

CS 55: Security and Privacy

Asymmetric encryption

ALICE SENDS A MESSAGE TO BOB
SAYING TO MEET HER SOMEWHERE.

UH HUH.

BUT EVE SEES IT, TOO,
AND GOES TO THE PLACE.

WITH YOU SO FAR.

BOB IS DELAYED, AND
ALICE AND EVE MEET.

YEAH?



I'VE DISCOVERED A WAY TO GET COMPUTER
SCIENTISTS TO LISTEN TO ANY BORING STORY.

Agenda

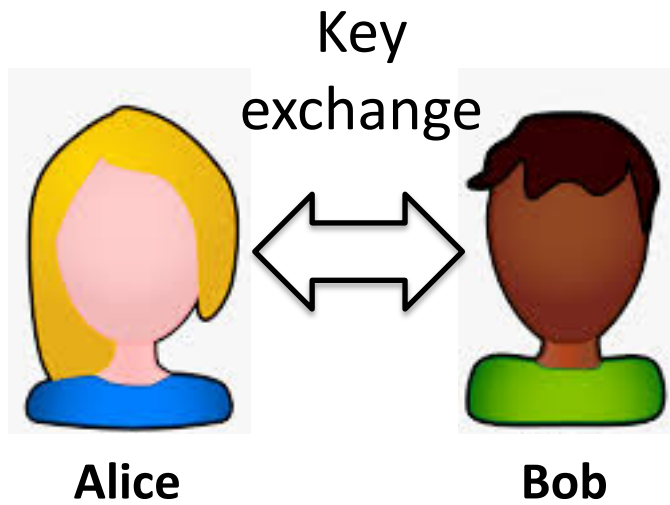
- 
1. Diffie-Helman key exchange
 2. Asymmetric encryption
 3. The RSA algorithm
 4. Digital Signatures

With symmetric key cryptography, both sender and receiver must know key

Both Alice and Bob must both know the same key for symmetric encryption

Traditionally keys distributed via paper and trusted couriers

Problematic in web age!

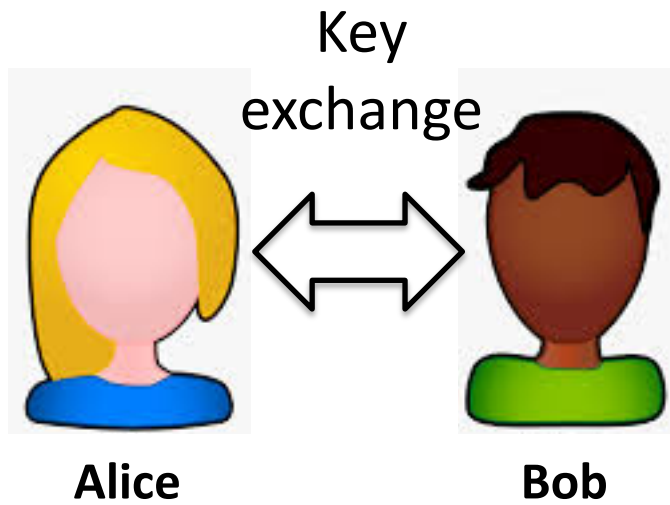


Eve

If Eve learns key, can decrypt messages

We assume Eve is always listening

Diffie-Helman (DH) allows a sender and receiver to develop the same key



Goal: develop the same key on both sides, but prevent Eve from doing the same

Then use the key for symmetric encryption (e.g., AES)

Called key agreement protocol



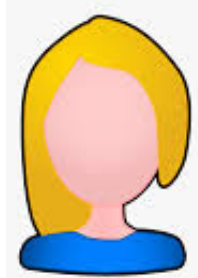
Eve

If Eve learns key, can decrypt messages

We assume Eve is always listening

NOTE: Diffie-Helman is non-authenticated (you don't know with whom you are agreeing a key)!

To get the intuition behind DH, consider mixing colors three colors



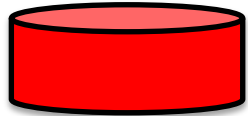
Alice



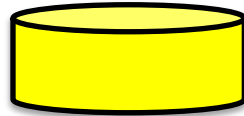
Eve



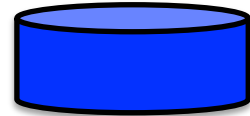
Bob



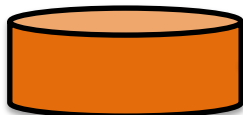
Alice picks color (private)



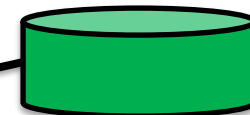
Pick color known to everyone
(Alice, Bob, and Eve)



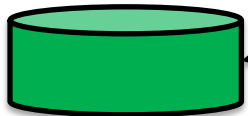
Bob picks color (private)



Private + public



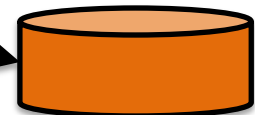
Private + public



Private
+
Bob's color

Send mixture to other
party (Eve can see)

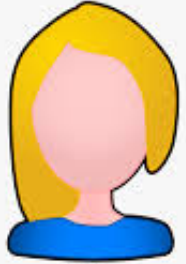
Alice and Bob have
same color, Eve cannot
make same



Private
+
Alice's color



In reality DH uses two public prime numbers and two private random numbers



Alice

Elliptic curve DH (ECDH) uses curves instead of p and g



Eve



Bob

Pick random $1 < a < p$

Alice and Bob pick public numbers g and p

- p large prime
- g small prime

Pick random $1 < b < p$

What is the problem here?
Non-authenticated, who did you agree a key with?

$g^a \bmod p$



$g^b \bmod p$



Compute
 $K = (g^b \bmod p)^a \bmod p$
 $= g^{ab} \bmod p$

Eve cannot separate x and y from g and p

Compute
 $K = (g^a \bmod p)^b \bmod p$
 $= g^{ab} \bmod p$

Now Alice and Bob know same key, can use with symmetric encryption (AES)

Test program confirms this approach allows Alice and Bob to calculate same key

diffie_helman.c

```
void main() {  
    int g = 5; //prime, known to alice, bob, eve  
    int p = 23; //prime, known to alice, bob, eve  
  
    int a = 6; //random private, known only to alice  
    int b = 15; //random private, known only to bob  
  
    //alice knows g, p, and a  
    //bob knows g, p, and b  
    //eve knows g, p  
  
    //alice sends to bob  $g^a \bmod p$   
    //bob sends to alice  $g^b \bmod p$   
    int a_to_b = (long long)(pow(g,a)) % p;  
    int b_to_a = (long long)(pow(g,b)) % p;  
    //eve sees both a_to_b and b_to_a  
  
    //alice calculates  $b\_to\_a^a \% p$   
    //bob calculates  $a\_to\_b^b \% p$   
    int alice = (long long)(pow(b_to_a,a)) % p;  
    int bob = (long long)(pow(a_to_b,b)) % p;  
  
    printf("Alice calculates %i\n",alice);  
    printf("Bob calculates %i\n",bob);  
}
```

g (small prime) and p (large prime)
to known all

Alice and Bob each pick private
random number

- Alice does not know b
- Bob does not know a
- Eve does not know either a or b

Alice sends $g^a \bmod p$ to Bob

Bob sends $g^b \bmod p$ to Alice

- Eve sees both numbers
- *Discrete log problem* says it is difficult for Eve to extract a or b from numbers she sees
- No known way to solve quickly

Alice calculates $(g^b \bmod p)^a \bmod p$

Bob calculates $(g^a \bmod p)^b \bmod p$

$= g^{ab} \bmod p$

Alice and Bob have same key, but
do not know each other's secret
Eve cannot calculate key

