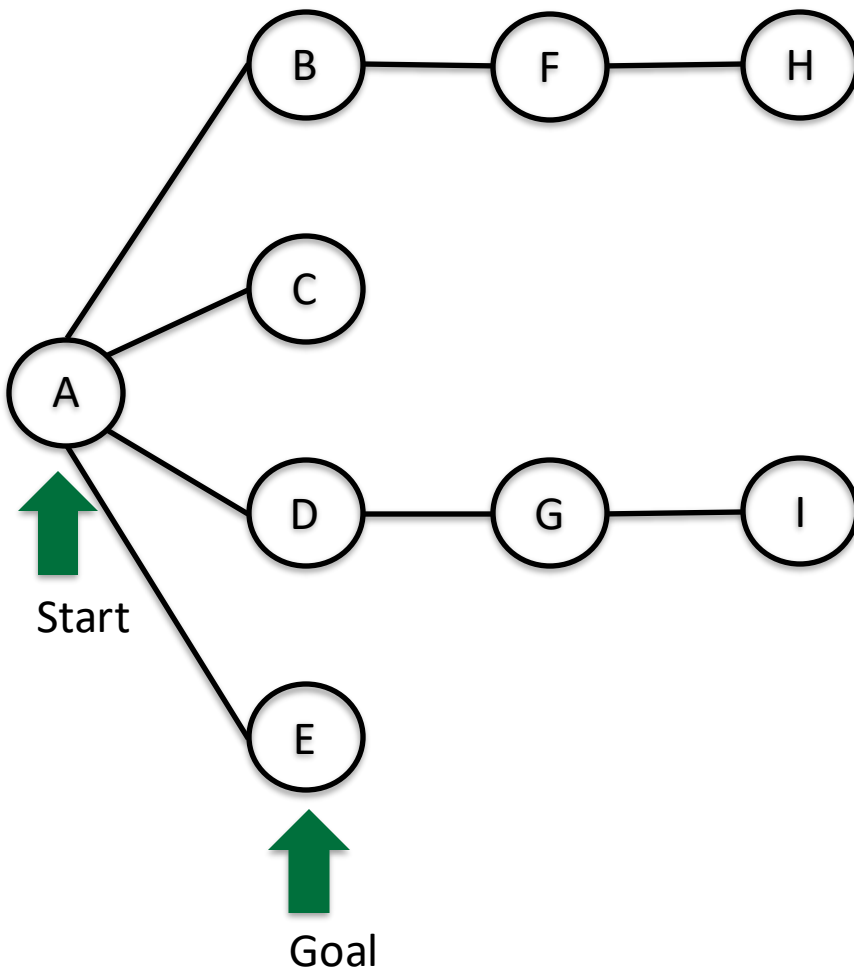
1. Depth first search (DFS)



2. Breadth first search (BFS)

3. Examples from last class and today

Breadth First Search (BFS) finds shortest path between *start* and other nodes



Goal: compute path from *start* to *goal* (or to all other nodes)

BFS basic idea

- Explore outward in “ripples”
- Look at all nodes 1 step away, then all nodes 2 steps away...
- Relies on a **Queue** (implicit or explicit) implementation
- Path from s to any other vertex is **shortest**

Some of you did Breadth First Search on Problem Set 1

RegionFinder

Loop over all the pixels

 If a pixel is unvisited and of the correct color

 Start a new region

 Keep track of pixels need to be visited, initially just one

 As long as there's some pixel that needs to be visited

 Get one to visit

 Add it to the region

 Mark it as visited

 Loop over all its neighbors

 If the neighbor is of the correct color

 Add it to the list of pixels to be visited

 If the region is big enough to be worth keeping, do so

Some of you did Breadth First Search on Problem Set 1

RegionFinder

Loop over all the pixels

 If a pixel is unvisited and of the correct color

 Start a new region

 Keep track of pixels need to be visited, initially just one

 As long as there's some pixel that needs to be visited

 Get one to visit

 Add it to the region

 Mark it as visited

 Loop over all its neighbors

 If the neighbor is of the correct color

Add it to the list of pixels to be visited

 If the region is big enough to be worth keeping, do so



If you added to end of list...

Some of you did Breadth First Search on Problem Set 1

RegionFinder

Loop over all the pixels

If a pixel is unvisited and of the correct color

Start a new region

Keep track of pixels need to be visited, initially just one

As long as there's some pixel that needs to be visited

Get one to visit



And if you get a pixel from front of list, you implemented a Queue

Add it to the region

Mark it as visited

Loop over all its neighbors

If the neighbor is of the correct color

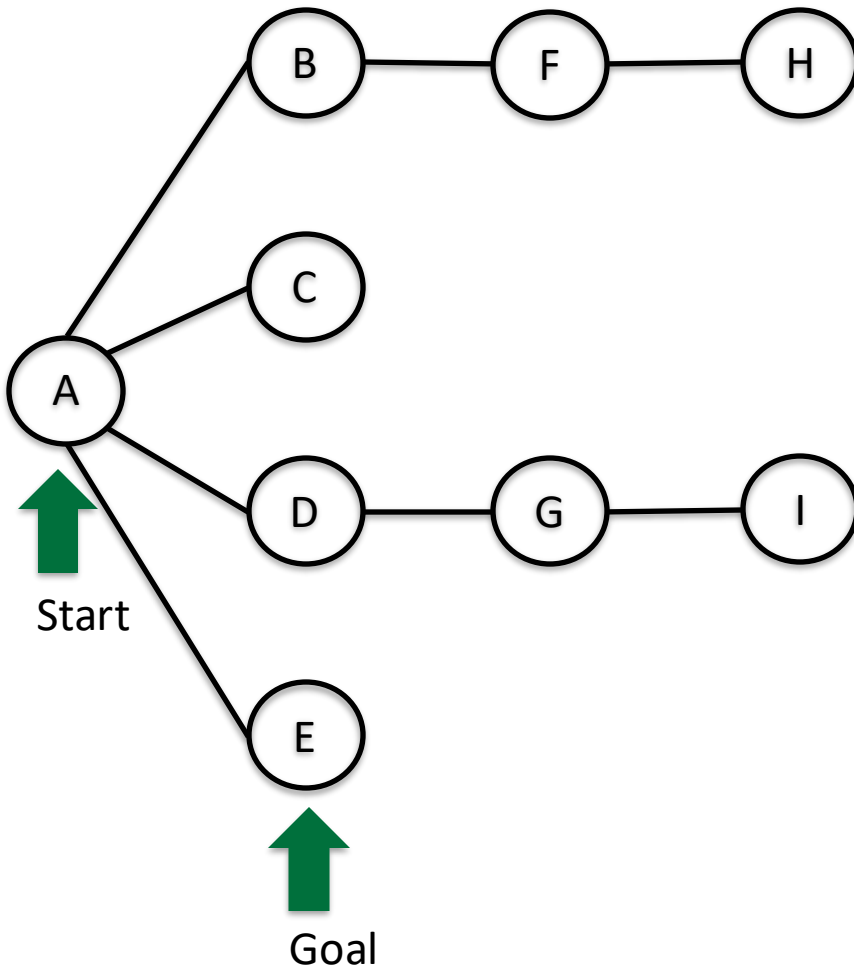
Add it to the list of pixels to be visited

If the region is big enough to be worth keeping, do so



If you added to end of list...

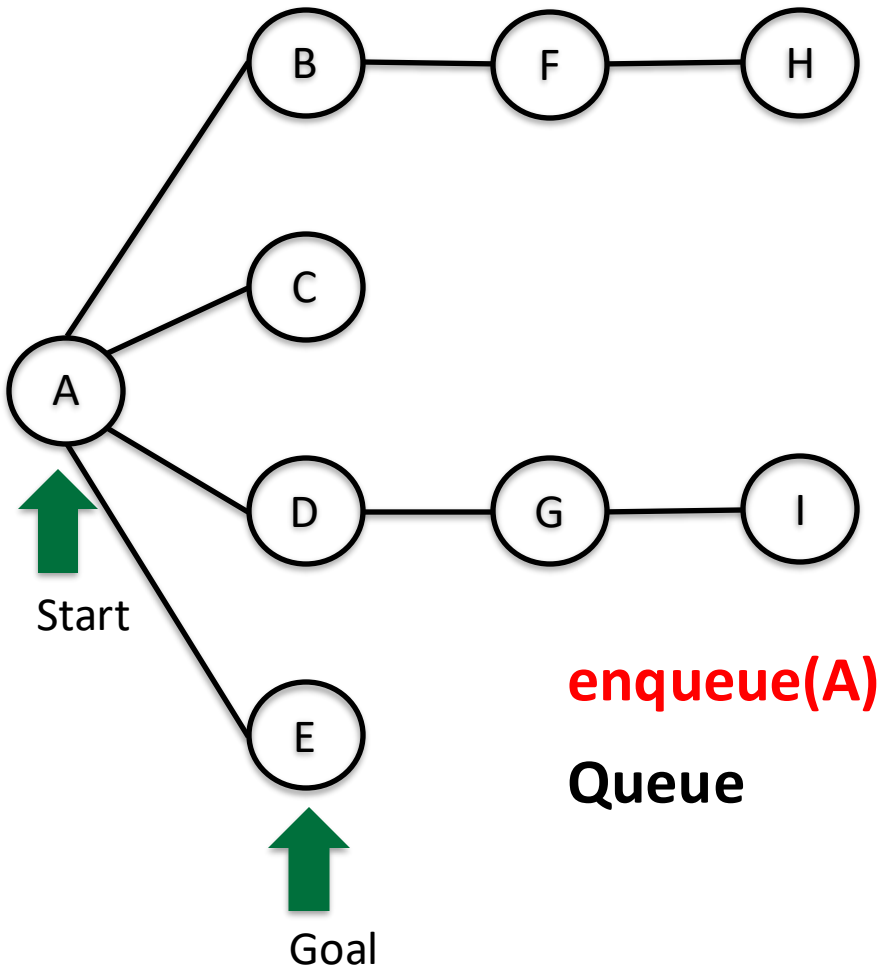
Breadth First Search (BFS) finds shortest path between *start* and other nodes



BFS algorithm

```
enqueue(s) //start node
s.visited = true
repeat until find goal vertex or
queue empty:
    u = dequeue()
    (do something here)
    for v ∈ u.adjacent
        if !v.visited
            v.visited = true
            enqueue(v)
```

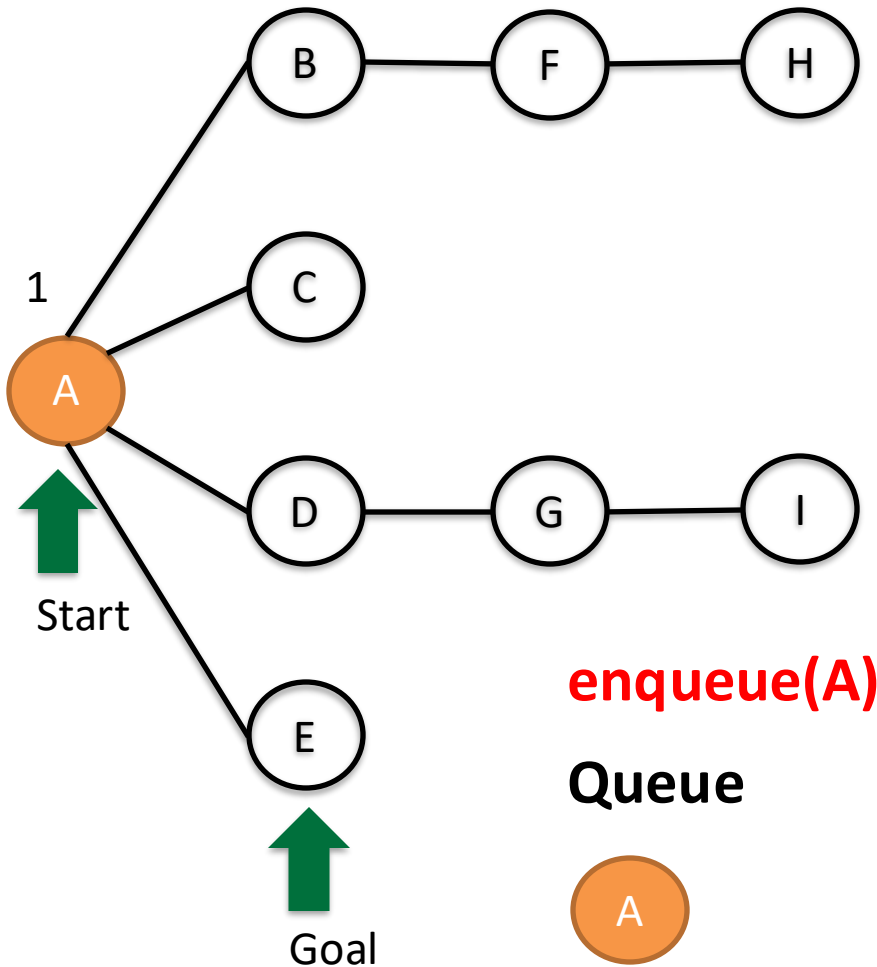
Breadth First Search (BFS) finds shortest path between *start* and other nodes