Each calculate 2
in this example

Agenda

1. Diffie-Helman key exchange



2. Asymmetric encryption

3. The RSA algorithm

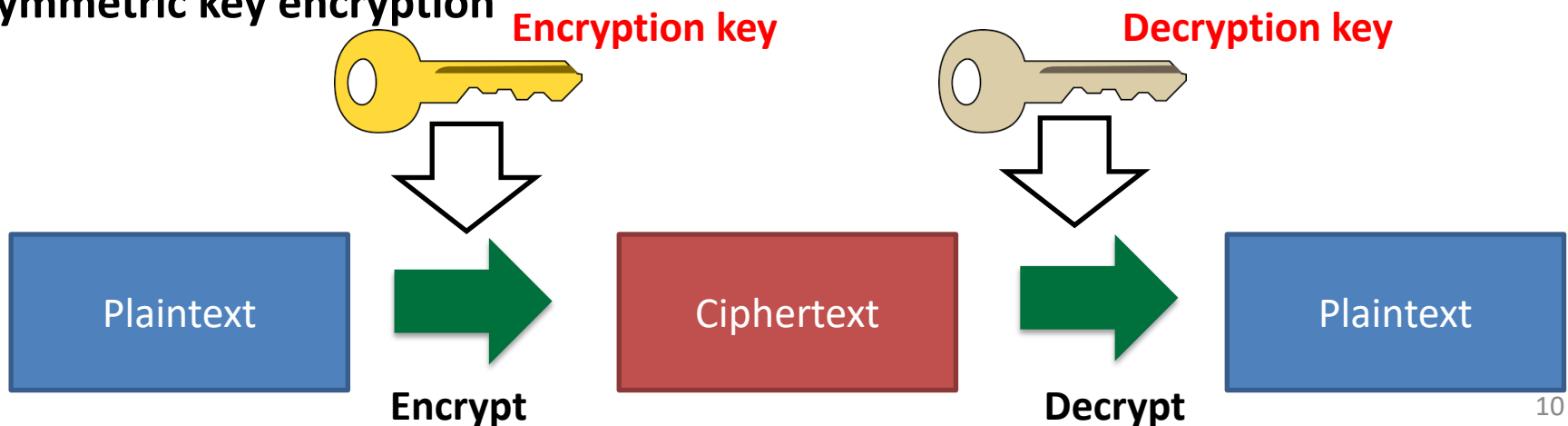
4. Digital Signatures

Asymmetric encryption uses a public and private key; symmetric only uses one key

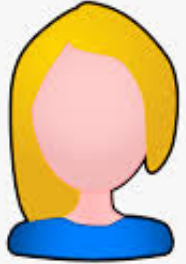
Symmetric key encryption



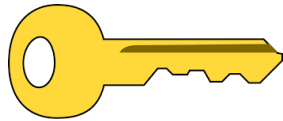
Asymmetric key encryption



Step 1: Alice creates public and private key, publishes public key; keeps private secret



Alice



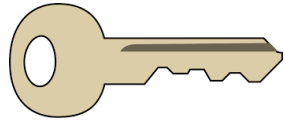
**Alice publishes
public key**



Eve



Bob

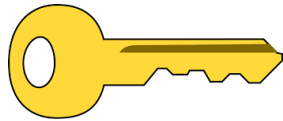


**Private key held
in secret**

Step 2: Bob gets Alice's public key



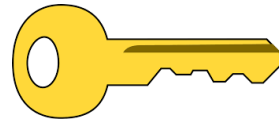
Alice



**Alice publishes
public key**



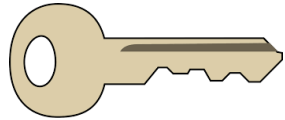
Eve



**Bob gets Alice's
public key**

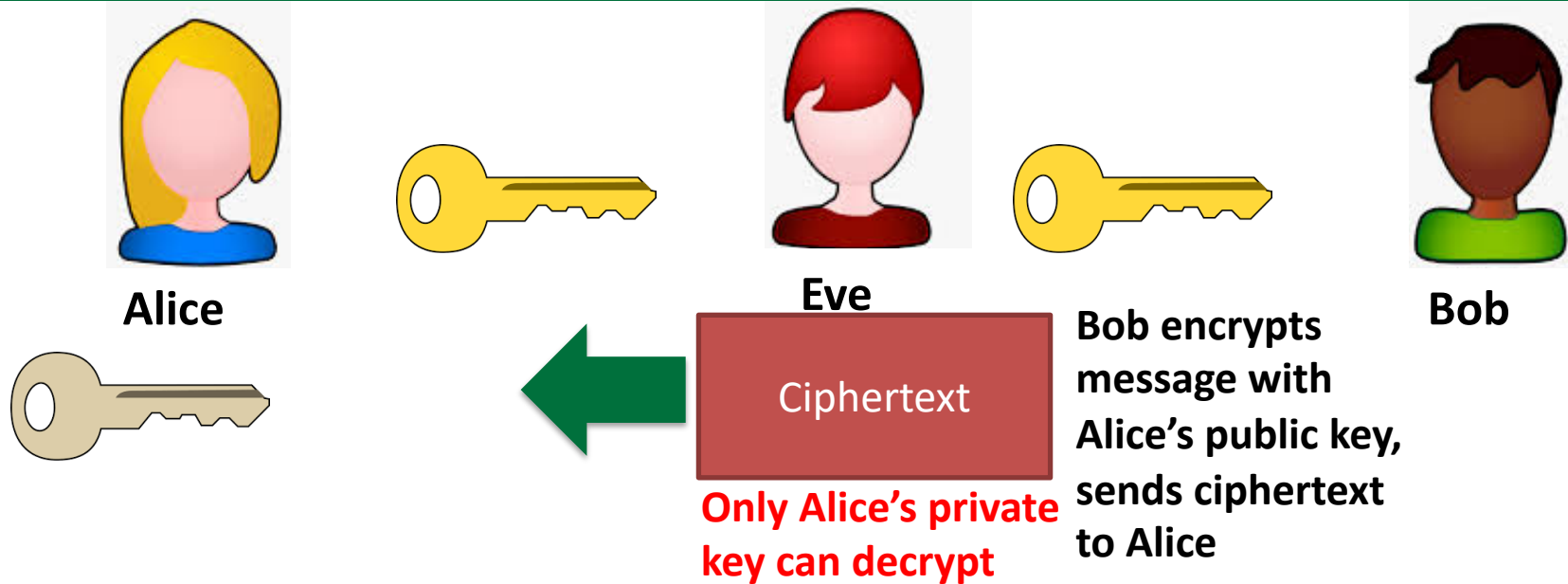


Bob

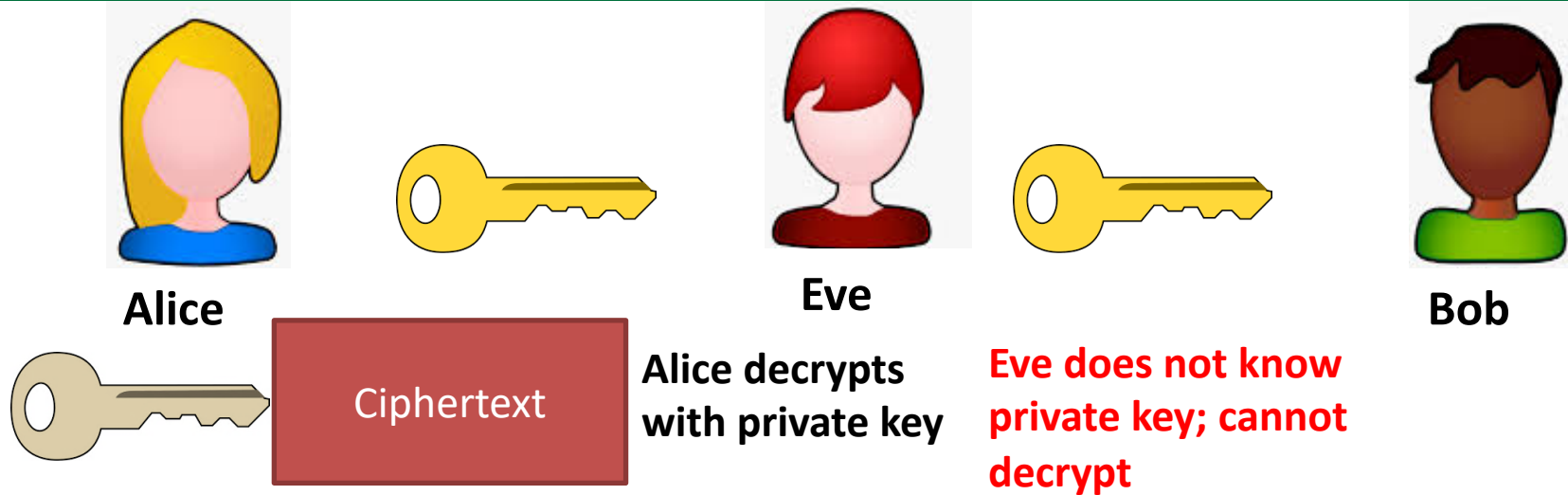


**Private key held
in secret**

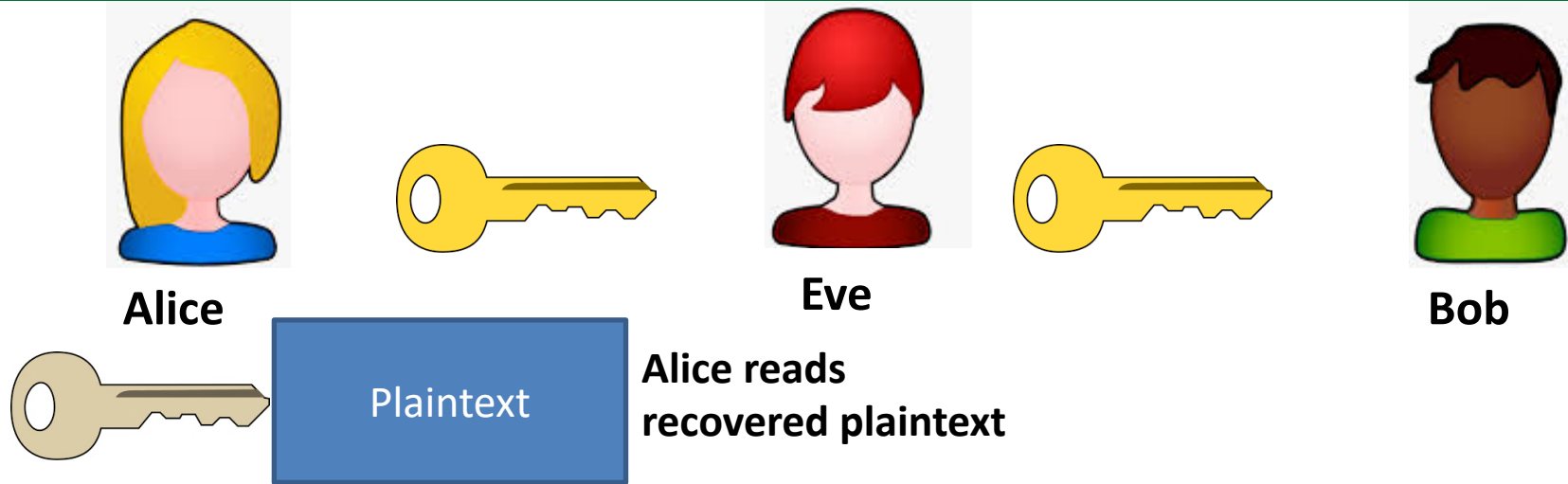
Step 3: Bob encrypts message to Alice using Alice's public key



Step 4: Alice decrypts message using private key



Step 5: Alice reads plaintext from Bob



We can tweak DH to turn it into a Public Key encryption scheme



Alice



Eve



Bob

Pick: g, p, a

Public key: $g, p, g^a \bmod p$

Private key: a

Pick: b

Works, but not used this way in practice

We use RSA instead

Send encrypted message to Alice:

- Get Alice public key = $g^a \bmod p$
- Compute $K = (g^a \bmod p)^b \bmod p = g^{ab} \bmod p$
- Use AES to encrypt $C = E(m, K)$
- Send C and $g^b \bmod p$



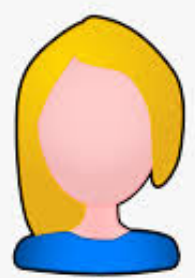
To decrypt

- $K = (g^b \bmod p)^a \bmod p = g^{ab} \bmod p$
- Use AES to decrypt $m = D(C, K)$

Agenda

1. Diffie-Helman key exchange
2. Asymmetric encryption
-  3. The RSA algorithm
4. Digital Signatures

Step 1: Alice generates a public encryption key (e, n) and private decryption key d



Alice

Key generation:

- Pick two large primes p and q
- Compute $n = pq$
- Select public encryption key e (often use $e = 65537 = 0x10001$)
- Find private decryption key d such that $ed \bmod \phi(n) = 1$
- Publish (e, n)
- Keep d secret

Choosing public key e

- Choice of e is made public (nothing to hide)
- Want e that is coprime with $\phi(n) = (p-1)(q-1)$
- In practice fix e first, often use 65537 (prime)

Choosing private key d

- Decryption key d based on choice of e , p , and q
- Solve $ed \bmod \phi(n) = 1$ (inverse e)

Implementation issues

- Will be dealing with big numbers, use **BigNum** package in C
- `sudo apt-get install libssl-dev`
- To get d , use:
`BN_mod_inverse(d, e, phi, ctx);`

The BIGNUM library in C can create public key (e, n) and private key d

rsa.c

```
BN_CTX *ctx = BN_CTX_new();  
BIGNUM *p, *q, *n, *phi, *e, *d, *m, *c, *res;  
BIGNUM *new_m, *p_minus_one, *q_minus_one;  
<snip>
```

Set up BIGNUM context

```
printf("Creating public and private keys\n");  
// Set the public key exponent e  
BN_dec2bn(&e, "65537");  
printBN("Public key (hex):", e);
```

Fix public key e as prime number
Need not be 65537, but commonly chosen

```
// Check whether  $e$  and  $(*\phi(n))$  are relatively prime.
```

```
do {
```

```
    // Generate random  $p$  and  $q$ .
```

```
    BN_generate_prime_ex(p, NBITS, 1, NULL, NULL, NULL); //random prime  $p$ 
```

```
    BN_generate_prime_ex(q, NBITS, 1, NULL, NULL, NULL); //random prime  $q$ 
```

```
    BN_sub(p_minus_one, p, BN_value_one()); // Compute  $p-1$ 
```

```
    BN_sub(q_minus_one, q, BN_value_one()); // Compute  $q-1$ 
```

```
    BN_mul(n, p, q, ctx); // Compute  $n=pq$ 
```

```
    //make sure  $e$  is relatively prime to  $\phi$ 
```

```
    BN_mul(phi, p_minus_one, q_minus_one, ctx); // Compute  $(*\phi(n))$ 
```

```
    BN_gcd(res, phi, e, ctx);
```

```
} while (!BN_is_one(res)); // try again if not relatively prime
```

```
// Compute the private key exponent  $d$ , s.t.  $ed \bmod \phi(n) = 1$ 
```

```
BN_mod_inverse(d, e, phi, ctx);
```

```
printBN("Private key (hex):", d);
```

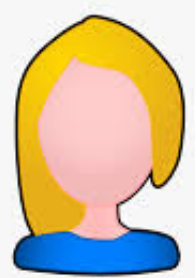
Calculate random
large primes p and q

Calculate $p-1, q-1$,
and n

Ensure e and $\phi(n) = (p-1)(q-1)$
are coprime ($\gcd == 1$)

Calculate d as inverse of e
(d undoes e 's encryption)
Solves $ed \bmod \phi(n) = 1$