BFS algorithm

```
enqueue(s) //start node
s.visited = true
repeat until find goal vertex or
queue empty:
    u = dequeue()
    (do something here)
    for v ∈ u.adjacent
        if !v.visited
            v.visited = true
            enqueue(v)
```

Breadth First Search (BFS) finds shortest path between *start* and other nodes



BFS algorithm

```
enqueue(s) //start node
```



```
s.visited = true
```

```
repeat until find goal vertex or  
queue empty:
```

```
u = dequeue()
```

```
(do something here)
```

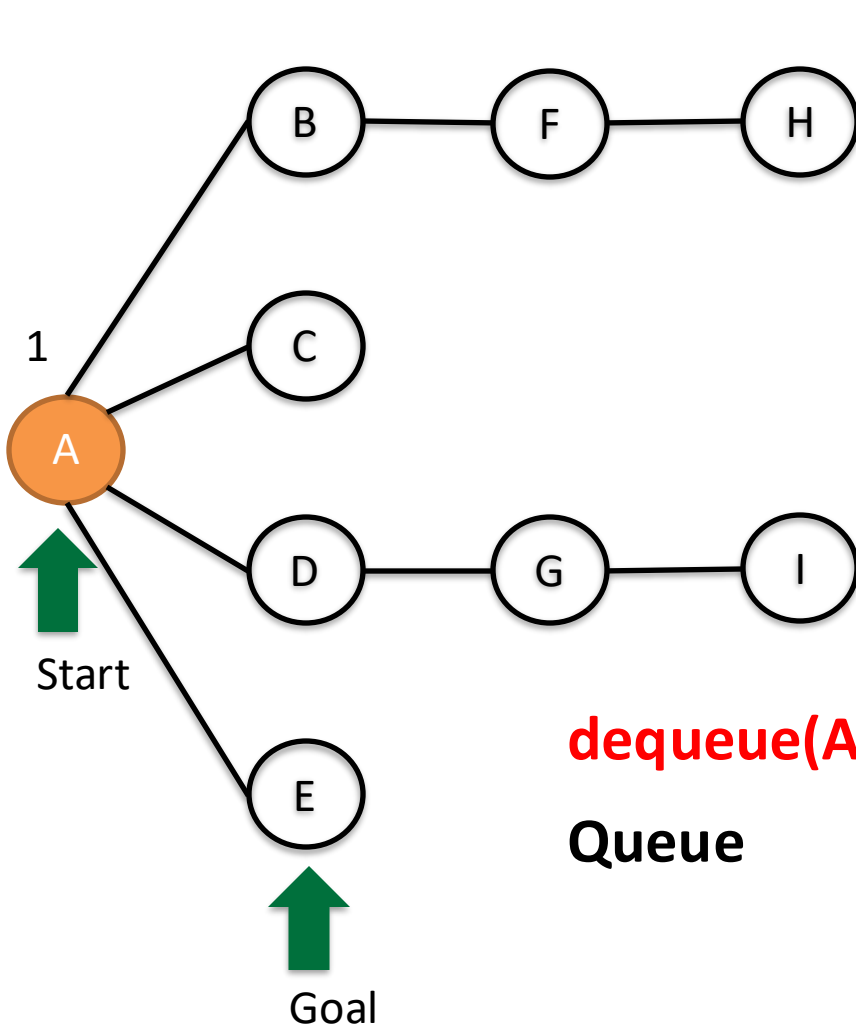
```
for v ∈ u.adjacent
```

```
if !v.visited
```

```
v.visited = true
```

```
enqueue(v)
```

Breadth First Search (BFS) finds shortest path between *start* and other nodes



dequeue(A), visit A

Queue

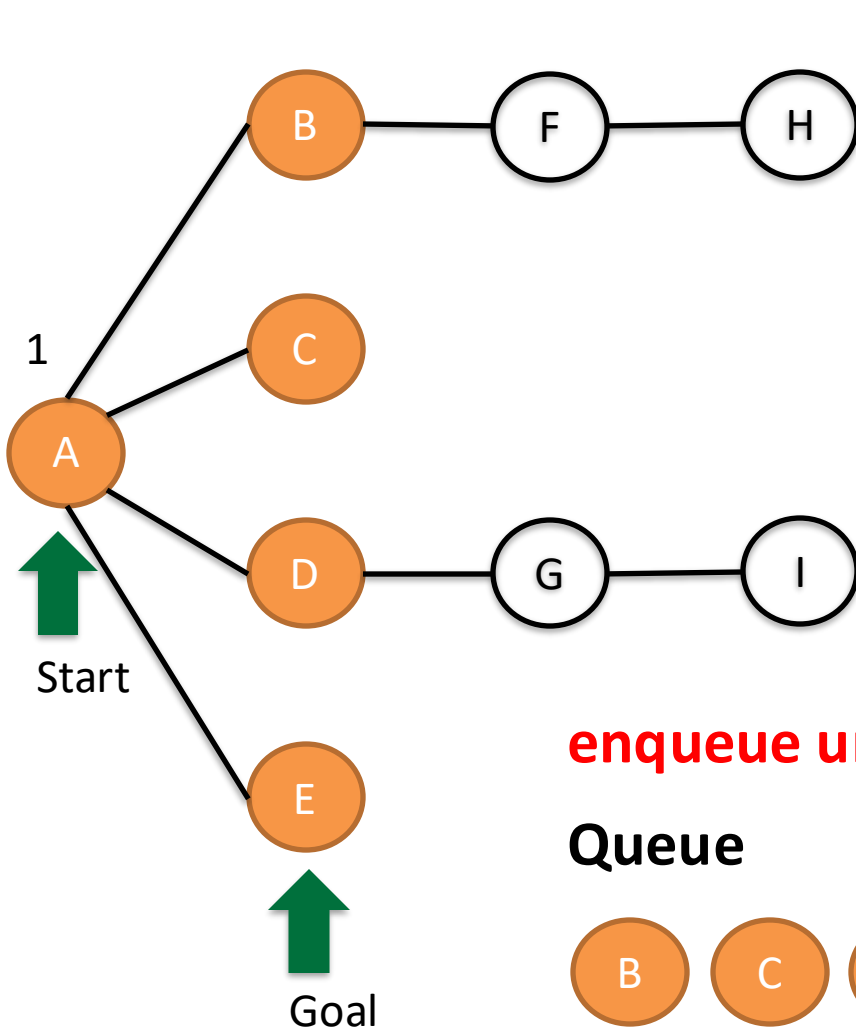
BFS algorithm

```
enqueue(s) //start node  
s.visited = true  
repeat until find goal vertex or  
queue empty:
```

```
→ u = dequeue()  
  (do something here)  
  for v ∈ u.adjacent  
    if !v.visited  
      v.visited = true  
      enqueue(v)
```

“Visit” node u

Breadth First Search (BFS) finds shortest path between *start* and other nodes



BFS algorithm

```
enqueue(s) //start node
s.visited = true
repeat until find goal vertex or
queue empty:
    u = dequeue()
    (do something here)
    for v ∈ u.adjacent
        if !v.visited
            v.visited = true
            enqueue(v)
```

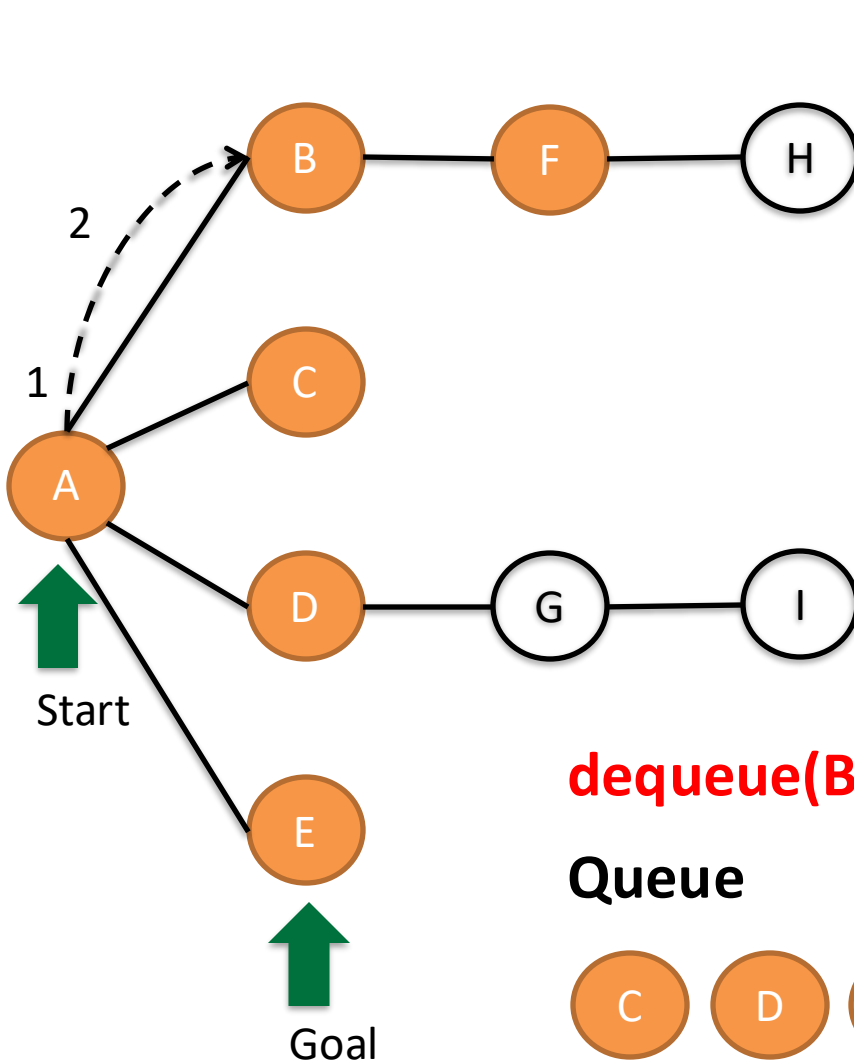
"Visit" node u

enqueue unvisited adjacent

Queue



Breadth First Search (BFS) finds shortest path between *start* and other nodes



--> Order nodes visited

BFS algorithm

```
enqueue(s) //start node  
s.visited = true  
repeat until find goal vertex or  
queue empty:
```

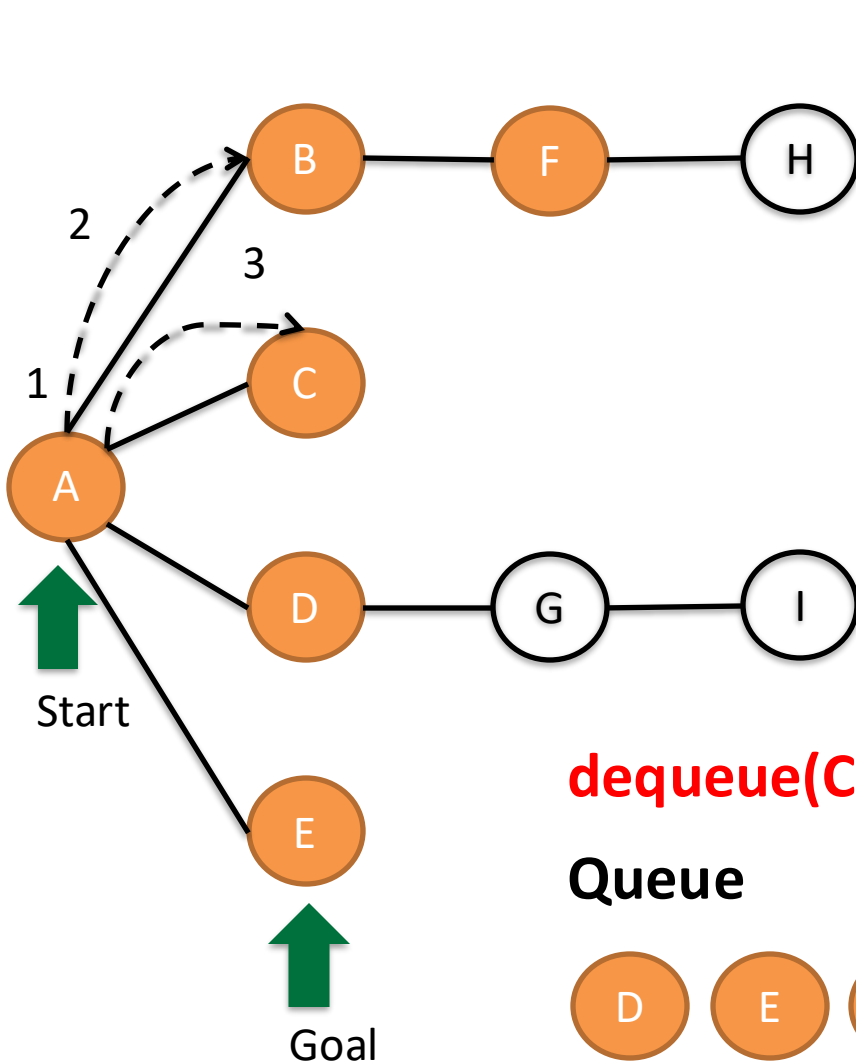
```
    u = dequeue()  
    (do something here)  
    for v ∈ u.adjacent  
        if !v.visited  
            v.visited = true  
            enqueue(v)
```

dequeue(B), enqueue unvisited adjacent F (not A)

Queue



Breadth First Search (BFS) finds shortest path between *start* and other nodes



--> Order nodes visited

BFS algorithm

```
enqueue(s) //start node
s.visited = true
repeat until find goal vertex or
queue empty:
```

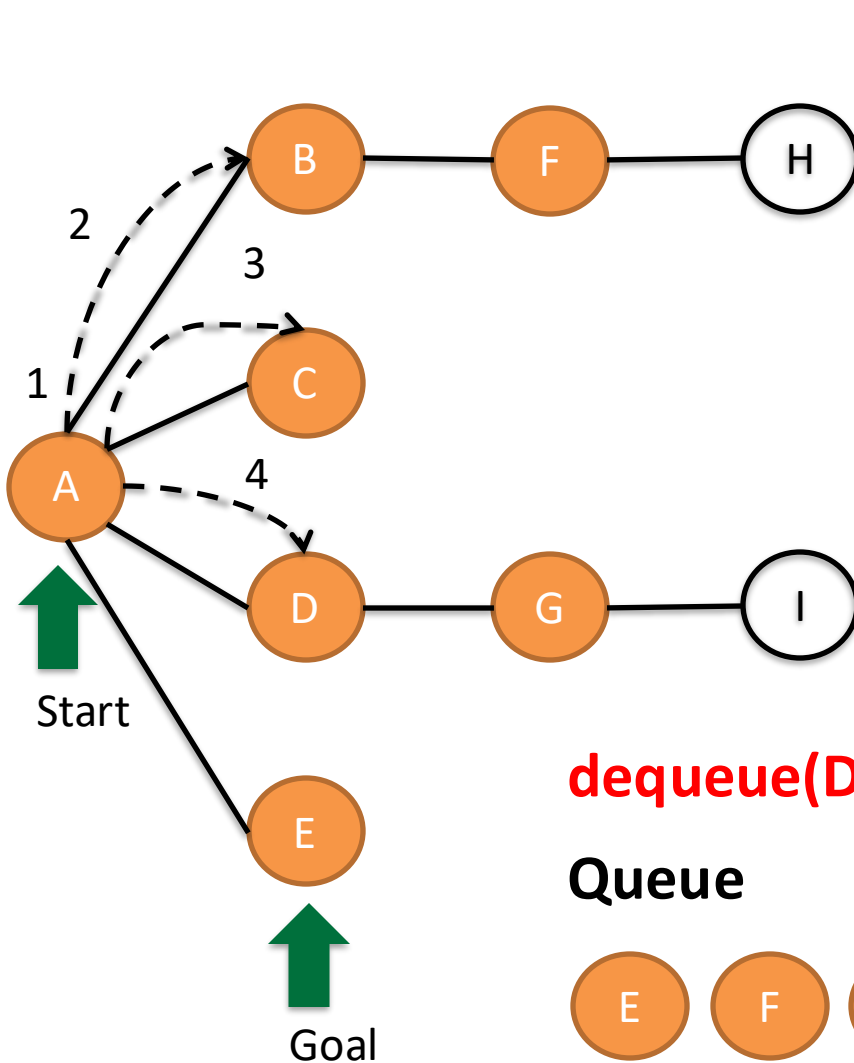
```
    u = dequeue()
    (do something here)
    for v ∈ u.adjacent
        if !v.visited
            v.visited = true
            enqueue(v)
```

dequeue(C), enqueue unvisited adjacent (none)

Queue



Breadth First Search (BFS) finds shortest path between *start* and other nodes



--> Order nodes visited

BFS algorithm

```
enqueue(s) //start node
s.visited = true
repeat until find goal vertex or
queue empty:
```

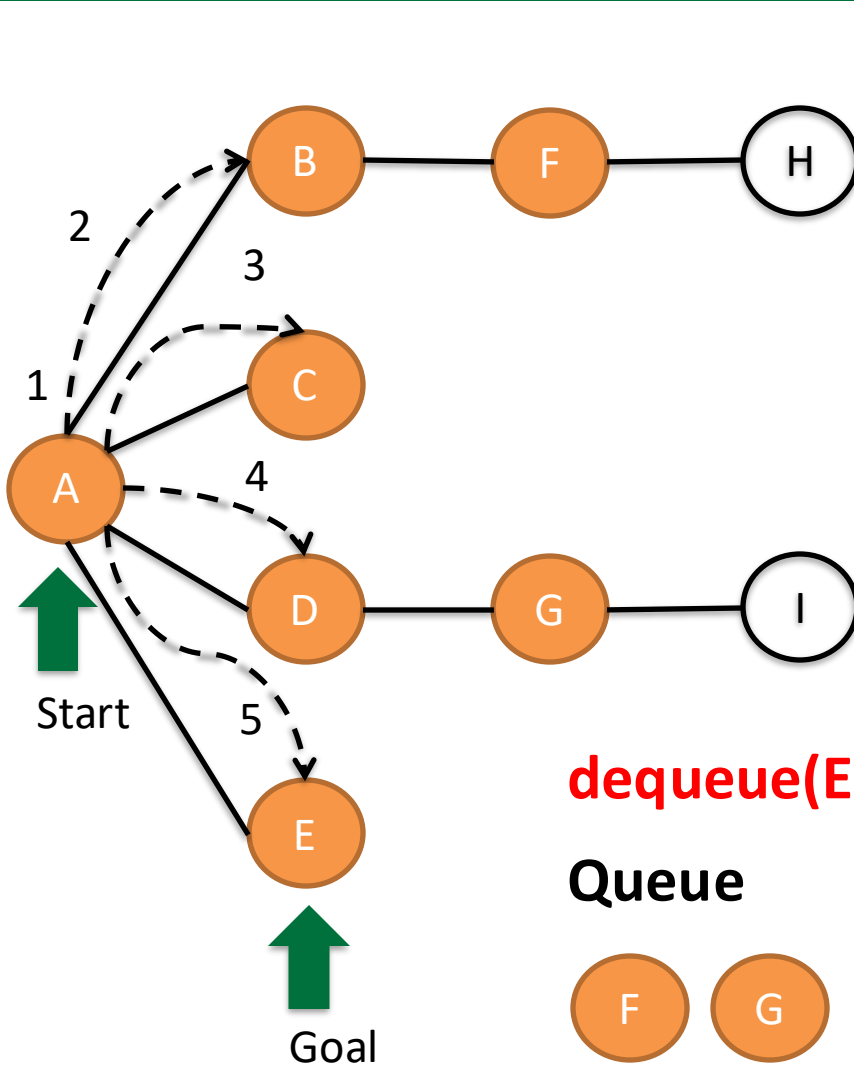
```
    u = dequeue()
    (do something here)
    for v ∈ u.adjacent
        if !v.visited
            v.visited = true
            enqueue(v)
```

dequeue(D), enqueue unvisited adjacent G (not A)

Queue



Breadth First Search (BFS) finds shortest path between *start* and other nodes



BFS algorithm

```
enqueue(s) //start node
s.visited = true
repeat until find goal vertex or
queue empty:
```

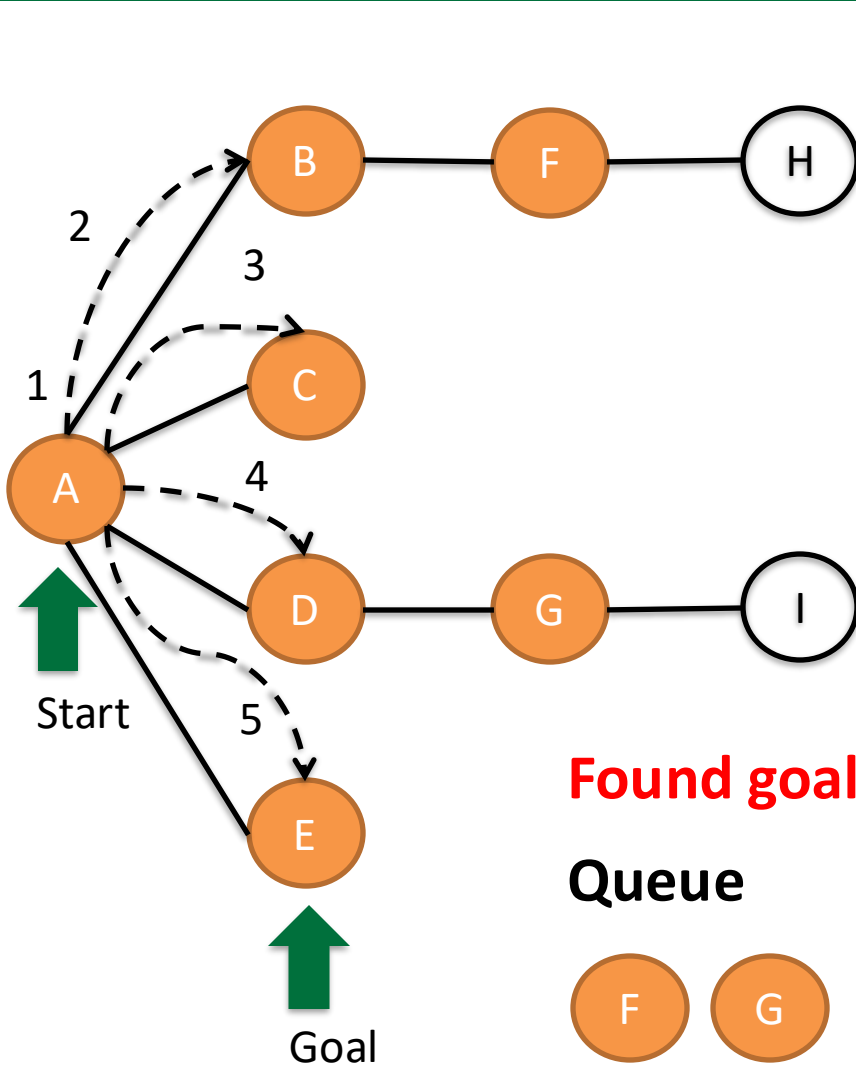
```
    u = dequeue()
    (do something here)
    for v ∈ u.adjacent
        if !v.visited
            v.visited = true
            enqueue(v)
```

dequeue(E), enqueue unvisited adjacent (none)