Step 2: Create ciphertext by converting message to number, then raise to e



Alice

Key generation:

- Pick two large primes p and q
- Compute $n = pq$
- Select public encryption key e
(often use $e = 65537 = 0x10001$)
- Find private decryption key d such
that $ed \bmod \phi(n) = 1$
- Publish (e, n)
- Keep d secret



Bob

2) Create ciphertext

- Get Alice's public key e and n
- Convert message to number m (string of hex numbers)
- Calculate ciphertext:
$$c = m^e \bmod n$$
- Send c to Alice

BIGNUM can create ciphertext from message using recipient's public key (e, n)

rsa.c

Convert message to send to number m (here a hex string based on characters in msgToSend)

// Encryption: calculate $m^e \bmod n$

```
printf("\nEncrypting message: %s\n", msgToSend);
```

```
char *msgHex = convertStringtoHex(msgToSend); //convert msgToSend to hex
```

```
BN_hex2bn(&m, msgHex);
```

```
BN_mod_exp(c, m, e, n, ctx); //encrypt with public key e and n
```

```
printBN("Encryption result:", c);
```

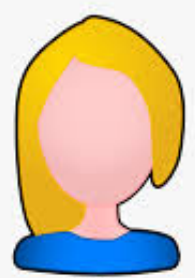
Concatenates character hex values into long string m
Create m in BIGNUM

Calculate ciphertext
 $c = m^e \bmod n$

- If *Bob* sending to *Alice* use *Alice's* published e and n
- If *Alice* sending to *Bob*, use *Bob's* published e and n

```
char *convertStringtoHex(char *msg) {  
    const int len = strlen(msg);  
    char *hex = malloc((len+1)*sizeof(char)*2);  
  
    for (int i = 0, j = 0; i < len; ++i, j += 2)  
        sprintf(hex + j, "%02x", msg[i] & 0xff);  
    return hex;  
}
```

Step 3: Use d to decrypt ciphertext C



Alice

Key generation:

- Pick two large primes p and q
- Compute $n = pq$
- Select public encryption key e
(often use $e = 65537 = 0x10001$)
- Find private decryption key d such
that $ed \bmod \phi(n) = 1$
- Publish (e, n)
- Keep d secret

3) Decrypt c using d

- Calculate $m = c^d \bmod n = (m^e \bmod n)^d \bmod n = m^{ed} \bmod n = m$



Bob

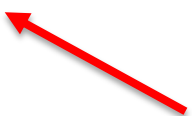
2) Create ciphertext

- Get Alice's public key e and n
- Convert message to number m (string of hex numbers)
- Calculate ciphertext:
$$c = m^e \bmod n$$
- Send c to Alice

BIGNUM can decrypt ciphertext C using private key d

```
rsa.c // Decryption: calculate  $c^d \bmod n$   Use private decryption key  $d$  to recover message  $m$ 
BN_mod_exp(new_m, c, d, n, ctx); //decrypt with private key d
printBN("Decryption result:", new_m);
char *string = BN_bn2hex(new_m);
char *recovered_message = convertHexToString(string);  Convert hex back to string
printf("Decrypted message: %s\n", recovered_message);

// Clear the sensitive data from the memory
BN_clear_free(p); BN_clear_free(q); BN_clear_free(d);
BN_clear_free(phi); BN_clear_free(m); BN_clear_free(new_m);
BN_clear_free(c); BN_clear_free(res);
BN_clear_free(p_minus_one); BN_clear_free(q_minus_one);

char *convertHexToString(char *hex) {  Don't leave crypto info lying around in memory!!
    const int len = strlen(hex);
    char *string = malloc((len/2+1)*sizeof(char));
    for (int i = 0, j = 0; j < len; ++i, j += 2) {
        int val[1];
        sscanf(hex + j, "%2x", val);
        string[i] = val[0];
        string[i + 1] = '\0';
    }
    return string; }
```

Use BIGNUM's methods to clear memory

OpenSSL can create public and private keys from the command line instead of in C

```
$ openssl genrsa -aes128 -out privateKey.pem 1024
```

```
Generating RSA private key, 2048 bit long modulus
```

```
.....+++
```

```
.....+++
```

```
e is 65537 (0x10001)
```

```
Enter pass phrase for privateKey.pem:
```

```
Verifying - Enter pass phrase for privateKey.pem:
```

Size of private key in bits

**Store key in file called
privateKey.pem**

**Encrypt output file with 128-bit
AES (using password
prompted – here cs55)**

**If this option not selected,
key file is not password
protected**

**.pem format stores data in
Base64 encoding**

Examine the contents of the key file (.pem) using OpenSSL's rsa command

```
$openssl rsa -in privateKey.pem -noout -text
```

```
Enter pass phrase for privateKey.pem:
```

```
Private-Key: (1024 bit)
```

```
modulus:
```

```
00:b3:b8:1e:de:de:2f:91:a1:00:c3:f0:4b:73:5d:...<snip>
```

```
publicExponent: 65537 (0x10001)
```

```
privateExponent:
```

```
00:8a:c0:ae:64:d7:19:d6:cf:7d:2d:c9:ca:16:e9:...<snip>
```

```
prime1:
```

```
00:de:c7:8b:8f:67:45:59:dd:f9:8f:65:dd:8b:87:...<snip>
```

```
prime2:
```

```
00:ce:84:c7:93:8b:20:d0:3c:35:9b:d6:01:cf:05:...<snip>
```

```
exponent1:
```

```
00:9b:81:0a:47:b5:3c:51:78:82:64:b8:24:26:ea:...<snip>
```

```
exponent2:
```

```
00:bd:9f:3f:5c:e2:ff:63:14:15:a9:1b:ec:17:39:...<snip>
```

```
coefficient:
```

```
00:a3:c0:5d:0e:5d:52:db:a1:d8:6e:55:63:e5:b3:...<snip>
```

Do not show encrypted data

Show data in plaintext

Output data stored
in key .pem file

Public key n

Public key e

Private key d

Other values for
performance
improvement

**DO NOT share the
private key file!**

Create a public key file using the rsa command also

```
$openssl rsa -in privateKey.pem -pubout > publicKey.pem
```

Enter pass phrase for privateKey.pem:
writing RSA key



**Extract publicKey from privateKey.pem,
save in publicKey.pem**

More shows the value of the public key

```
$ openssl rsa -in privateKey.pem -pubout > publicKey.pem
```

```
Enter pass phrase for privateKey.pem:  
writing RSA key
```

**Extract publicKey from privateKey.pem,
save in publicKey.pem**



```
$ more publicKey.pem
```

```
-----BEGIN PUBLIC KEY-----
```

```
MIGfMA0GCSqGSIb3DQEBAQUAA4GNADCBiQKBgQCzuB7e3i+RoQDD8EtzXXVHi24C  
VpcXWro5BFw1gRHQIkN61A6cGEbta5KhPKTz8eqd9AihflHwRSB2U7Cna26aYK+  
e9tdyMuFt8hAEtlk2MBYmxfpw2p8pdcBznKLiLzLJt4ozsf+Fsw0NUiE2wwYI+ZG  
jLW1wJ4NM0iTm1JYjwIDAQAB
```

```
-----END PUBLIC KEY-----
```

See the entire public key



OpenSSL shows public key (n, e) in a more readable form

```
$ openssl rsa -in privateKey.pem -pubout > publicKey.pem
```

```
Enter pass phrase for privateKey.pem:  
writing RSA key
```

Extract publicKey from privateKey.pem,
save in publicKey.pem

```
$ more publicKey.pem
```

```
-----BEGIN PUBLIC KEY-----
```

```
MIGfMA0GCSqGSIb3DQEBAQUAA4GNADCBiQKBgQCzuB7e3i+RoQDD8EtzXXVHi24C  
VpcXWro5BFw1gRHQIkN61A6cGEbta5KhPKTz8eqd9AihflLHwRSB2U7Cna26aYK+  
e9tdyMuFt8hAEtlk2MBYmxfpw2p8pdcBznKLiLzLJt4ozsf+Fsw0NUiE2wwYI+ZG  
jLW1wJ4NM0iTm1JYjwIDAQAB
```

```
-----END PUBLIC KEY-----
```