Queue



Breadth First Search (BFS) finds shortest path between *start* and other nodes



BFS algorithm

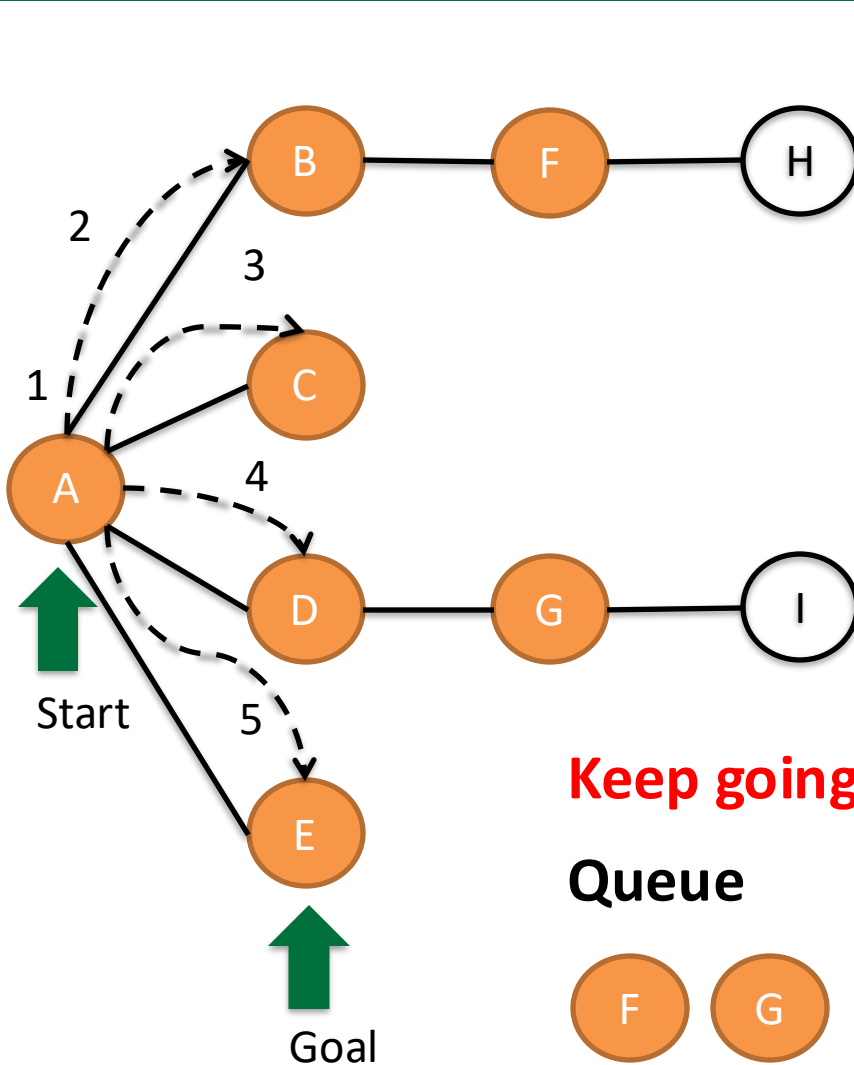
```
enqueue(s) //start node
s.visited = true
repeat until find goal vertex or
queue empty:
    u = dequeue()
    (do something here)
    for v ∈ u.adjacent
        if !v.visited
            v.visited = true
            enqueue(v)
```

Found goal! Can stop now

Queue



Breadth First Search (BFS) finds shortest path between *start* and other nodes



BFS algorithm

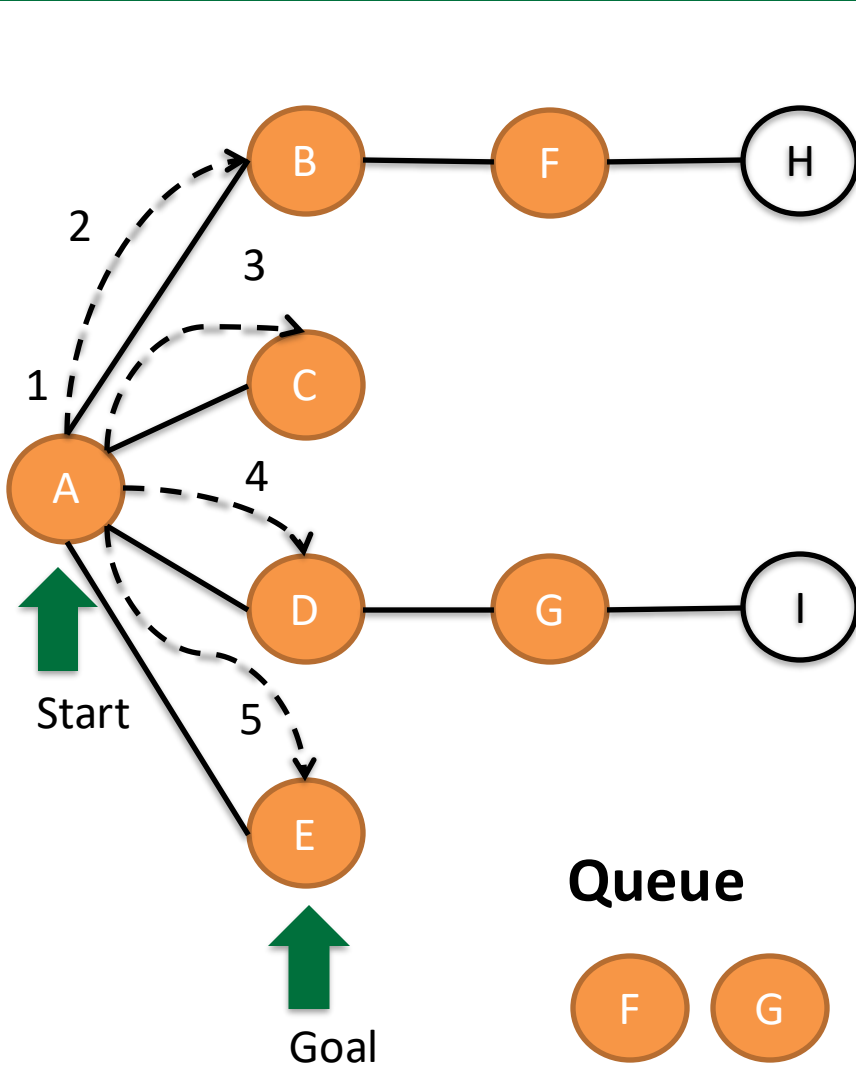
```
enqueue(s) //start node
s.visited = true
repeat until find goal vertex or
queue empty:
    u = dequeue()
    (do something here)
    for v ∈ u.adjacent
        if !v.visited
            v.visited = true
            enqueue(v)
```

Keep going to further illustrate BFS process

Queue



Breadth First Search (BFS) finds shortest path between *start* and other nodes

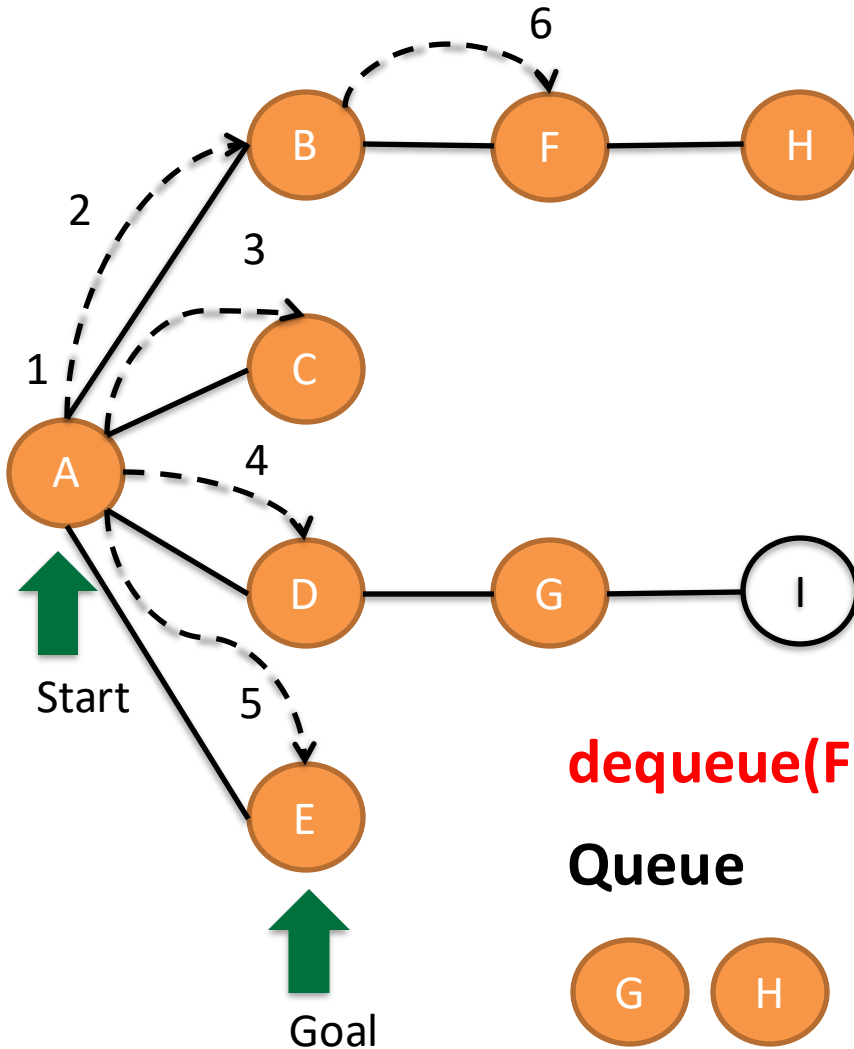


BFS algorithm

```
enqueue(s) //start node
s.visited = true
repeat until find goal vertex or
queue empty:
    u = dequeue()
    (do something here)
    for v ∈ u.adjacent
        if !v.visited
            v.visited = true
            enqueue(v)
```

Notice that all nodes 1 step away are visited before any node 2 steps away is visited

Breadth First Search (BFS) finds shortest path between *start* and other nodes



BFS algorithm

```
enqueue(s) //start node  
s.visited = true  
repeat until find goal vertex or  
queue empty:
```

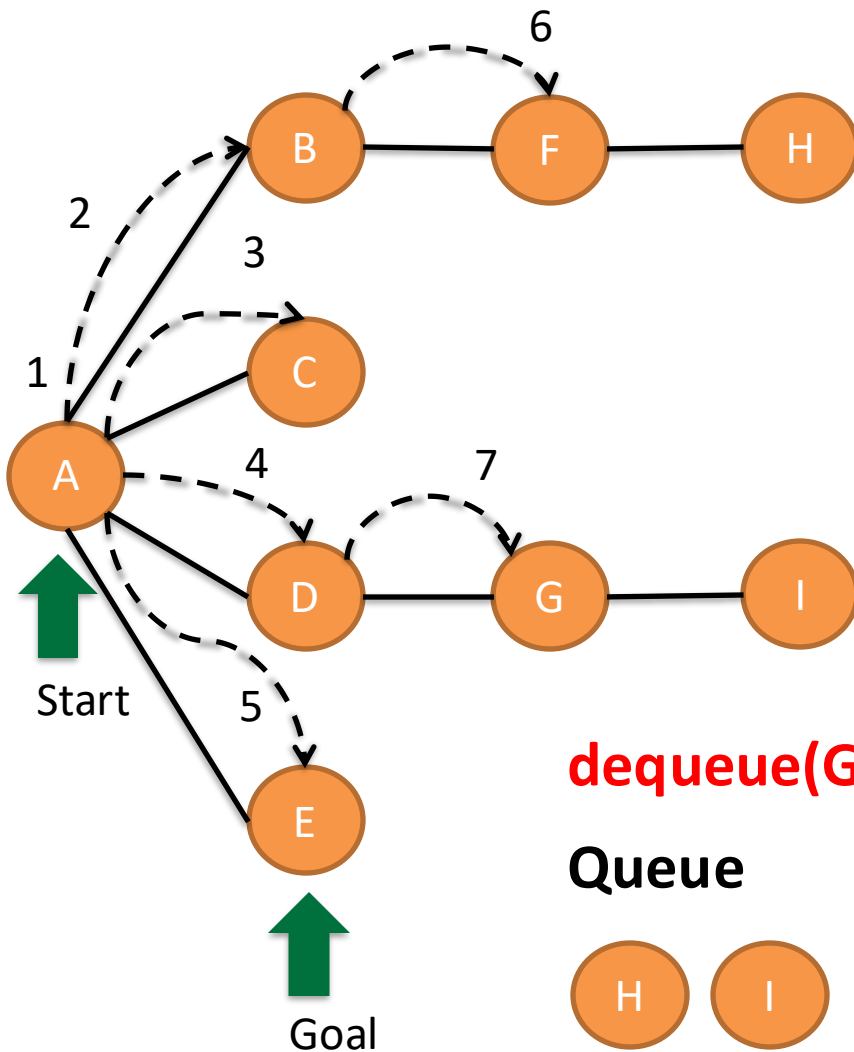
```
    → u = dequeue()  
    (do something here)  
    for v ∈ u.adjacent  
        if !v.visited  
            v.visited = true  
            enqueue(v)
```

dequeue(F), enqueue unvisited adjacent H

Queue



Breadth First Search (BFS) finds shortest path between *start* and other nodes



BFS algorithm

```
enqueue(s) //start node
s.visited = true
repeat until find goal vertex or
queue empty:
```

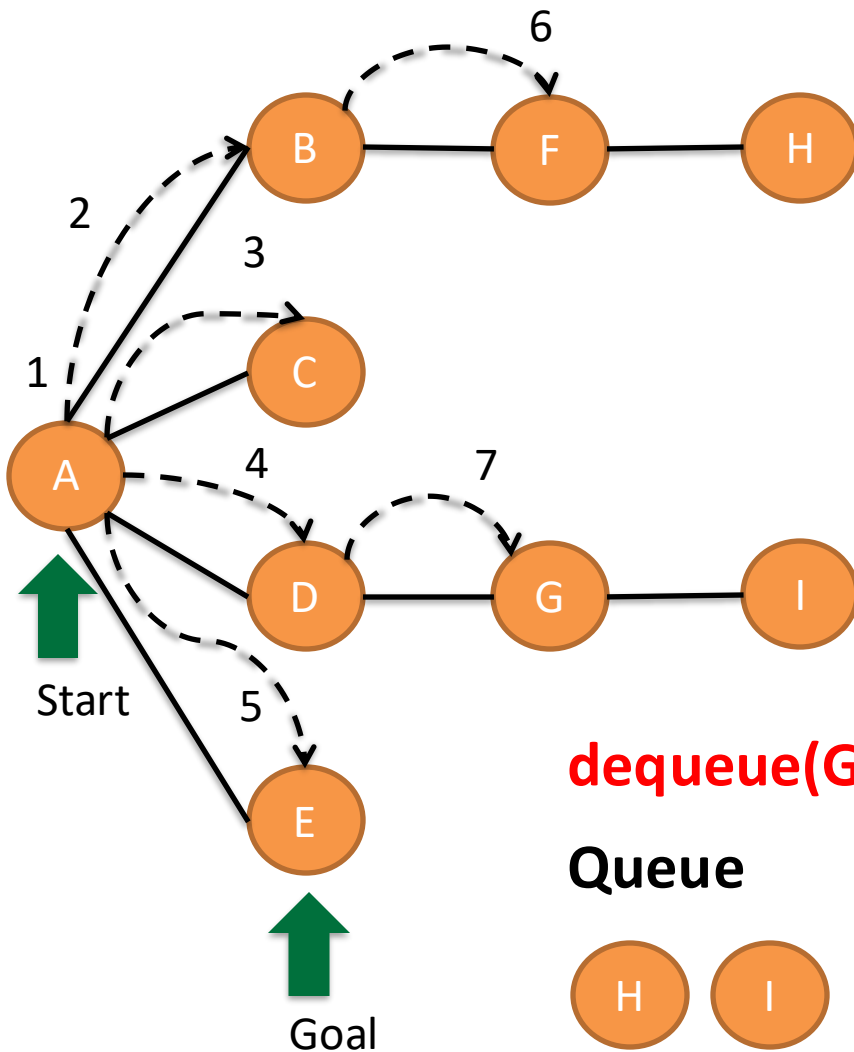
```
    u = dequeue()
    (do something here)
    for v ∈ u.adjacent
        if !v.visited
            v.visited = true
            enqueue(v)
```

dequeue(G), enqueue unvisited adjacent I

Queue



Breadth First Search (BFS) finds shortest path between *start* and other nodes



BFS algorithm

```
enqueue(s) //start node
s.visited = true
repeat until find goal vertex or
queue empty:
```

```
    u = dequeue()
    (do something here)
    for v ∈ u.adjacent
        if !v.visited
            v.visited = true
            enqueue(v)
```

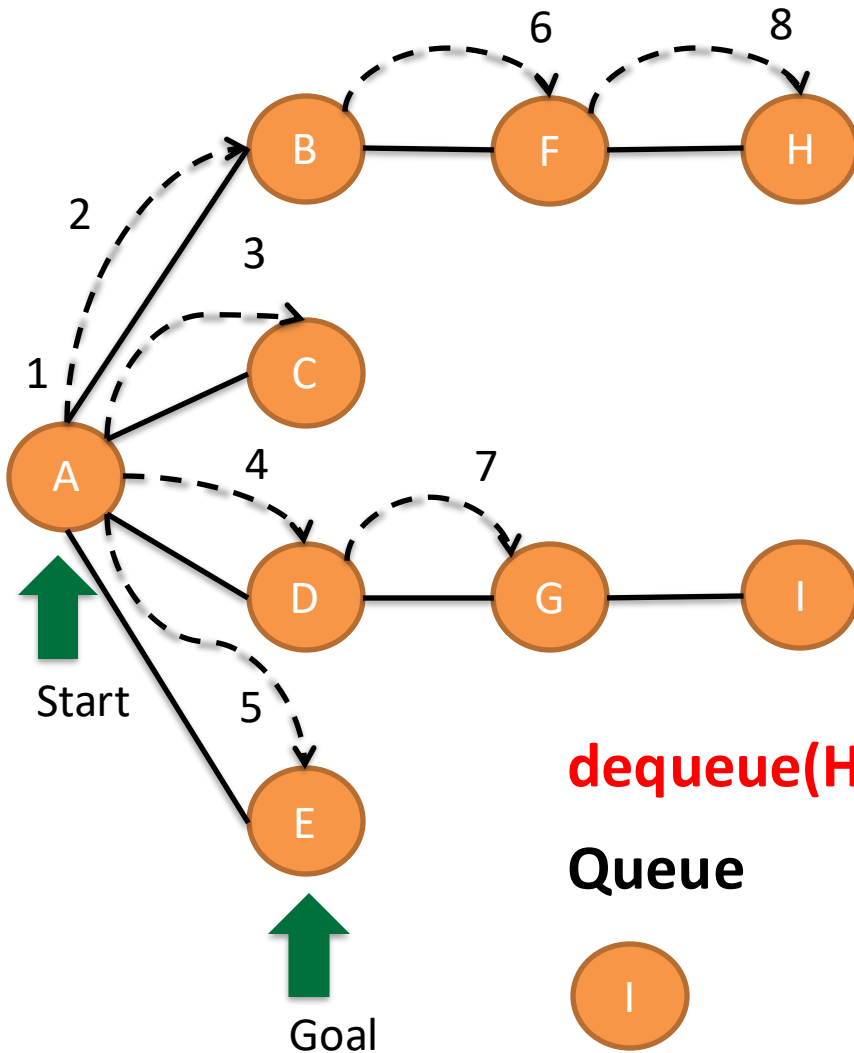
dequeue(G), enqueue unvisited adjacent I

Queue



Notice that all nodes 2 steps away are visited before any node 3 steps away is visited

Breadth First Search (BFS) finds shortest path between *start* and other nodes



---> Order nodes visited

BFS algorithm

```
enqueue(s) //start node  
s.visited = true  
repeat until find goal vertex or  
queue empty:
```

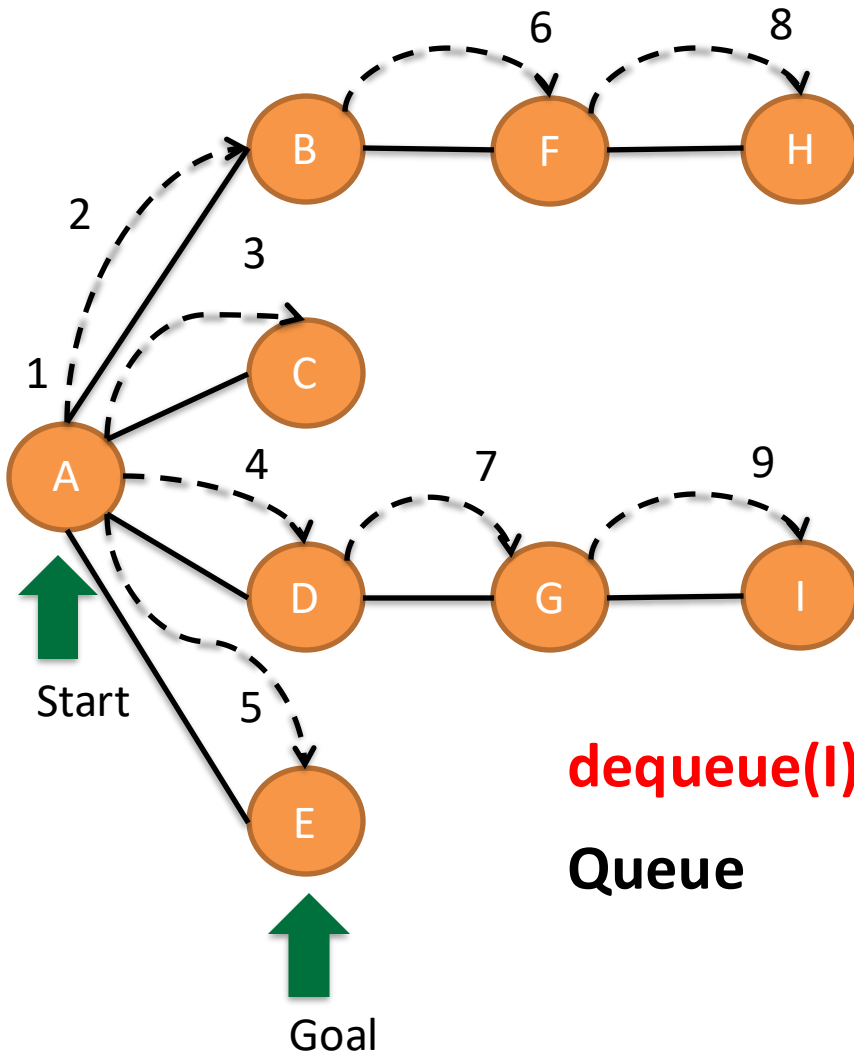
```
    u = dequeue()  
    (do something here)  
    for v ∈ u.adjacent  
        if !v.visited  
            v.visited = true  
            enqueue(v)
```

dequeue(H), enqueue unvisited adjacent (none)

Queue



Breadth First Search (BFS) finds shortest path between *start* and other nodes



BFS algorithm

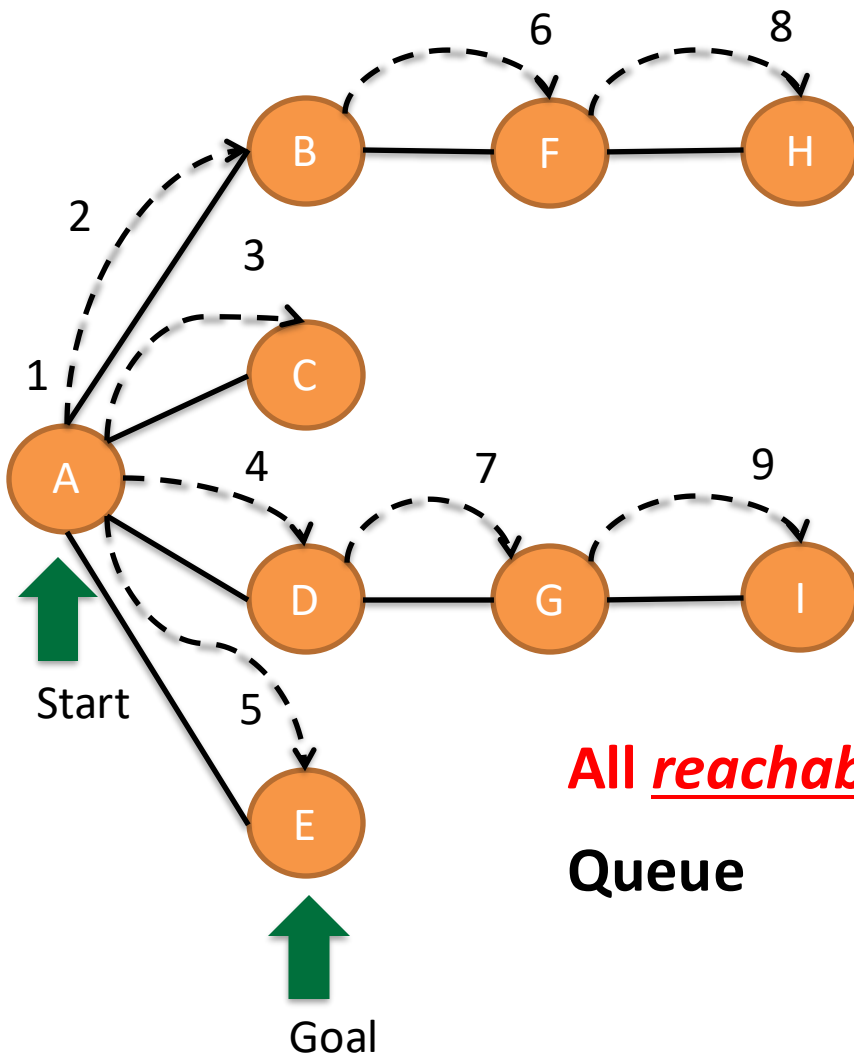
```
enqueue(s) //start node  
s.visited = true  
repeat until find goal vertex or  
queue empty:
```

```
    u = dequeue()  
    (do something here)  
    for v ∈ u.adjacent  
        if !v.visited  
            v.visited = true  
            enqueue(v)
```

dequeue(I), enqueue unvisited adjacent (none)

Queue

Breadth First Search (BFS) finds shortest path between *start* and other nodes



BFS algorithm

```
enqueue(s) //start node
s.visited = true
repeat until find goal vertex or
queue empty:
    u = dequeue()
    (do something here)
    for v ∈ u.adjacent
        if !v.visited
            v.visited = true
            enqueue(v)
```