See the entire public key

```
$ openssl rsa -in publicKey.pem -pubin -text -noout
```

```
Public-Key: (1024 bit)
```

```
Modulus:
```

```
00:b3:b8:1e:de:de:2f:91:a1:00:c3:f0:4b:73:5d:...<snip>
```

```
Exponent: 65537 (0x10001)
```

Get n (modulus) and e

Encrypt and decrypt data using public and private keys

```
$ echo "We attack at dawn!" > msg.txt
```



Message to encrypt/decrypt

```
$ openssl rsautl -encrypt -inkey publicKey.pem -pubin -in msg.txt -out msg.enc
```



Encrypt using
public key
(assume public
key shared with
message
sender)

Encrypt and decrypt data using public and private keys

```
$ echo "We attack at dawn!" > msg.txt
```



Message to encrypt/decrypt

```
$ openssl rsautl -encrypt -inkey publicKey.pem -pubin -in msg.txt -out msg.enc
```

```
$ xxd msg.enc
```

```
00000000: 03a5 e47f 68dc ff98 dc59 c976 ccd1 6351 ....h....Y.v..cQ
00000010: a7ab d475 c336 0530 ac77 dc4b ff87 2ba1 ...u.6.0.w.K..+.
00000020: 6c87 3937 3f76 3220 5359 9242 4c2d 0b1c l.97?v2 SY.BL-..
00000030: 7335 52f4 3609 1610 dd69 cdf6 2c2d 80de s5R.6....i.,-..
00000040: df6c ad76 0cb6 0ba8 fe0c 0d75 1c00 853b .l.v.....u...;
00000050: 5762 ce15 aa5e 3c14 f70b 95b5 a940 c4e3 Wb...^<.....@..
00000060: 56bb 4e2f c296 b9fd fb48 d617 17d9 0f05 V.N/.....H.....
00000070: 7f74 32e7 ee26 156e 5b90 21f7 617b 3f04 .t2..&.n[.!a{?.
```



Encrypt using
public key
(assume public
key shared with
message
sender)



Ciphertext unreadable

Encrypt and decrypt data using public and private keys

```
$ echo "We attack at dawn!" > msg.txt
```



Message to encrypt/decrypt

```
$ openssl rsautl -encrypt -inkey publicKey.pem -pubin -in msg.txt -out msg.enc
```

```
$ xxd msg.enc
```

```
00000000: 03a5 e47f 68dc ff98 dc59 c976 ccd1 6351 ....h....Y.v..cQ
00000010: a7ab d475 c336 0530 ac77 dc4b ff87 2ba1 ...u.6.0.w.K..+.
00000020: 6c87 3937 3f76 3220 5359 9242 4c2d 0b1c l.97?v2 SY.BL-..
00000030: 7335 52f4 3609 1610 dd69 cdf6 2c2d 80de s5R.6....i.,-..
00000040: df6c ad76 0cb6 0ba8 fe0c 0d75 1c00 853b .l.v.....u...;
00000050: 5762 ce15 aa5e 3c14 f70b 95b5 a940 c4e3 Wb...^<.....@..
00000060: 56bb 4e2f c296 b9fd fb48 d617 17d9 0f05 V.N/.....H.....
00000070: 7f74 32e7 ee26 156e 5b90 21f7 617b 3f04 .t2..&.n[.!a{?.
```



Encrypt using
public key
(assume public
key shared with
message
sender)

```
$ openssl rsautl -decrypt -inkey privateKey.pem -in msg.enc
```

```
Enter pass phrase for privateKey.pem:
We attack at dawn!
```



Decrypt with private key (also asks
for password to access private key)



Ciphertext unreadable

NOTE: does not use AES, instead uses RSA to encrypt entire message – slow
Also make sure $\text{len}(\text{msg}) > \text{len}(\text{e})$

Using RSA to encrypt a large message is slow; use it with AES

Computing ciphertext $c = m^e \bmod n$ takes a long time

- m is generally a large number (two hex digits per plaintext character), long if message is long
- Raising m to a large number e takes some time
- Result is normally too big to use *int* or *long*, need special library (BIGNUM) to calculate and store value

Computing plaintext $m = c^d \bmod n$ is also slow

Use RSA with AES for long messages m

- Generate random key K as message and exchange K using RSA
- Encrypt plaintext m with AES using random key K
- Send AES encrypted ciphertext to recipient
- Recipient decrypts using key K

There are some “gotchas” to be aware of when using RSA

RSA is deterministic

- Same plaintext always gives same ciphertext (with same keys)
- Can tell if two messages are the same
- Use AES random IV (say in CBC mode) once keys exchanged
- OpenSSL uses random padding

Poorly chosen e with short m encryptions can be easily decrypted

- If e is small (say $e=3$) and message m is short, m^e can be $< n$
- Because $c = m^e \bmod n$
 - If $m^e < n$ then mod does not matter
 - Ciphertext is simply m^e
 - Decrypt by just taking e^{th} root of m
- **Choose large e and pad m if needed!**

If same plaintext is encrypted more than e times using same e but different n , can decrypt plaintext using Chinese Remainder Theorem

Practice

1) Given

$p = \text{F7E75FDC469067FFDC4E847C51F452DF}$

$q = \text{E85CED54AF57E53E092113E62F436F4F}$

$e = \text{0D88C3}$

Compute d

2) Given

$n = \text{DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDDE3A4D0CB81629242FB1A5}$

$e = \text{010001}$ (this hex value is decimal 65537)

$M = \text{Attack at dawn!}$

Compute C

3) Given

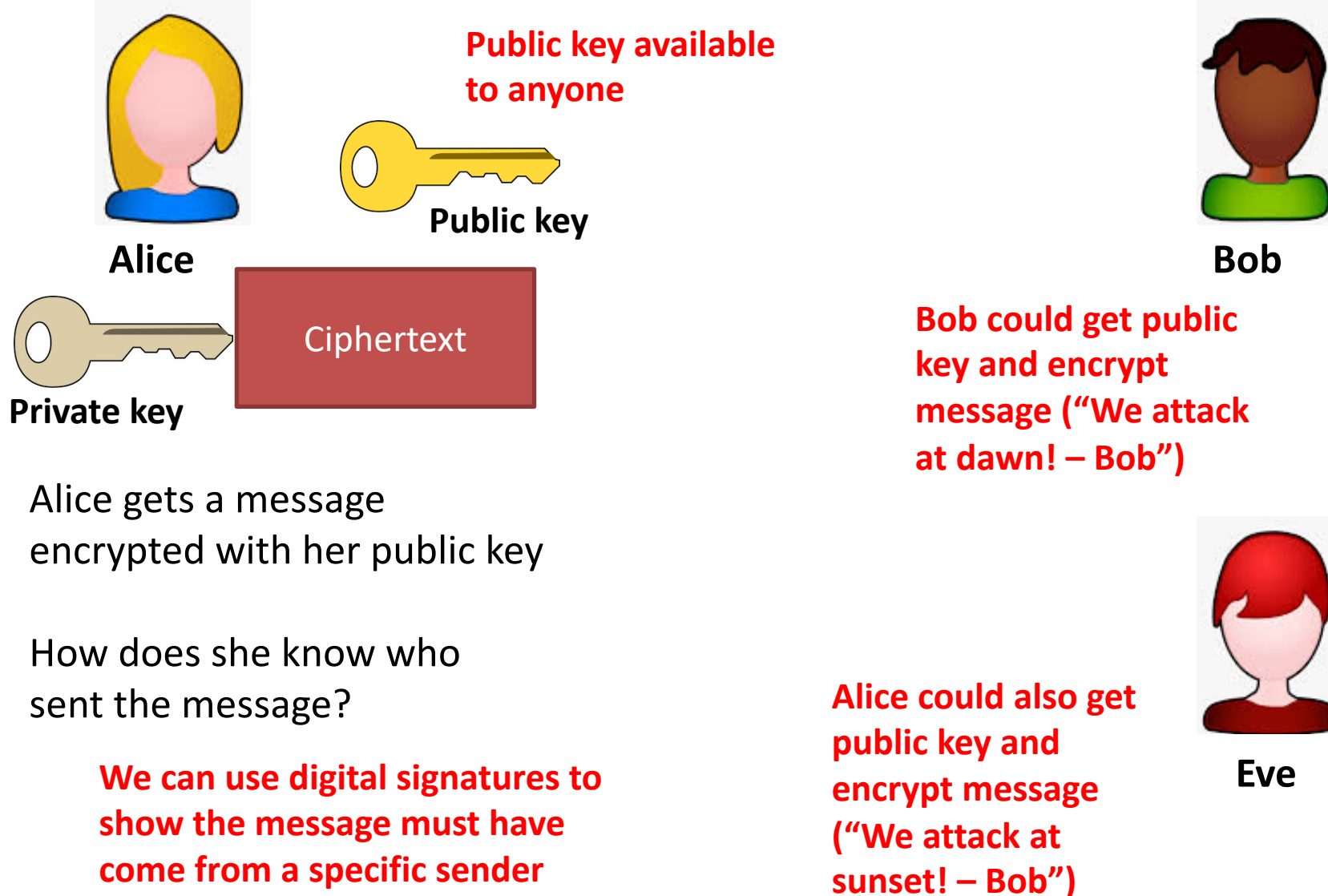
$d = \text{74D806F9F3A62BAE331FFE3F0A68AFE35B3D2E4794148AACBC26AA381CD7D30D}$

Decrypt C from part 2

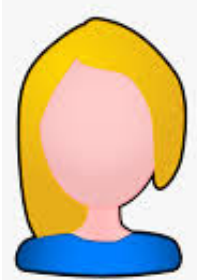
Agenda

1. Diffie-Helman key exchange
2. Asymmetric encryption
3. The RSA algorithm
-  4. Digital Signatures

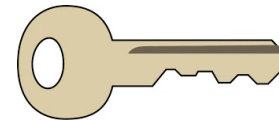
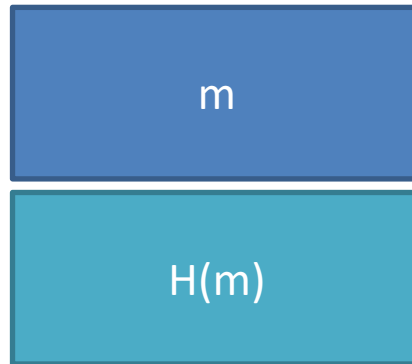
If Alice gets an encrypted message, how does she authenticate the sender?



Digital signatures can be used to ensure a message came from a specific sender



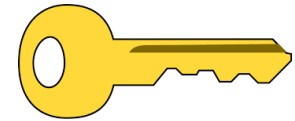
Alice



Private key



Bob

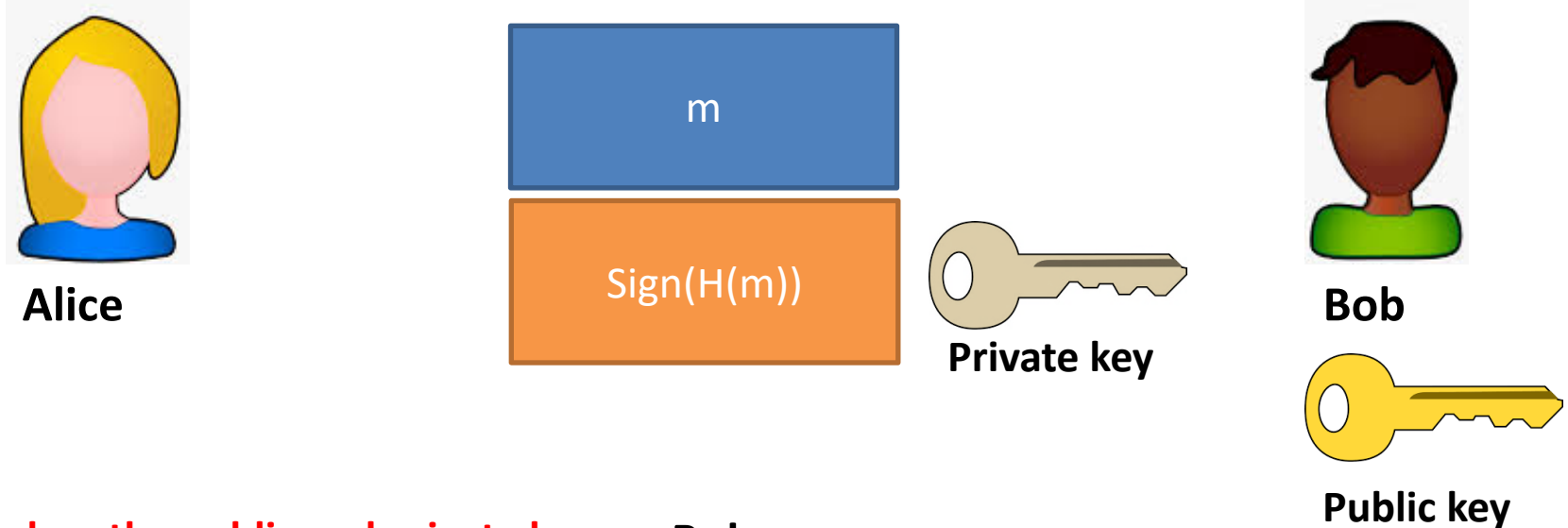


Public key

Bob

- Plaintext message m may be long
- Hash message to get small size (e.g., 256 bits)

Digital signatures can be used to ensure a message came from a specific sender



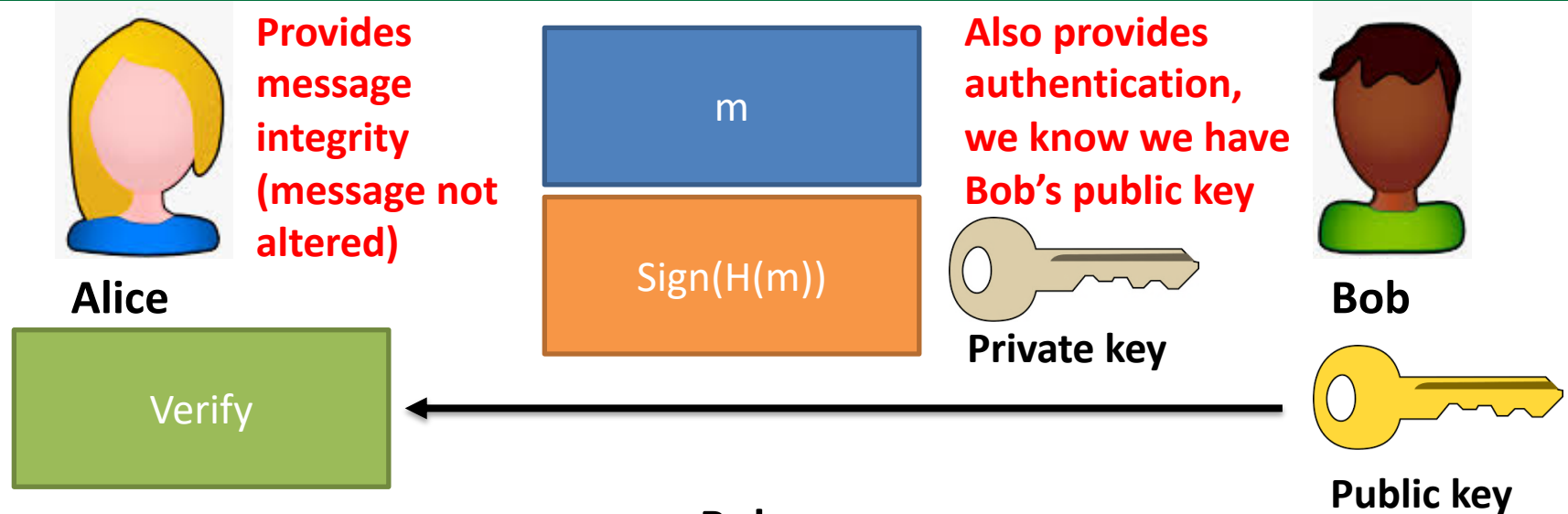
Remember, the public and private keys are inverses of each other