All reachable nodes from *start* explored

Queue

Node discovery tells us something about the graph

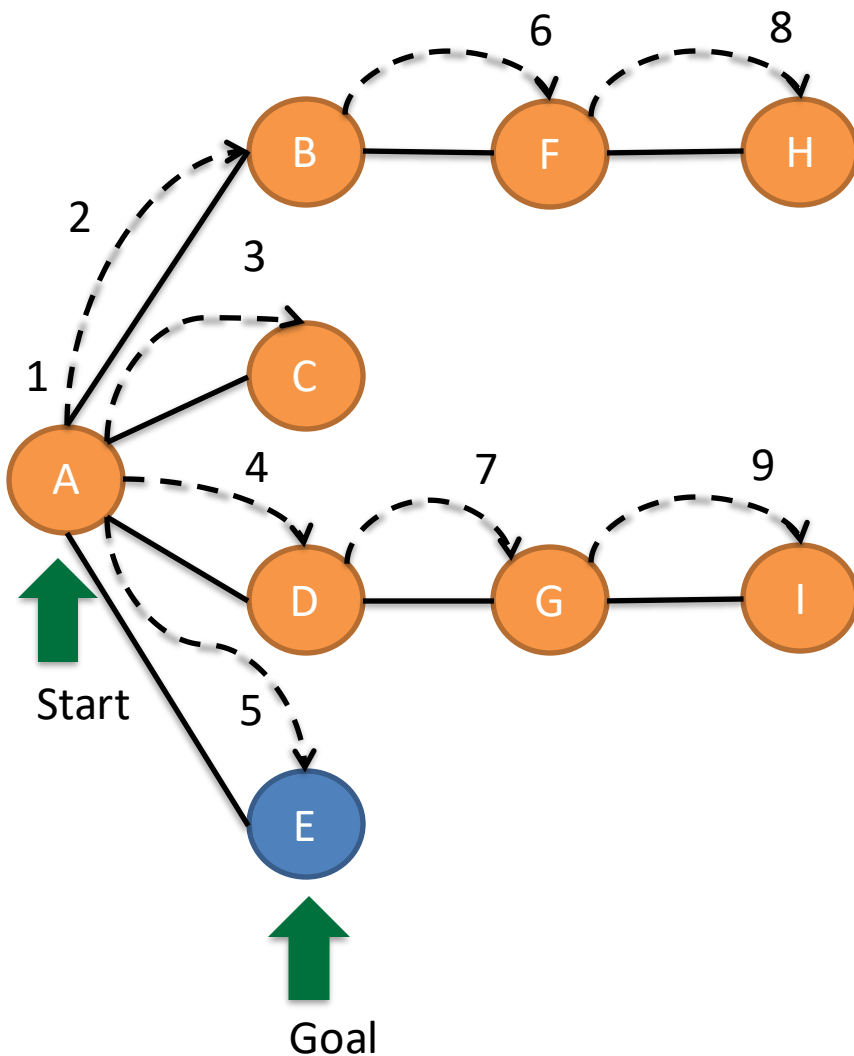
Discovery edges

- Edges that lead to unvisited nodes called *discovery edges*
- Discovery edges form a tree on the graph (root, no cycles)
- Can traverse from *start* to *goal* on tree (if goal reachable)
- Can tell us which nodes are not reachable (not on path formed by discovery edges)
- **Path guaranteed to have smallest number of edges**

Can track how we got to node to find shortest path

- Keep track of parent vertex
- Parent of each vertex is vertex that discovered it
- Parent is unique because we don't visit vertices twice

To find path from *start* to *goal*, keep track of previous node as nodes are “discovered”



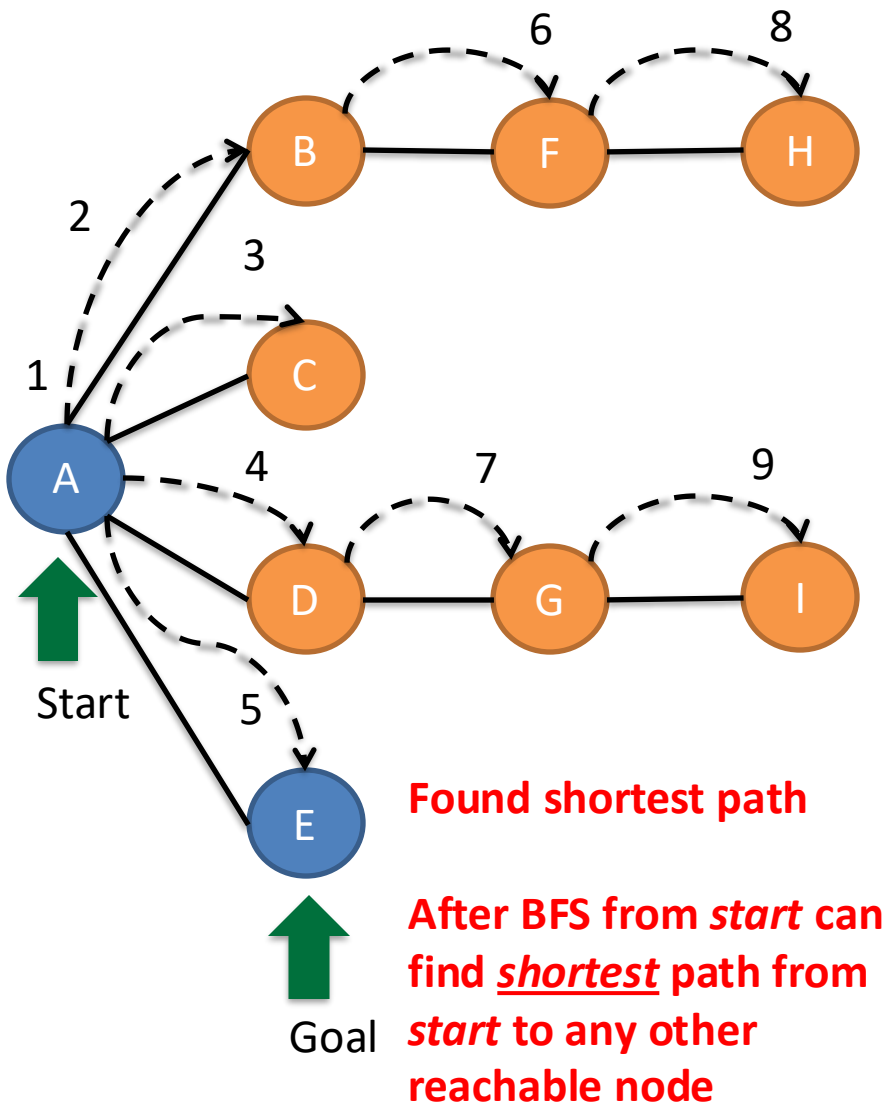
Path from *start* to *goal*

1. Do BFS from *start*
 - When node *discovered*, record previous node
 - Could keep Map with node as Key and previous as Value
2. After BFS complete, find path on Map
 - Begin at *goal* node
 - Track backward on Map until find *start* node
 - **Will find shortest path if it exists**

Path A to E

Key	Value
A	Null
B	A
C	A
D	A
E	A
F	B
G	D
H	F
I	G

To find path from *start* to *goal*, keep track of previous node as nodes are “discovered”



Path from *start* to *goal*

- Do BFS from *start*
 - When node *discovered*, record previous node
 - Could keep Map with node as Key and previous as Value
- After BFS complete, find path on Map
 - Begin at *goal* node
 - Track backward on Map until find *start* node
 - Will find shortest path if it exists**

Path A to E

Key	Value
A	Null
B	A
C	A
D	A
E	A
F	B
G	D
H	F
I	G

Path
A,E

BFS run-time complexity is $O(n+m)$

Run time

- Assume graph with n nodes and m edges
- Visit each node at most one time due to visited indicator
- Visit each edge at most one time
- Run-time complexity $O(n+m)$
- Useful for the Kevin Bacon game (PS-4)!

GraphTraversal.java: BFS code

GraphTraversal.java


```
60 public void BFS(AdjacencyMapGraph<V,E> G, V start) {
61     System.out.println("\nBreadth First Search from " + start);
62     backtrack = new HashMap<V,V>(); //initialize backtrack
63     backtrack.put(start, null); //load start vertex with null parent
64     Set<V> visited = new HashSet<V>(); //Set to track which vertices have already been visited
65     Queue<V> queue = new LinkedList<V>(); //queue to implement BFS
66
67     queue.add(start); //enqueue start vertex
68     visited.add(start); //add start to visited Set
69     while (!queue.isEmpty()) { //loop until no more vertices
70         V u = queue.remove(); //dequeue
71         for (V v : G.outNeighbors(u)) { //loop over out neighbors
72             if (!visited.contains(v)) { //if neighbor not visited, then neighbor is discovered
73                 visited.add(v); //add neighbor to visited Set
74                 queue.add(v); //enqueue neighbor
75                 backtrack.put(v, u); //save that this vertex was discovered from prior vertex
76             }
77         }
78     }
79 }
```

- When running BFS, keep track of prior vertex when a vertex is discovered
- *backTrack* Map Key is current vertex, Value is prior (parent) vertex

BFS – given Graph G and start vertex

- Use Set to track visited vertices
- Use Queue to track which vertices to visit
- Follow pseudo code
- Add vertex to *backTrack* when discovered
- Use same *findPath()* method

Agenda

1. Depth first search (DFS)
2. Breadth first search (BFS)
-  3. Examples from last class and today

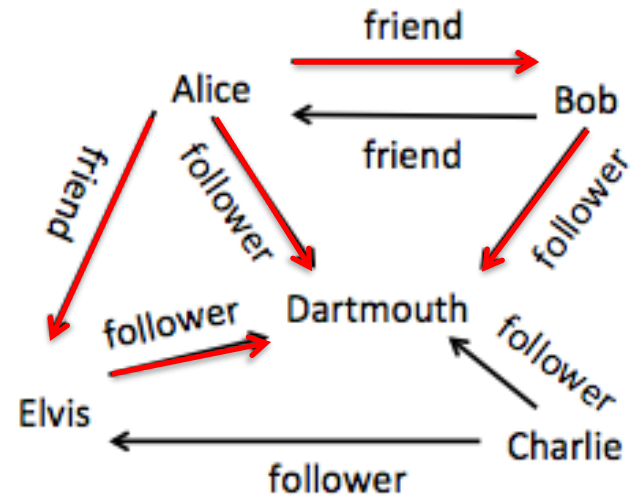
GraphTraversal.java: DFS and BFS on graph we looked at last class

```

113 public static void main(String[] args) {
114     //set up graph from class introducing Graphs
115     GraphTraversal<String,String> GT = new GraphTraversal<String,String>();
116     AdjacencyMapGraph<String,String> g = new AdjacencyMapGraph<String,String>();
117     g.insertVertex("Alice");
118     g.insertVertex("Bob");
119     g.insertVertex("Charlie");
120     g.insertVertex("Dartmouth");
121     g.insertVertex("Elvis");
122     g.insertDirected("Alice", "Dartmouth", "follower");
123     g.insertDirected("Bob", "Dartmouth", "follower");
124     g.insertDirected("Charlie", "Dartmouth", "follower");
125     g.insertDirected("Elvis", "Dartmouth", "follower");
126     g.insertUndirected("Alice", "Bob", "friend"); // symmetric, undirected edge
127     g.insertDirected("Alice", "Elvis", "friend"); // not symmetric, directed edge!
128     g.insertDirected("Charlie", "Elvis", "follower");
129
130     //run DFS from Alice
131     GT.DFS(g, "Alice");
132     //find path from start to end
133     GT.findPath("Bob", "Dartmouth"); //DFS wasn't run from Bob, should reject this
134     GT.findPath("Alice", "Dartmouth");
135     GT.findPath("Alice", "Charlie");
136     GT.findPath("Alice", "Alice");
137
138     //run BFS
139     GT.BFS(g, "Alice");
140
141     //find path from start to end
142     GT.findPath("Alice", "Dartmouth");
143     GT.findPath("Alice", "Charlie");
144

```

Create graph



- Run DFS with start=Alice
- Find paths from Alice

Key	Value
Alice	Null
Bob	Alice
Dartmouth	Elvis
Elvis	Alice

```

Problems  Javadoc  Declaration  Console  Debug  Expressions  Error Log  Call Hierarchy
terminated: GraphTraversal [Java Application] /Library/Java/JavaVirtualMachines/jdk1.8.0_112.jdk/Contents/Home/bin/java (Feb 12, 2018, 4:31:06 PM)
Depth First Search from Alice
Run DFS or BFS on Bob before trying to find a path
Path from Alice to Dartmouth
[Alice, Elvis, Dartmouth]
Path from Alice to Charlie
No path found
Path from Alice to Alice
[Alice]

Breadth First Search from Alice
Path from Alice to Dartmouth
[Alice, Dartmouth]
Path from Alice to Charlie
No path found

```

findPath("Bob", "Dartmouth")

DFS not run from Bob

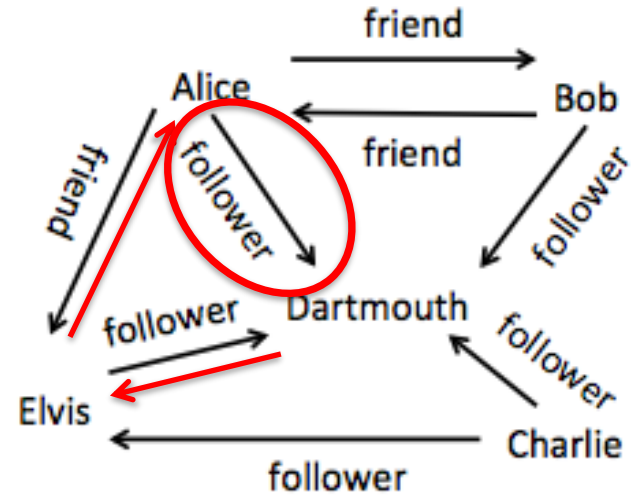
DFS was run from Alice

So do not do this search (check findPath code)

GraphTraversal.java: DFS and BFS on graph we looked at last class

```
113 public static void main(String[] args) {
114     //set up graph from class introducing Graphs
115     GraphTraversal<String,String> GT = new GraphTraversal<String,String>();
116     AdjacencyMapGraph<String,String> g = new AdjacencyMapGraph<String,String>();
117     g.insertVertex("Alice");
118     g.insertVertex("Bob");
119     g.insertVertex("Charlie");
120     g.insertVertex("Dartmouth");
121     g.insertVertex("Elvis");
122     g.insertDirected("Alice", "Dartmouth", "follower");
123     g.insertDirected("Bob", "Dartmouth", "follower");
124     g.insertDirected("Charlie", "Dartmouth", "follower");
125     g.insertDirected("Elvis", "Dartmouth", "follower");
126     g.insertUndirected("Alice", "Bob", "friend"); // symmetric, undirected edge
127     g.insertDirected("Alice", "Elvis", "friend"); // not symmetric, directed edge!
128     g.insertDirected("Charlie", "Elvis", "follower");
129
130     //run DFS from Alice
131     GT.DFS(g, "Alice");
132     //find path from start to end
133     GT.findPath("Bob", "Dartmouth"); //DFS wasn't run from Bob, should reject this
134     GT.findPath("Alice", "Dartmouth");
135     GT.findPath("Alice", "Charlie");
136     GT.findPath("Alice", "Alice");
137
138     //run BFS
139     GT.BFS(g, "Alice");
140
141     //find path from start to end
142     GT.findPath("Alice", "Dartmouth");
143     GT.findPath("Alice", "Charlie");
144 }
```

Create graph



- Run DFS with start=Alice
- Find paths from Alice

Key	Value
Alice	Null
Bob	Alice
Dartmouth	Elvis
Elvis	Alice

```
Problems Javadoc Declaration Console Debug Expressions Error Log Call Hierarchy
<terminated> GraphTraversal [Java Application] /Library/Java/JavaVirtualMachines/2k1.8.0_112.jdk/Contents/Home/bin/java (Feb 12, 2018, 4:31:06 PM)
Depth First Search from Alice
Run DFS or BFS on Bob before trying to find a path
Path from Alice to Dartmouth
[Alice, Elvis, Dartmouth]
Path from Alice to Charlie
No path found
Path from Alice to Alice
[Alice]

Breadth First Search from Alice
Path from Alice to Dartmouth
[Alice, Dartmouth]
Path from Alice to Charlie
No path found
```

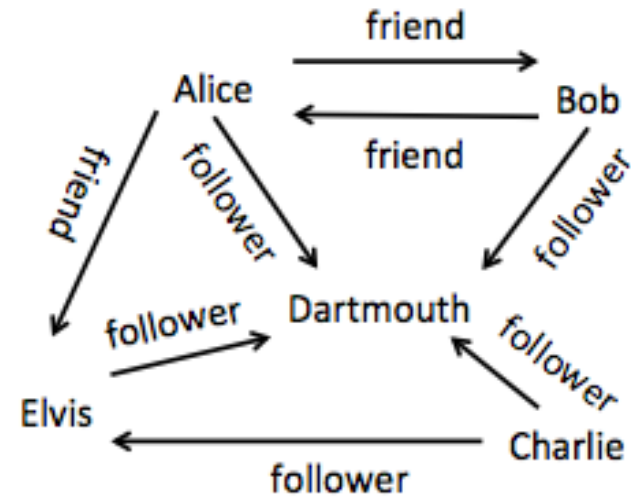
findPath("Alice", "Dartmouth") finds path Alice->Elvis->Dartmouth
Path yes, but not shortest path
Shortest is Alice->Dartmouth

GraphTraversal.java: DFS and BFS on graph we looked at last class

```
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115     GraphTraversal<String,String> GT = new GraphTraversal<String,String>();
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121     g.insertVertex("Elvis");
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124     g.insertDirected("Charlie", "Dartmouth", "follower");
125     g.insertDirected("Elvis", "Dartmouth", "follower");
126     g.insertUndirected("Alice", "Bob", "friend"); // symmetric, undirected edge
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128     g.insertDirected("Charlie", "Elvis", "follower");
129
130     //run DFS from Alice
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135     GT.findPath("Alice", "Charlie");
136     GT.findPath("Alice", "Alice");
137
138     //run BFS
139     GT.BFS(g, "Alice");
140
141     //find path from start to end
142     GT.findPath("Alice", "Dartmouth");
143     GT.findPath("Alice", "Charlie");
144 }
```

Create graph

- Run DFS with start=Alice
- Find paths from Alice



Key	Value
Alice	Null
Bob	Alice
Dartmouth	Elvis
Elvis	Alice

```
Problems Javadoc Declaration Console Debug Expressions Error Log Call Hierarchy
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Depth First Search from Alice
Run DFS or BFS on Bob before trying to find a path
Path from Alice to Dartmouth
[Alice, Elvis, Dartmouth]
Path from Alice to Charlie
No path found
Path from Alice to Alice
[Alice]

Breadth First Search from Alice
Path from Alice to Dartmouth
[Alice, Dartmouth]
Path from Alice to Charlie
No path found
```

Alice can't reach Charlie in this graph
Charlie is not in *backTrack*

GraphTraversal.java: DFS and BFS on graph we looked at last class

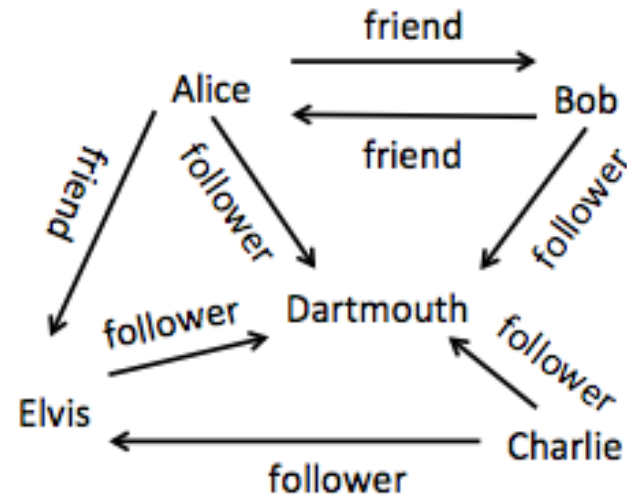
```

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114     //set up graph from class introducing Graphs
115     GraphTraversal<String,String> GT = new GraphTraversal<String,String>();
116     AdjacencyMapGraph<String,String> g = new AdjacencyMapGraph<String,String>();
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121     g.insertVertex("Elvis");
122     g.insertDirected("Alice", "Dartmouth", "follower");
123     g.insertDirected("Bob", "Dartmouth", "follower");
124     g.insertDirected("Charlie", "Dartmouth", "follower");
125     g.insertDirected("Elvis", "Dartmouth", "follower");
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140
141     //find path from start to end
142     GT.findPath("Alice", "Dartmouth");
143     GT.findPath("Alice", "Charlie");
144

```

Create graph

- Run DFS with start=Alice
- Find paths from Alice



Key	Value
Alice	Null
Bob	Alice
Dartmouth	Elvis
Elvis	Alice

```

Problems  Javadoc  Declaration  Console  Debug  Expressions  Error Log  Call Hierarchy
<terminated> GraphTraversal [Java Application] /Library/Java/JavaVirtualMachines/jdk1.8.0_112.jdk/Contents/Home/bin/java (Feb 12, 2018, 4:31:06 PM)
Depth First Search from Alice
Run DFS or BFS on Bob before trying to find a path
Path from Alice to Dartmouth
[Alice, Elvis, Dartmouth]
Path from Alice to Charlie
No path found
Path from Alice to Alice
[Alice]

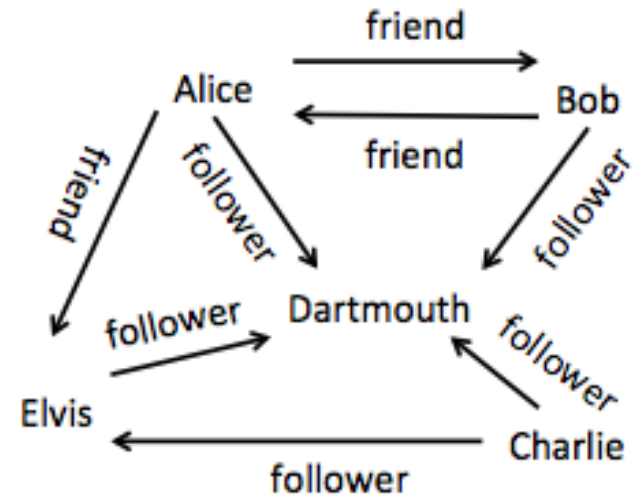
Breadth First Search from Alice
Path from Alice to Dartmouth
[Alice, Dartmouth]
Path from Alice to Charlie
No path found

```

Alice can reach herself

GraphTraversal.java: DFS and BFS on graph we looked at last class

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113 public static void main(String[] args) {
114     //set up graph from class introducing Graphs
115     GraphTraversal<String,String> GT = new GraphTraversal<String,String>();
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120     g.insertVertex("Dartmouth");
121     g.insertVertex("Elvis");
122     g.insertDirected("Alice", "Dartmouth", "follower");
123     g.insertDirected("Bob", "Dartmouth", "follower");
124     g.insertDirected("Charlie", "Dartmouth", "follower");
125     g.insertDirected("Elvis", "Dartmouth", "follower");
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138     //run BFS
139     GT.BFS(g, "Alice");
140
141     //find path from start to end
142     GT.findPath("Alice", "Dartmouth");
143     GT.findPath("Alice", "Charlie");
144 }
```



- Run BFS start=Alice

Problems Javadoc Declaration Console Debug Expressions Error Log Call Hierarchy
<terminated> GraphTraversal [Java Application] | Library/Java/JavaVirtualMachines/jdk1.8.0_112.jdk/Contents/Home/bin/java (Feb 12, 2018, 4:31:06 PM)

Depth First Search from Alice
Run DFS or BFS on Bob before trying to find a path

Path from Alice to Dartmouth

[Alice, Elvis, Dartmouth]

Path from Alice to Charlie

No path found

Path from Alice to Alice

[Alice]

Breadth First Search from Alice

Path from Alice to Dartmouth

[Alice, Dartmouth]

Path from Alice to Charlie

No path found

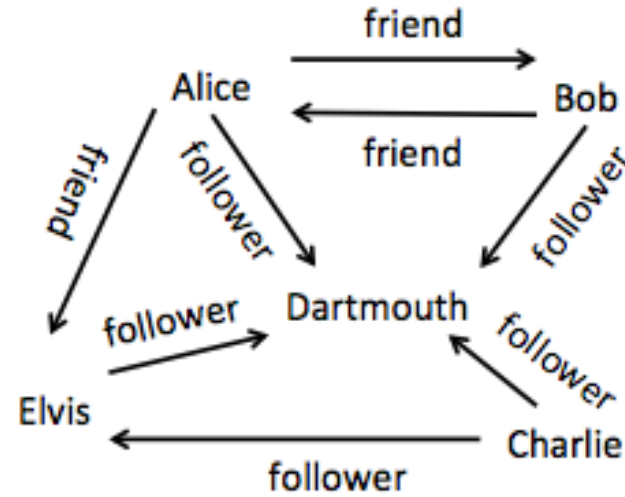
GraphTraversal.java: DFS and BFS on graph we looked at last class

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113> public static void main(String[] args) {
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140
141     //find path from start to end
142     GT.findPath("Alice", "Dartmouth");
143     GT.findPath("Alice", "Charlie");
144