Order they are applied doesn't matter
 $[m^e \bmod n]^d \bmod n$ (first e, then d)
 $= [m^d \bmod n]^e \bmod n$ (first d, then e)
 $= m^{ed} \bmod n$ (both orderings give this)
 $= m$ (which is the plaintext)

Bob

- Plaintext message m may be long
- Hash message to get small size (e.g., 256 bits)
- Encrypt (sign) hash using **private** key d
- Signature $s = (H(m))^d \bmod n$
- Everyone can get back $H(m)$ using Bob's public key e , but only Bob could create s from $H(m)$
- Send plaintext message and signature to Alice
- Note: message not encrypted in this example (but it could be)

Digital signatures can be used to ensure a message came from a specific sender



Alice

- Gets plaintext message and signature from Bob
- Verify:
 - Decrypt signature using Bob's public key to get Bob's hash of plaintext (anyone can do this)
 - Alice hashes plaintext
 - See if hashes match
- Verifies unchanged msg from Bob

Bob

- Plaintext message m may be long
- Hash message to get small size (e.g., 256 bits)
- Encrypt (sign) hash using **private** key d
- Signature $s = (H(m))^d \bmod n$
- Everyone can get back $H(m)$ using Bob's public key e , but only Bob could create s from $H(m)$
- Send plaintext message and signature to Alice
- Note: message not encrypted in this example (but it could be)

Demo: Alice signs message, Bob can be assured message came from Alice

#Bob creates message

```
$ echo -n "We attack at dawn!" > msg.txt
```

```
$ cat msg.txt
```

```
We attack at dawn!
```

#Bob hashes msg.txt using sha256

```
$ openssl sha256 -binary msg.txt > msg.sha256
```

```
$ xxd msg.sha256
```

```
00000000: cdc1 866c 2088 9e65 f705 fc42 e556 7da8 ...l ..e...B.V}.
```

```
00000010: a310 dd80 fc9f 1853 84e7 8abb a669 95b0 .....S.....i..
```

Hash message -> fixed size fingerprint
of message

-binary leaves in binary form (signature
in hex form if not included)

Demo: Alice signs message, Bob can be assured message came from Alice

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```

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```

```
00000010: a310 dd80 fc9f 1853 84e7 8abb a669 95b0 .....S.....i..
```

#Bob signs hash

```
$ openssl rsautl -sign -inkey privateKey.pem -in msg.sha256 -out msg.sig
```

```
Enter pass phrase for privateKey.pem:
```

Hash message -> fixed size fingerprint
of message

-binary leaves in binary form (signature
in hex form if not included)

Sign message using private key
Signature in msg.sig

Demo: Alice signs message, Bob can be assured message came from Alice

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$ echo -n "We attack at dawn!" > msg.txt
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```
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```

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```

```
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```

```
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```

```
00000010: a310 dd80 fc9f 1853 84e7 8abb a669 95b0 .....S.....i..
```

#Bob signs hash

```
$ openssl rsautl -sign -inkey privateKey.pem -in msg.sha256 -out msg.sig
```

```
Enter pass phrase for privateKey.pem:
```

#Alice verifies hash

```
$ openssl rsautl -verify -inkey publicKey.pem -in msg.sig -pubin -raw | xxd
```

```
00000000: 0001 ffff ffff ffff ffff ffff ffff ..... 
```

```
00000010: ffff ffff ffff ffff ffff ffff ffff ..... 
```

```
<snip>
```

```
00000050: ffff ffff ffff ffff ffff ffff ff00 ..... 
```

```
00000060: cdc1 866c 2088 9e65 f705 fc42 e556 7da8 ...l ..e...B.V}.
```

```
00000070: a310 dd80 fc9f 1853 84e7 8abb a669 95b0 .....S.....i..
```

Hash message -> fixed size fingerprint of message

-binary leaves in binary form (signature in hex form if not included)

Sign message using private key
Signature in msg.sig

If msg changed,
hash will not match

Verify signature
using public key

If sig changed, will
not match hash

Match after
padding

Message must have
been sent by Bob
because only his public
key can undo the
private key encryption

We can use Python for encryption, decryption, and signatures also

rsa_encrypt.py

```
#run: python3 rsa_encrypt.py publicKey.pem ciphertext.bin
```

```
message = b'We attack at dawn!'
```

```
if __name__ == '__main__':
```

```
    #read public key and set padding to OAEP
```

```
    print("Reading public key from",sys.argv[1])
```

```
    key = RSA.importKey(open(sys.argv[1],'rb').read())
```

```
    cipher = PKCS1_OAEP.new(key) #use OAEP padding
```

```
    #encrypt message using public key
```

```
    ciphertext = cipher.encrypt(message)
```

```
    #write output file
```

```
    print("Writing output to",sys.argv[2])
```

```
    f = open(sys.argv[2],'wb')
```

```
    f.write(base64.b64encode(ciphertext))
```

```
    f.close()
```

**Encrypt a message using
message ("We attack at dawn!")
using publicKey.pem**

Store results in ciphertext.bin

We can use Python for encryption, decryption, and signatures also

rsa_decrypt.py

#run: python3 rsa_decrypt.py privateKey.pem cs55 ciphertext.bin

```
if __name__ == '__main__':  
    print("Reading ciphertext from",sys.argv[3])  
    ciphertext = open(sys.argv[3], 'rb').read()  
  
    print("Reading private key from",sys.argv[1])  
    private_key_pem = open(sys.argv[1],'rb').read()  
    private_key = RSA.importKey(private_key_pem, passphrase=sys.argv[2])  
    cipher = PKCS1_OAEP.new(private_key)  
  
    print("Decrypting ciphertext")  
    message = cipher.decrypt(base64.b64decode(ciphertext))  
  
    print("Message:",message)
```

Read ciphertext.bin
Decrypt using privateKay.pem
(using password cs55)
Print recovered message

We can use Python for encryption, decryption, and signatures also

rsa_sign.py

```
#run: python3 rsa_sign.py privateKey.pem cs55 signature.bin
```

```
message = b'An important message' #same message used in rsa_verify.py
```

```
if __name__ == '__main__':  
    print("Reading private key",sys.argv[1])  
    key_pem = open(sys.argv[1]).read()  
    key = RSA.import_key(key_pem, passphrase=sys.argv[2])
```

Sign message ("An important message") using privateKey.pem (password cs55)

```
    print("Message to sign is:",message)  
    print("Hashing message")  
    h = SHA256.new(message)
```

Store signature in signature.bin

```
    print("Signing hash")  
    signer = pss.new(key)  
    signature = signer.sign(h)
```

Note: pss is a padding scheme that adds random input

```
    print("Writing signature to",sys.argv[3])  
    open(sys.argv[3], 'wb').write(signature)
```