```

- Run BFS start=Alice



Key	Value
Alice	Null
Bob	Alice
Dartmouth	Alice
Elvis	Alice

```

Problems  Javadoc  Declaration  Console  Debug  Expressions  Error Log  Call Hierarchy
<terminated> GraphTraversal [Java Application] /Library/Java/JavaVirtualMachines/jdk1.8.0_112.jdk/Contents/Home/bin/java (Feb 12, 2018, 4:31:06 PM)
Depth First Search from Alice
Run DFS or BFS on Bob before trying to find a path
Path from Alice to Dartmouth
[Alice, Elvis, Dartmouth]
Path from Alice to Charlie
No path found
Path from Alice to Alice
[Alice]

Breadth First Search from Alice
Path from Alice to Dartmouth
[Alice, Dartmouth]
Path from Alice to Charlie
No path found

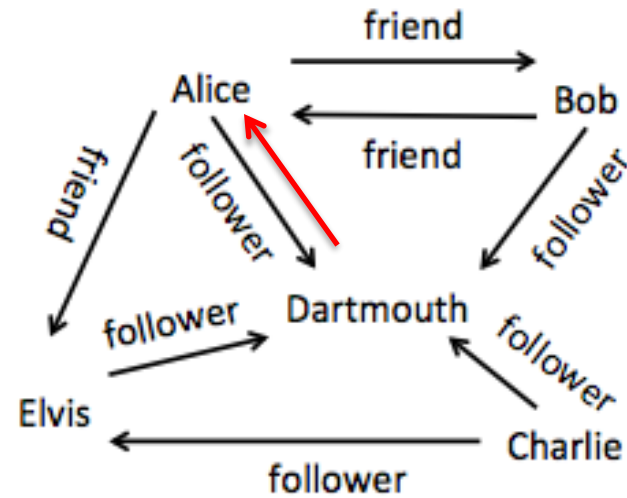
```


GraphTraversal.java: DFS and BFS on graph we looked at last class

```

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133     GT.findPath("Bob", "Dartmouth"); //DFS wasn't run from Bob, should reject this
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136     GT.findPath("Alice", "Alice");
137
138     //run BFS
139     GT.BFS(g, "Alice");
140
141     //find path from start to end
142     GT.findPath("Alice", "Dartmouth");
143     GT.findPath("Alice", "Charlie");
144

```



- Run BFS start=Alice
- Find paths from Alice

Key	Value
Alice	Null
Bob	Alice
Dartmouth	Alice
Elvis	Alice

```

Problems  Javadoc  Declaration  Console  Debug  Expressions  Error Log  Call Hierarchy
<terminated> GraphTraversal [Java Application] /Library/Java/JavaVirtualMachines/jdk1.8.0_112.jdk/Contents/Home/bin/java (Feb 12, 2018, 4:31:06 PM)
Depth First Search from Alice
Run DFS or BFS on Bob before trying to find a path
Path from Alice to Dartmouth
[Alice, Elvis, Dartmouth]
Path from Alice to Charlie
No path found
Path from Alice to Alice
[Alice]

Breadth First Search from Alice
Path from Alice to Dartmouth
[Alice, Dartmouth]
Path from Alice to Charlie
No path found

```

BFS
findPath("Alice", "Dartmouth") finds shortest path
Alice->Dartmouth (DFS went through Elvis before Dartmouth)

DFS on today's graph

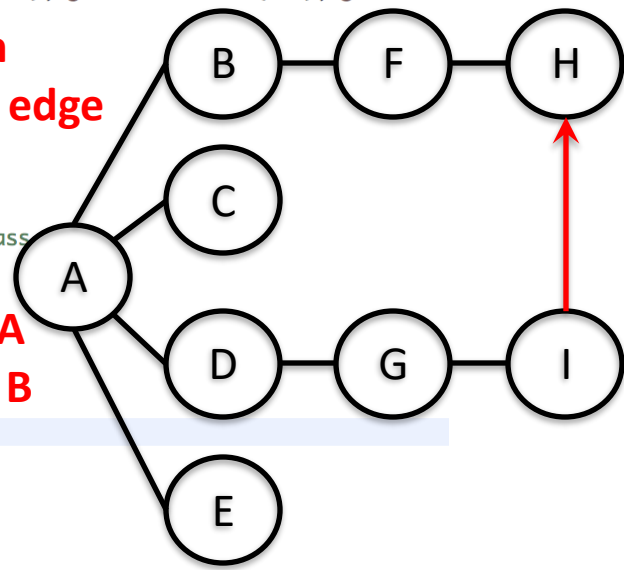
GraphTraversal.java

```

145 //set up graph from Graph Traversal class
146 AdjacencyMapGraph<String,String> g2 = new AdjacencyMapGraph<String,String>();
147 g2.insertVertex("A"); g2.insertVertex("B"); g2.insertVertex("C"); g2.insertVertex("D");
148 g2.insertVertex("E"); g2.insertVertex("F"); g2.insertVertex("G"); g2.insertVertex("H"); g2.insert
149 g2.insertUndirected("A", "B", "");
150 g2.insertUndirected("B", "F", "");
151 g2.insertUndirected("F", "H", "");
152 g2.insertUndirected("A", "C", "");
153 g2.insertUndirected("A", "D", "");
154 g2.insertUndirected("D", "G", "");
155 g2.insertUndirected("G", "I", "");
156 g2.insertUndirected("A", "E", "");
157 g2.insertDirected("I", "H", ""); //directed edge not from class
158
159 //run DFS from A and find path to H
160 GT.DFS(g2, "A");
161 GT.findPath("A", "B");
162
163 //run BFS from A and find path to H
164 GT.BFS(g2, "A");
165 GT.findPath("A", "B");
166
167 }
168
169 }
170

```

- Create graph
- Added extra edge
- Run DFS from A
- Find path A to B



DFS

Key	Value
A	Null
B	F
C	A
D	A
E	A
F	H
G	D
H	I
I	G



Depth First Search from A
 Path from A to B
 [A, D, G, I, H, F, B]

Breadth First Search from A
 Path from A to B
 [A, B]

DFS on today's graph

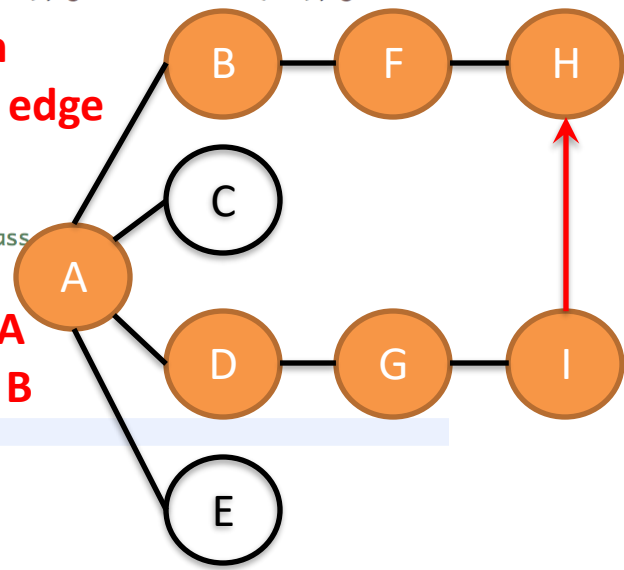
GraphTraversal.java

```

145 //set up graph from Graph Traversal class
146 AdjacencyMapGraph<String,String> g2 = new AdjacencyMapGraph<String,String>();
147 g2.insertVertex("A"); g2.insertVertex("B"); g2.insertVertex("C"); g2.insertVertex("D");
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150 g2.insertUndirected("B", "F", "");
151 g2.insertUndirected("F", "H", "");
152 g2.insertUndirected("A", "C", "");
153 g2.insertUndirected("A", "D", "");
154 g2.insertUndirected("D", "G", "");
155 g2.insertUndirected("G", "I", "");
156 g2.insertUndirected("A", "E", "");
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163 //run BFS from A and find path to H
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165 GT.findPath("A", "B");
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167 }
168
169 }
170

```

- Create graph
- Added extra edge
- Run DFS from A
- Find path A to B



DFS

Key	Value
A	Null
B	F
C	A
D	A
E	A
F	H
G	D
H	I
I	G



Depth First Search from A
 Path from A to B
 [A, D, G, I, H, F, B]

Breadth First Search from A
 Path from A to B
 [A, B]

DFS findPath("A", "B") finds path, but not shortest path!

A->D->G->I->H->F->B

Why?

DFS explores as in a maze, as far as it can go before backing up

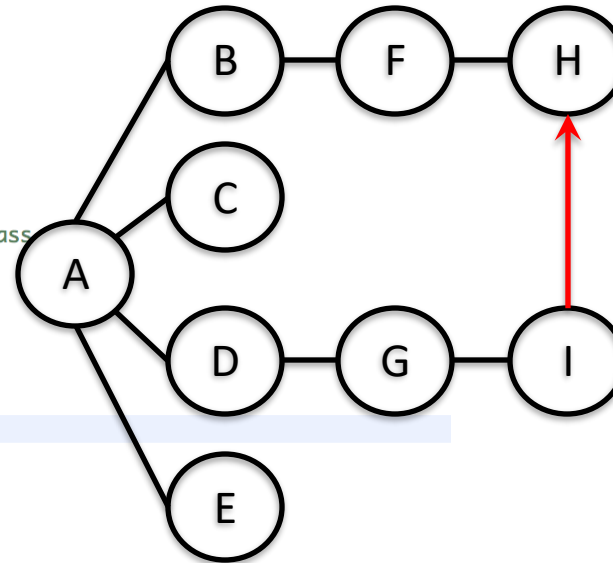
Here DFS popped D from Stack before it popped B and explored until B found

BFS on today's graph

GraphTraversal.java

```
145 //set up graph from Graph Traversal class
146 AdjacencyMapGraph<String,String> g2 = new AdjacencyMapGraph<String,String>();
147 g2.insertVertex("A"); g2.insertVertex("B"); g2.insertVertex("C"); g2.insertVertex("D");
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165 GT.findPath("A", "B");
166
167 }
168
169 }
170
```

- Run BFS
- Find path A to B



BFS

Key	Value
A	Null
B	A
C	A
D	A
E	A
F	B
G	D
H	F
I	G

Problems Javadoc Declaration Console Debug Expressions Error Log Call Hierarchy
<terminated> GraphTraversal [Java Application] /Library/Java/JavaVirtualMachines/jdk1.8.0_112.jdk/Contents/Home/bin/java (Feb 12, 2018, 5:14:16 PM)

Depth First Search from A
Path from A to B
[A, D, G, I, H, F, B]

Breadth First Search from A
Path from A to B
[A, B]

BFS on today's graph

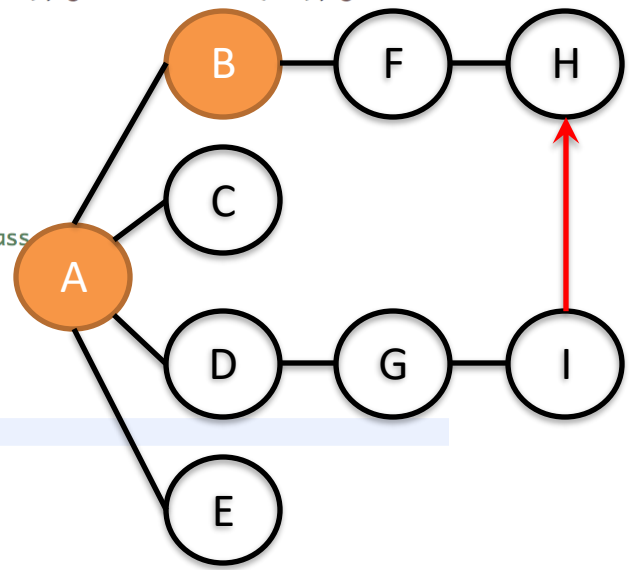
GraphTraversal.java

```

145 //set up graph from Graph Traversal class
146 AdjacencyMapGraph<String,String> g2 = new AdjacencyMapGraph<String,String>(C);
147 g2.insertVertex("A"); g2.insertVertex("B"); g2.insertVertex("C"); g2.insertVertex("D");
148 g2.insertVertex("E"); g2.insertVertex("F"); g2.insertVertex("G"); g2.insertVertex("H"); g2.insert
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165 GT.findPath("A", "B");
166
167 }
168
169 }
170

```

- Run BFS
- Find path A to B



BFS

Key	Value
A	Null
B	A
C	A
D	A
E	A
F	B
G	D
H	F
I	G



Depth First Search from A
 Path from A to B
 [A, D, G, I, H, F, B]

Breadth First Search from A
 Path from A to B
 [A, B]

BFS findPath("A", "B") finds shortest path
A->B
Why?
BFS explores outward in ripples