We can use Python for encryption, decryption, and signatures also

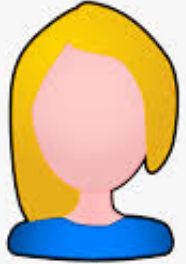
rsa_verify.py

```
#run: python3 rsa_verify.py publicKey.pem signature.bin  
message = b'An important message' #same message used in rsa_sign.py
```

```
if __name__ == '__main__':  
    print("Reading signature from",sys.argv[2])  
    signature= open(sys.argv[2], 'rb').read()  
  
    print("Reading public key from",sys.argv[1])  
    key = RSA.import_key(open(sys.argv[1]).read())  
  
    print("Hashing and verifying hash")  
    h = SHA256.new(message)  
    verifier = pss.new(key)  
    try:  
        verifier.verify(h, signature)  
        print("The signature is valid.")  
    except (ValueError, TypeError):  
        print("The signature is NOT valid.")
```

**Verify signature file
signature.bin using
publicKey.pem**

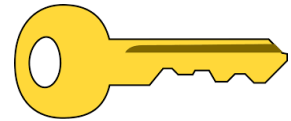
A common use of public keys is for authentication (better than passwords)



Alice



Bob



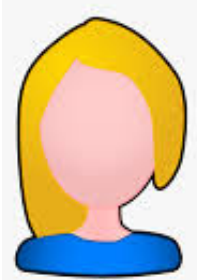
**Alice
Public key**

Bob wants to authenticate Alice

But anyone who knows Alice's password could appear to be Alice

Assume Bob knows Alice's public key

A common use of public keys is for authentication (better than passwords)



Alice

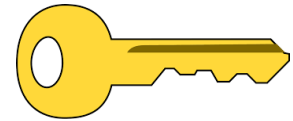
Challenge R



Bob issues random
challenge R to Alice



Bob



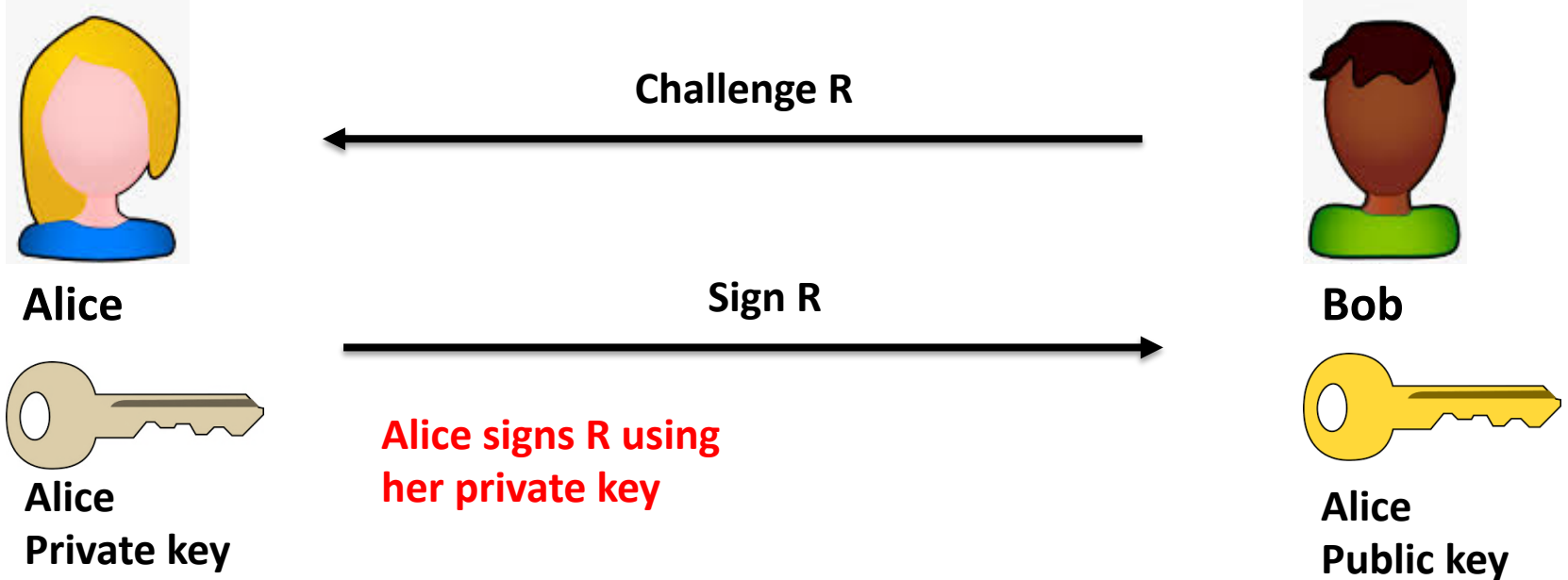
Alice
Public key

Bob wants to authenticate Alice

But anyone who knows Alice's
password could appear to be
Alice

Assume Bob knows Alice's
public key

A common use of public keys is for authentication (better than passwords)

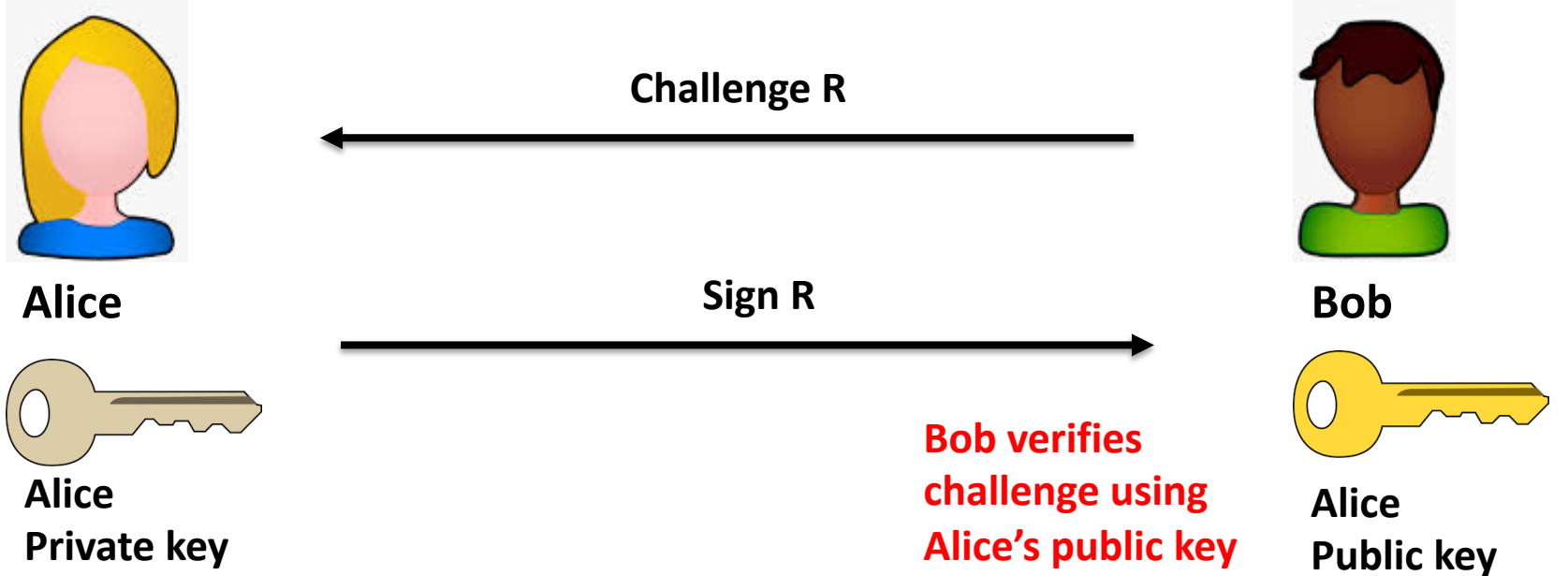


Bob wants to authenticate Alice

But anyone who knows Alice's password could appear to be Alice

Assume Bob knows Alice's public key

A common use of public keys is for authentication (better than passwords)



Now simply knowing a static password is not enough

Adversary needs the private key

Bob wants to authenticate Alice
But anyone who knows Alice's password could appear to be Alice

Assume Bob knows Alice's public key

